

# 1 **Intrinsic Climate Cooling**

## 2 Abstract

3 Lower heating of our planet by the young Sun was compensated by higher warming from factors  
4 such as greater greenhouse gas concentrations or reduced albedo. Earth's climate history has  
5 therefore been one of increasing solar forcing through time roughly cancelled by decreasing forcing  
6 due to geological and biological processes. The current generation of coupled carbon-cycle/climate  
7 models suggest that decreasing geological forcing—due to falling rates of outgassing, continent-  
8 growth and plate-spreading—can account for much of Earth's climate history. If Earth-like planets  
9 orbiting in the habitable zone of red-dwarfs experience a similar history of decreasing geological  
10 forcing, their climates will cool at a faster rate than is compensated for by the relatively slow  
11 evolution of their smaller stars. As a result, they will become globally glaciated within a few billion  
12 years. The results of this paper therefore suggest that coupled carbon-cycle/climate models  
13 account, parsimoniously, for both the faint young Sun paradox and the puzzle of why Earth orbits a  
14 relatively rare and short-lived star-type.

15

## 16 1. Introduction

17 This paper proposes that gradual climate-cooling, driven by geology and/or biology, is an inherent  
18 process on Earth-like planets and that this proceeds at a rate with the same order of magnitude on  
19 all such worlds. For definiteness an Earth-like planet is defined, in this paper, as a rocky-world that is  
20 partially covered by a surface ocean.

21 The idea that biological and geological processes have changed Earth's atmosphere and reflectivity—  
22 hence keeping the climate cool despite slowly increasing solar insolation—is not novel (e.g.,

23 Lovelock & Margulis (1974); Walker, Hays, & Kasting (1981); Berner et. al. (1983); Berner & Berner,  
24 (1997); Schwartzman (2002); Lenton & Watson (2011)) but the consequences of assuming that a  
25 similar rate of geo-biological cooling is common to all Earth-like worlds, have not been previously  
26 explored. The justification for this proposal is that it links two independent mysteries concerning  
27 astrobiology and the habitability of Earth. These are:

- 28 • The faint, young Sun paradox (see review by Feulner, 2012). There has been a substantial  
29 increase in solar luminosity over the last 4.5 Gy but there is no evidence for an early Earth  
30 that was significantly cooler than today.
- 31 • The red-dwarf puzzle (see recent analysis by Waltham, 2017). Red dwarfs are more  
32 common and longer lived than sun-sized stars and so it is surprising that we find ourselves  
33 orbiting a significantly rarer and shorter-lived type of star.

34 This paper links these because the rate of geo-biological cooling required to resolve the faint young  
35 Sun paradox would, if repeated on other worlds, cause planets orbiting red-dwarfs to cool faster  
36 than they are warmed by their slowly evolving stars. As a result, initially habitable planets would  
37 become too cold for life within a timescale much shorter than that of their traditional habitable  
38 lifetime (i.e., one based upon the time until planetary over-heating).

39 This paper begins by quantifying the climate forcing required to avoid a frozen, young Earth. This  
40 analysis does not in itself reveal anything new but, in the following section, a similar analysis is  
41 applied to habitable-zone (HZ) planets orbiting smaller stars to show that—if there really is a roughly  
42 constant rate of cooling— it leads to glaciation. These results do not, in themselves, demonstrate  
43 that a constant cooling hypothesis is correct; they merely demonstrate that the hypothesis has  
44 dramatic consequences if it happens to be true. A discussion therefore follows on whether the  
45 constant cooling assumption is reasonable and on the further research needed to strengthen or  
46 refute the hypothesis.

47        2. The faint young Sun paradox

48        Our Sun's luminosity,  $L_{\odot}$ , was only 68% of the current luminosity,  $L_0$ , when it entered the main  
49        sequence  $\sim 4.57$  Gy ago (see Fig. 1 and note that, for consistency with published stellar evolution  
50        models, all times in this paper run forwards from the moment a star reaches the main sequence—  
51        ZAMS; zero age main sequence—rather than backwards from the present day). The gradually  
52        increasing solar-luminosity should have made modern Earth much warmer than early Earth and,  
53        hence, the global mean temperature should have been well below freezing in the distant past (Donn  
54        et. al., 1965; Sagan & Mullen, 1972; Walker, 1982; Jenkins, 1993; Kienert et. al., 2012; Feulner, 2012;  
55        Charnay et al., 2013). This is contradicted by geological data (e.g., evidence of liquid water) which  
56        suggests that temperatures were similar to or, perhaps, significantly higher in the distant past  
57        (Walker, 1982; Schwartzman, 2002; Valley et. al., 2002; Knauth & Lowe, 2003; Sleep & Hessler, 2006;  
58        Hren et. al., 2009; Blake et. al., 2010). A range of explanations have been proposed for resolving this  
59        dilemma.

