

First direct detection constraints on Planck-scale mass dark matter with multiple-scatter signatures using the DEAP-3600 detector

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Dark matter with Planck-scale mass ($\simeq 10^{19}$ GeV/ c^2) arises in well-motivated theories and could be produced by several cosmological mechanisms. A search for multi-scatter signals from supermassive dark matter was performed with a blind analysis of data collected over a 813 d live time with DEAP-3600, a 3.3 t single-phase liquid argon-based detector at SNOLAB. No candidate signals were observed, leading to the first direct detection constraints on Planck-scale mass dark matter. Leading limits constrain dark matter masses between 8.3×10^6 and 1.2×10^{19} GeV/ c^2 , and ^{40}Ar -scattering cross sections between 1.0×10^{-23} and 2.4×10^{-18} cm². These results are interpreted as constraints on composite dark matter models with two different nucleon-to-nuclear cross section scalings.

I. INTRODUCTION

Despite the abundance of dark matter (DM) [1], little is known about its particle nature. While Weakly Interacting Massive Particles (WIMPs) of electroweak masses and possible thermal origin are promising candidates and are the subject of several recent searches (e.g. Refs. [2–8], also Ref. [9]), other well-motivated candidates span many orders of magnitude in mass and may evade current constraints.

DM with Planck-scale mass ($m_\chi \simeq 10^{19}$ GeV/ c^2) may be produced non-thermally, such as in inflaton decay or gravitational mechanisms related to inflation [10–14], often related to Grand Unified Theories (GUTs). Other models describe super-heavy DM produced by primordial black hole radiation [15] or extended thermal production in a dark sector [16].

Direct detection constraints at these masses are limited by the DM number density rather than the cross section. As a result, even large cross sections permitting multiple scatters remain unconstrained. While the finite overburden may allow sufficiently massive particles to be detected underground [17], typical WIMP analyses that reject pileup and multiple-scatter signatures cannot be extrapolated to these high cross sections. Instead, dedicated analyses are required [17–19], which can probe a variety of theoretical scenarios giving super-heavy, stable, and strongly interacting states [18, 20–25].

Previous direct detection searches constrain DM with $m_\chi \lesssim 6 \times 10^{17}$ GeV/ c^2 [26–30]. The present study uses data taken with DEAP-3600, 2 km underground at SNOLAB, to probe m_χ up to the Planck scale using multiple-scatter signals, placing the first direct detection constraints at these masses.

II. DETECTOR, EVENT RECONSTRUCTION & DATA SET

DEAP-3600 contains (3279 ± 96) kg LAr in a spherical acrylic vessel (AV) with inner surface area 9.1 m^2 , viewed by 255 photomultiplier tubes (PMTs), submerged in a water Cherenkov muon veto (MV). Additional details are described in Refs. [31, 32]. The data acquisition and WIMP search analysis are described in Refs. [2, 33].

Energy depositions are measured by counting photoelectrons (PEs) in the PMTs resulting from LAr scintillation. PEs are measured by charge-division, as in Ref. [33], rather than the Bayesian algorithm in Ref. [2], as the energies and event topologies of interest extend beyond the latter’s validation range.

The pulse shape of a waveform $w(t)$ summed over

all PMTs is quantified with F_{prompt} , as in Ref. [33],

$$F_{\text{prompt}} = \frac{\int_{-28 \text{ ns}}^{150 \text{ ns}} w(t) dt}{\int_{-28 \text{ ns}}^{10000 \text{ ns}} w(t) dt}. \quad (1)$$

F_{prompt} discriminates single-scatter electronic and nuclear recoils [34] and decreases with the number of scatters, separating single- and multiple-scatters with increasing efficiency at high cross sections.

A second discriminator N_{peaks} is calculated with a peak-finding algorithm based on the waveforms’ slope and identifies coincident scintillation pulses in a $10 \mu\text{s}$ window. This algorithm best identifies multiple-scatter events when the scatters are spread out in time and produce well-separated peaks.

To reduce the volume of data written to disk due to the (3.3 ± 0.3) kBq of ^{39}Ar [2, 35], a “pre-scale” region is defined at low F_{prompt} for 50–565 keV $_{ee}$ energies. Only trigger-level information is recorded for 99% of such events, limiting sensitivity to the lowest cross sections of interest in the present analysis.