60        Firstly, on sufficiently long time scales there may be negative feedback mechanisms which act to  
61        stabilize temperatures. In particular, silicate weathering feedback (Walker et al., 1981) is widely  
62        accepted as important for Earth habitability and is expected to buffer the climate of other Earth-like  
63        worlds too. The question of whether it is sufficiently strong to undermine the hypothesis of this  
64        paper will be central to much of what follows. Silicate weathering involves dissolution of silicate  
65        rocks, by  $\text{CO}_2$  dissolved in rainwater, to produce bicarbonate ions that are eventually incorporated  
66        into calcium carbonate on the seafloor. The overall effect is to lock-up carbon from the atmosphere  
67        into Earth's crust from where it is slowly liberated by rainfall-dissolution of uplifted carbonate or  
68        through volcanic emission of  $\text{CO}_2$  following carbonate subduction into the mantle. The dissolution of  
69        silicate rocks by acid rain (i.e., the first step in this cycle) is climate dependent (it is faster when the  
70        world is warmer and wetter) and so carbon dioxide is preferentially removed from the atmosphere  
71        when climate is warm. In the distant past, when solar warming was smaller, the cooler climate

72 would have reduced the rate of removal of CO<sub>2</sub> from the air and the resulting enhanced greenhouse  
73 warming helped prevent global freezing.

74 An additional possibility is that Earth's climate system has been significantly altered by biological  
75 factors. The evolution of lichens, and then vascular land-plants, may have accelerated continental  
76 weathering, hence enhancing carbon-dioxide drawdown by silicate weathering (Berner & Berner,  
77 1997; Moulton et. al., 2000; Schwartzman, 2002; Taylor et. al., 2011; Lenton et. al., 2012; Boyce &  
78 Lee, 2017). This would have led to a decline in CO<sub>2</sub> levels as the biosphere developed. The existence  
79 of methanogens may also have played a major role in enhancing methane levels in the early  
80 atmosphere and, hence, the strength of the greenhouse effect (Kasting, 2005; Ozaki et. al., 2018).  
81 Furthermore, the later evolution of oxygenic photosynthesis and the subsequent appearance of free  
82 oxygen in the atmosphere (Lyons et. al., 2014) probably led to chemical scrubbing of this methane  
83 from the atmosphere and a fall in greenhouse warming (Pavlov et. al., 2000). Indeed, rapid rise of  
84 oxygen in the atmosphere has been implicated in the major glaciations of the early Proterozoic and  
85 may also have played a role in Neoproterozoic glaciations (Och & Shields-Zhou, 2012). Another  
86 relevant biological process is burial of carbon, in the form of fossil-fuel deposits, leading to its  
87 extraction from the atmosphere and climate cooling (Berner, 2003; Feulner, 2017).

88 Given these plausible mechanisms, it is widely accepted that biosphere evolution played a significant  
89 role in climate evolution. Some researchers have gone further and proposed that biospheres  
90 necessarily stabilize their climates (i.e., the Gaia hypothesis (Lovelock & Margulis, 1974)) but, while  
91 progress has been made in finding a theoretical basis for the Gaia hypothesis (e.g. see Lenton et al.  
92 (2018)), it remains highly contentious (e.g., see Tyrrell (2013)).

93 Finally, geological evolution, too, has contributed to the climate history of our planet. In particular,  
94 arc-volcanism has slowly added continental lithosphere so that the amount of land-surface available  
95 for silicate weathering has increased through time. However, the few studies undertaken on the  
96 effect of land-area on climate indicated either that habitability is monotonically reduced as land-area

97 increases (Franck et. al., 2003) or—in direct contradiction—that it monotonically rises as land-area  
98 increases (Abe et. al., 2011). Abbot et. al. (2012), on the other hand, concluded that the effect is  
99 minimal unless there is no land at all. Thus there is no consensus on the effect that increasing land-  
100 area had (but note that it must also have altered planetary albedo).

101 An additional, relevant geological process is that secular cooling of Earth’s interior has resulted in  
102 less volcanic outgassing and, hence, less input of CO<sub>2</sub> into the atmosphere (Kadoya & Tajika, 2015).  
103 Carbon dioxide is also removed from ocean water by carbonatization of basalt in hydrothermal  
104 systems close to spreading ridges (Sleep & Zahnle, 2001) and this will have occurred at a rate that  
105 may have dropped if ocean-spreading slowed over time.

106 When incorporated into a combined carbon-cycle and climate simulation, these time-dependent  
107 geological processes predict climate evolution that, in some models at least, agrees with the  
108 available data on Earth’s temperature (Kadoya & Tajika, 2015) as well as with data on CO<sub>2</sub>  
109 concentration, seafloor-weathering and ocean pH (Krissansen-Totton et. al., 2018).

110 Hence, many mechanisms may have combined to yield the relatively stable temperature history of  
111 Earth although the details remain contentious and there is no consensus on whether the dominant  
112 cause was negative feedback or intrinsic changes due to biology or geology. Nevertheless, the  
113 changes required can be quantified by using the definition of climate sensitivity,  $\lambda$ , that

$$114 \quad \lambda = \Delta T_{earth} / \Delta F \quad (1)$$

115 where  $\Delta T_{earth}$  is the change in mean temperature at Earth’s surface produced by a change,  $\Delta F$ , in  
116 heating at the top of the atmosphere (e.g., see Rohling et al. (2012)). Unless stated otherwise, all  
117 differences in this paper are relative to the present-day Earth (e.g.,  $\Delta T_{earth}$  will be taken from here on  
118 as the difference in temperature from the present day global mean of ~15 C). Note that, in some  
119 references,  $\lambda$  is defined as the inverse of the definition above (i.e.,  $\lambda = \Delta F / \Delta T_{earth}$ ).