This search uses a blind analysis of (813 ± 8) live-days of data collected between November 4, 2016 and March 8, 2020, excluding (3 ± 3) $\mu\text{s}/\text{trigger}$ to account for DM signals that may be divided between two recorded traces, a 9 d open physics run, and a 6 d muon-coincidence sideband, composed of events within $[-10, 90]$ μs of MV triggers. These open datasets informed the background model and cuts, which were frozen prior to unblinding.

III. SIMULATION

DM is simulated via Monte Carlo with the RAT software [36], built upon Geant4 [37], in two steps: 1) it is attenuated in the overburden, 2) it is propagated in the detector, simulating optical and data acquisition (DAQ) responses. DM is generated 80 km above the Earth’s surface with the Standard Halo Model velocity distribution [38–44] and propagated through the Earth to a 1.5 m shell surrounding the AV. DM is boosted into the detector’s reference frame for a randomized date, following Refs. [28, 45].

Assuming continuous energy loss, the attenuation of DM at position \vec{r} is calculated numerically as [18]

$$\left\langle \frac{dE_\chi}{dt} \right\rangle(\vec{r}) = - \sum_i n_i(\vec{r}) \sigma_{i,\chi} \langle E_R \rangle_i v, \quad (2)$$

with v the lab-frame DM speed, n_i the number density of nuclide i , $\sigma_{i,\chi}$ the DM-nucleus scattering cross

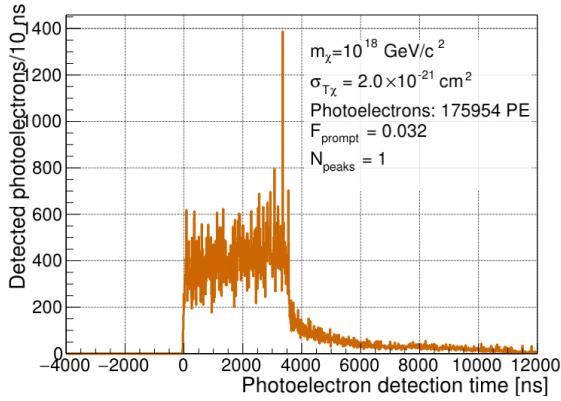
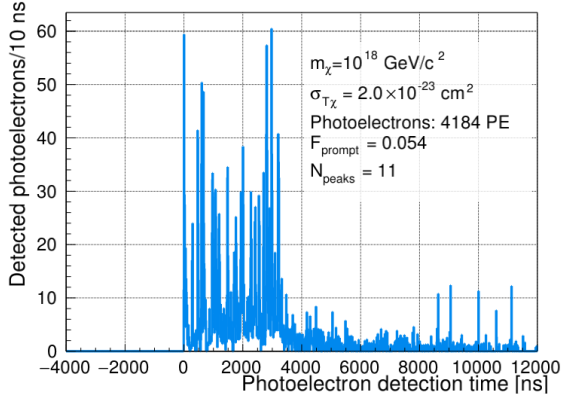


FIG. 1. Example simulated PE time distributions for DM with $m_\chi = 10^{18}$ GeV/ c^2 with low and high $\sigma_{T\chi}$.

section, and $\langle E_R \rangle_i$ the average recoil energy,

$$\langle E_R \rangle_i = \frac{1}{\sigma_{i,\chi}} \int_0^{E_i^{\max}} E_R \frac{d\sigma_{i,\chi}}{dE_R} dE_R, \quad (3)$$

$$E_i^{\max} = [4m_\chi m_i / (m_\chi + m_i)^2] E_\chi,$$

where m_χ and m_i are the DM and nucleus mass, respectively, and $d\sigma_{i,\chi}/dE_R$ is the model-dependent differential scattering cross section (see Sec. V).

The atmospheric density profile is taken from Ref. [46], composed of 79% N₂ and 21% O₂, and the Earth's density profile and composition are from Refs. [47, 48]. Uncertainties in the Earth and atmosphere models negligibly affect the present study.

DM is then propagated through DEAP-3600. The detector response is calibrated up to 10 MeV_{ee} using (n, γ) lines from an ²⁴¹AmBe source, giving a factor of 0.9 ± 0.1 used to scale the simulated PE response.

Fig. 1 shows two simulated PE time distributions. At lower nuclear scattering cross sections (denoted $\sigma_{T\chi}$), N_{peaks} counts peaks from individual scatters, which merge at higher $\sigma_{T\chi}$, causing it to lose accuracy. In this regime, the signal energy and duration, typically $< 6 \mu\text{s}$, depend on the DM speed and track

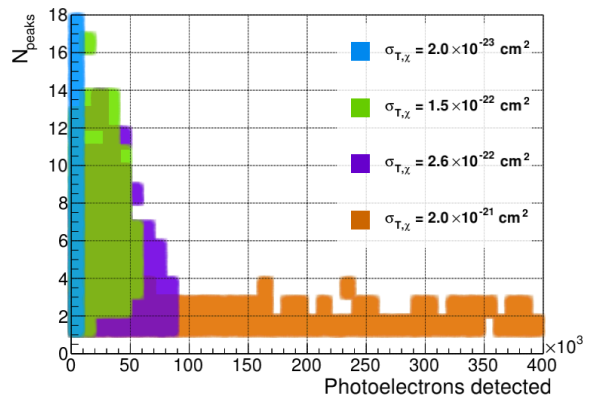
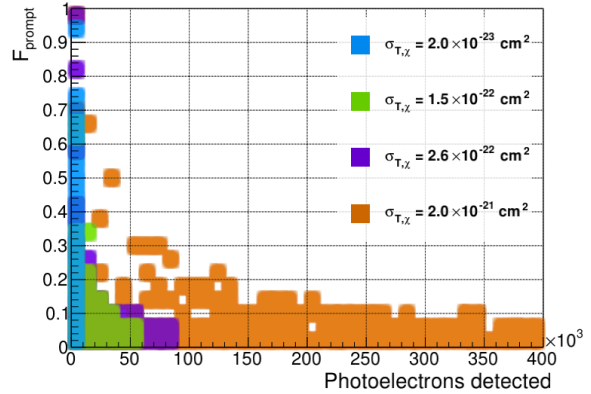


FIG. 2. Simulated F_{prompt} and N_{peaks} distributions for DM with $m_\chi = 10^{18}$ GeV/ c^2 for various $\sigma_{T\chi}$.

length in LAr, making F_{prompt} an estimate of the fraction of scatters in a 150 ns window around the start of the signal, which decreases at higher $\sigma_{T\chi}$.

Near $\sigma_{T\chi} \simeq 10^{-23}$ cm², N_{peaks} grows with increasing $\sigma_{T\chi}$ as the DM scatters more times. As peaks merge, N_{peaks} decreases with $\sigma_{T\chi}$, as seen in Fig. 2. However, F_{prompt} also decreases and narrows as $\sigma_{T\chi}$ grows. For the simulated $\sigma_{T\chi}$, overburden effects have a negligible impact on the DM signal above 10^{12} GeV/ c^2 and become significant at lower m_χ .

IV. ANALYSIS AND RESULTS

To identify DM over a wide range of energies and scattering lengths, four regions of interest (ROIs) are defined with different cuts on N_{peaks} and F_{prompt} , summarized in Tab. I. Cuts for ROIs 1–3 mitigate pileup backgrounds that are negligible in ROI 4, which uses minimal cuts that can be evaluated without the full simulation. Doing this allows for constraints on DM-nucleon scattering cross sections $\sigma_{n\chi}$ that are computationally prohibitive to simulate.

ROI	PE range	Energy [MeV _{ee}]	N _{peaks} ^{min}	F _{prompt} ^{max}	μ _b	N _{obs.}
1	4000–20 000	0.5–2.9	7	0.10	(4 ± 3) × 10 ⁻²	0
2	20 000–30 000	2.9–4.4	5	0.10	(6 ± 1) × 10 ⁻⁴	0
3	30 000–70 000	4.4–10.4	4	0.10	(6 ± 2) × 10 ⁻⁴	0
4	70 000–4 × 10 ⁸	10.4–60 000	0	0.05	(10 ± 3) × 10 ⁻³	0

TABLE I. ROI definitions, background expectations μ_b, and observed event counts N_{obs.} in the 813 d exposure. A cut rejecting events in a [−10, 90] μs window surrounding each MV trigger is applied to all ROIs; low-level cuts requiring that signals be consistent with bulk LAr scintillation are applied to ROIs 1–3. The upper energy bound on ROI 4 is estimated assuming a constant light yield above 10 MeV_{ee}, the highest energy at which the detector is calibrated.

A. Backgrounds and selection cuts

The primary backgrounds come from uncorrelated pileup of signals produced by radioactivity in detector materials, described in Ref. [35]. Correlated backgrounds, such as ²¹²Po α-decays following ²¹²Bi β-decays with a 300 ns half-life, are removed by requiring N_{peaks} > 2 for all energies they may populate.

Pileup was modeled by simulation, validated with a 3.8 h calibration run with an ²⁴¹AmBe source, which emits neutrons at a (4.6 ± 0.7) kHz rate, and with a 9 d non-blind physics run, testing pileup reconstruction for N_{peaks} ≤ 4 up to 7.4 MeV and N_{peaks} ≤ 5 up to 2.6 MeV. Simulated N_{peaks} distributions agreed to within 5% in both datasets. ROI 4 relies solely on F_{prompt} for multi-scatter detection, since N_{peaks} could not be tested at these energies.

Two low-level cuts in ROIs 1–3 ensure signals are from bulk LAr scintillation: <5% of PE must be in PMTs in gaseous Ar, with a DM acceptance of (99.1 ± 0.1)%, and <5% of PE must be in the brightest channel, with a (86.5 ± 0.3)% acceptance.

The dominant backgrounds in ROIs 1–3 are from pileup. Pileup rates decrease with energy, allowing the N_{peaks} threshold to accommodate the decreasing accuracy at higher cross sections. Pileup is negligible in ROI 4, where muons produce the dominant backgrounds. Muons are tagged by the veto. Untagged muons are rejected by the F_{prompt} cut, tuned on the muon-coincidence dataset. The background expectation is determined using the flux in Ref. [49].

Tab. I summarizes cuts and backgrounds in each ROI, defined by the PE range. Energies are provided for illustrative purposes; the listed upper bound on ROI 4 assumes the light yield remains constant above 10 MeV_{ee}, the maximum energy at which the detector is calibrated. Its upper PE bound is consistent with the highest scale at which the DAQ system’s performance was tested using calibration data collected with a light injection system. Fig. 3 shows the probability of 10¹⁸ GeV/c² DM reconstructing in the PE range for each ROI and passing all cuts.

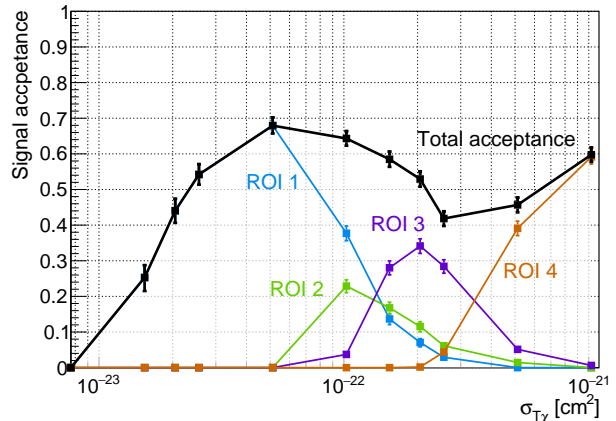


FIG. 3. Probability of DM with m_χ=10¹⁸ GeV/c² populating each ROI and surviving all cuts at varying σ_{Tχ}.

B. Results

After finalizing the selection cuts and background model with a total background expectation of 0.05 ± 0.03 across all ROIs, the blinded dataset was opened, revealing zero events. These null results allow any DM model predicting more than 2.3 events across all ROIs to be excluded at the 90% C. L.

The number of events expected in live time *T* is

$$\mu_s = T \int d^3\vec{v} \int dA \frac{\rho_\chi}{m_\chi} |v| f(\vec{v}) \epsilon(\vec{v}, \sigma_{T\chi}, m_\chi), \quad (4)$$

with local DM density ρ_χ = 0.3 GeV/(c² cm³) [39], DM velocity at the detector \vec{v} , acceptance ε, and surface area *A*. Eq. 4 is evaluated by Monte Carlo simulation, including effects detailed in Sec. III, systematic uncertainties on energy and N_{peaks} reconstruction, and Monte Carlo statistical uncertainties.

V. THEORETICAL INTERPRETATIONS

The DM signal and σ_{nχ}-σ_{Tχ} scaling depend on the DM model. Two composite models are considered.

241 For each model, μ_s is determined at several m_χ
 242 and $\sigma_{n\chi}$, and exclusion regions are built account-
 243 ing for uncertainties as prescribed in Ref. [50]. Up-
 244 per bounds on m_χ are interpolated with a ρ_χ/m_χ
 245 flux scaling; lower bounds are set to the value at
 246 which the overburden calculation predicts that 90 %
 247 of expected DM signals will be below 1 MeV_{ee} after
 248 quenching. Upper bounds on $\sigma_{n\chi}$ are set by the low-
 249 est simulated values that that can be excluded, while
 250 lower bounds are limited by the highest $\sigma_{n\chi}$ that
 251 were computationally possible to simulate, $\sigma_{n\chi}^{\max}$. At
 252 higher $\sigma_{n\chi}$, the continuous scattering approximation
 253 and the time-of-flight in LAr imply a lower bound on
 254 the ROI 4 acceptance of 35 %. Conservatively treat-
 255 ing the probability of reconstructing in ROI 4 as
 256 constant above $\sigma_{n\chi}^{\max}$ and scaling the flux as ρ_χ/m_χ ,
 257 exclusion regions are extrapolated to m_χ consistent
 258 with null results. Upper bounds on $\sigma_{n\chi}$ are set to
 259 $\sigma_{n\chi}^{\max} \times (\text{PE}_{\max}^{\text{ROI4}}/\text{PE}_{90}^{\text{sim}})$, where $\text{PE}_{\max}^{\text{ROI4}}$ is the upper
 260 PE bound of ROI 4 and $\text{PE}_{90}^{\text{sim}}$ is the 90 %
 261 quantile on the PE distribution at $\sigma_{n\chi}^{\max}$. These con-
 262 straints are labeled “extrapolated” in Fig. 4.

263 A. Model I

264 In this model, DM is opaque to the nucleus, so
 265 that the scattering cross section at zero momentum
 266 transfer q is the geometric size of the DM regardless
 267 of the target nucleus. More generally,

$$\frac{d\sigma_{T\chi}}{dE_R} = \frac{d\sigma_{n\chi}}{dE_R} |F_T(q)|^2, \quad (5)$$

268 where $F_T(q)$ is the Helm form factor [55, 56]. This
 269 scaling may give conservative limits for strongly in-
 270 teracting composite DM [57]. The region excluded
 271 for this model is shown in Fig. 4 (top). Here (and in
 272 the bottom panel) the lower and upper boundaries
 273 are flat because, unlike in WIMP searches where
 274 these exclusion $\sigma_{T\chi} \propto m_D$ at high DM masses, the
 275 cross section sensitivity is only dependent on the
 276 detector’s multi-scatter acceptance. The right-hand
 277 boundary is nearly vertical due to the drop in DM
 278 flux with increasing m_D ; above the notch is the re-
 279 gion where the Earth overburden is dominated by
 280 the crust. On the left-hand boundary $\sigma_{T\chi} \propto m_D$
 281 due to attenuation in the overburden.

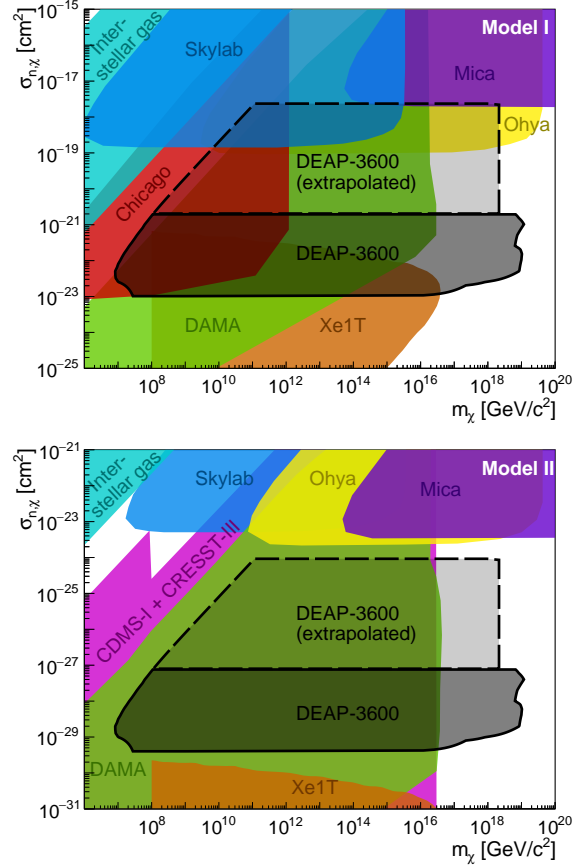


FIG. 4. DM masses m_χ and nucleon scattering cross sections $\sigma_{n\chi}$ excluded by DEAP-3600, for Model I (top) and Model II (bottom). Extrapolated regions exclude dark matter above the highest simulated cross sections. Also shown are other constraints using DAMA [26, 51], interstellar gas clouds [52, 53], a recast of CRESST and CDMS-I [28], a detector in U. Chicago [29], a XENON1T single-scatter analysis [30], and tracks in the Skylab and Ohyha plastic etch detectors [51], and in ancient mica [54]. Limits from MAJORANA DEMONSTRATOR [30] are not shown as the corresponding regions are already excluded by DAMA and XENON1T.

B. Model II

In this scenario the cross section scales as

$$\begin{aligned}
 \frac{d\sigma_{T\chi}}{dE_R} &= \frac{d\sigma_{n\chi}}{dE_R} \left(\frac{\mu_{T\chi}}{\mu_{n\chi}} \right)^2 A^2 |F_T(q)|^2 \\
 &\simeq \frac{d\sigma_{n\chi}}{dE_R} A^4 |F_T(q)|^2,
 \end{aligned} \quad (6)$$

where $\mu_{\{n,T\}\chi}$ is the {nucleon, target}-DM reduced mass and A is the target mass number. The excluded region is shown in Fig. 4 (bottom).

Eq. 6 is the most commonly used scaling, allowing for comparisons with other experiments and with single-scatter constraints. It may arise from nuclear

DM models, outlined in Refs. [58, 59], which describe a dark nucleus with N_D nucleons of mass m_D and radius r_D , yielding a total mass $m_\chi = N_D m_D$ and radius $R_D = N_D^{1/3} r_D$. For $m_\chi \gg m_T$,

$$\frac{d\sigma_{T\chi}}{dE_R} = \frac{d\sigma_{nD}}{dE_R} N_D^2 |F_\chi(q)|^2 A^4 |F_T(q)|^2, \quad (7)$$

where σ_{nD} is the nucleon-dark nucleon scattering cross section. To preserve the Born approximation, Eq. 7 is bounded by the geometric cross section:

$$\sigma_{T\chi} \leq \sigma_{\text{geo}} (= 4\pi R_D^2 = 4\pi N_D^{2/3} r_D^2). \quad (8)$$

For dark nuclei of size $R_D \gg 1$ fm, we may identify $\sigma_{n\chi} = N_D^2 \sigma_{nD}$ for potentials that give rise to $|F_\chi(q)|^2 \simeq 1$, and Fig. 4 could then constrain such nuclear DM in regions satisfying Eq. 8. We leave detailed studies of such possibilities to future work.

VI. SUMMARY AND SCOPE

This study uses DEAP-3600 data to derive new constraints on composite DM, including the first direct detection results probing Planck-scale masses. These constraints were obtained through a dedicated analysis of multiple-scatter signals, accounting for the attenuation that the DM would experience in the laboratory's overburden. The analysis used to achieve these results represents the first study of this kind in a tonne-scale direct detection experiment, extending Planck-scale limits from ancient mica [54] and etched plastic studies [51] to lower cross sections.

The high-mass sensitivity achieved by DEAP-3600 was possible due to its large cross sectional area, which provides a large net to catch dilute DM. As a result, limits were placed on two classes of DM models describing strongly interacting, opaque composites and dark nuclei motivated by the QCD scale with a spherical top-hat potential.

This analysis may be extended to superheavy DM depositing energy via modes other than elastic scattering, (*e.g.* Ref. [25]), to future LAr, liquid xenon and bubble chamber detectors, and to large-scale liquid scintillator (*e.g.* SNO+, JUNO) [18] and segmented detectors (*e.g.* MATHUSLA) [19].

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