120 Changes in forcing can be produced by changes in solar output but also by changes in Earth's albedo  
121 or in the atmospheric concentration of greenhouse gasses. In the latter two cases,  $\Delta F$  is the change  
122 in heating at the top of the atmosphere that would produce the same effect as the change in albedo  
123 or greenhouse gas concentration. An accessible discussion of the forcing concept is given in Stocker  
124 (2013).

125 A reasonable objection, to the use of equation (1), is that it is a linear approximation that will not be  
126 appropriate when there are large changes in forcing. However, the whole point of the faint young  
127 Sun paradox is that there must be some additional forcing that, at least partially, cancels solar  
128 changes. Hence, the total change in forcing is (by hypothesis) small and a linear approximation  
129 should remain reasonably accurate. For example, if temperature changes are of order 10 K and  $\lambda$  is  
130 of order 1 K W<sup>-1</sup> m<sup>2</sup> (see below), the change in total forcing is of order 10 Wm<sup>-2</sup> which is less than 3%  
131 of the solar forcing.

132 Another issue is that  $\lambda$  will have changed as Earth's atmosphere, biosphere, hydrosphere and  
133 lithosphere have evolved. This can be handled by using a suitably averaged climate sensitivity of the  
134 form

$$135 \quad \bar{\lambda} = \int_{F_0}^{F_1} \lambda dF / (F_1 - F_0) \quad (2)$$

136 where the forcing has changed from  $F_0$  to  $F_1$  over the period being modelled and integration is along  
137 a (possibly complicated) path in the  $\lambda$ - $F$  plane. All climate sensitivities discussed subsequently  
138 should be understood as being averages in this sense. Note that, for the simple case of forcing  
139 changes in the form  $F(t) = F_0 + \alpha t$ , equation (2) just gives the time-averaged sensitivity.

140 Climate sensitivity estimates are subject to the measurement uncertainties of all empirical data and,  
141 in addition, vary depending upon (i) their precise definition; (ii) the time-scale of the measurement;  
142 (iii) the methodology used (Rohling et al., 2012). Sensitivity is also likely to have changed through  
143 time (Caballero & Huber, 2013) and may have been significantly different in the distant past. These

144 difficulties lead to a wide diversity of reported values for climate sensitivity but most long-term  
145 estimates fall in the range  $1.1 \pm 0.8 \text{ K W}^{-1} \text{ m}^2$  (Covey et. al., 1996; Borzenkova, 2003; Bijl et al., 2010;  
146 Park & Royer, 2011; van de Wal et al., 2011; Rohling et al., 2012; Royer et. al., 2012). This range of  
147 sensitivities implies that total feedback is positive since a value of  $0.3 \text{ K W}^{-1} \text{ m}^2$  corresponds to the,  
148 so-called, Planck sensitivity (the sensitivity expected if there are no feedbacks other than an increase  
149 in thermal radiation with temperature, see (Bony et al., 2006) and (Soden, & Held, 2006)).

150 However, a key consideration in the current paper is that it is widely accepted that the silicate  
151 weathering cycle has played a major role in maintaining Earth's climate stability over the extremely  
152 long time-scales relevant to discussion of the faint young Sun paradox. It is therefore important to  
153 highlight the climate sensitivity associated with this process in particular. An estimate can be  
154 derived from the work of Abbot et al. (2012) whose figure 3 implies

$$155 \quad \lambda \approx \lambda_0 \cdot (0.5 \pm 0.2) \quad (3)$$

156 where  $\lambda_0$  is the climate sensitivity in the absence of silicate weathering. For Abbot et al's (2012)  
157 typical parameter values,  $\lambda_0 \sim 0.9 \text{ K W}^{-1} \text{ m}^2$  and hence their climate sensitivity, when silicate  
158 weathering is included, can go as low as  $0.27 \text{ K W}^{-1} \text{ m}^2$ .

159 In summary, climate sensitivity estimates are generally of order  $1 \text{ K W}^{-1} \text{ m}^2$  but models of silicate-  
160 weathering can push this below the Planck value of  $0.3 \text{ K W}^{-1} \text{ m}^2$  thus allowing weak negative  
161 feedback. To be maximally conservative, this paper will investigate the effects of sensitivities as low  
162 as  $0.2 \text{ K W}^{-1} \text{ m}^2$ . Specifically, this paper will investigate climate sensitivities varying over one order of  
163 magnitude from  $0.2$  to  $2.0 \text{ K W}^{-1} \text{ m}^2$ .

164 The next step is to split the forcing term of eqn (1) into extrinsic (to Earth) and intrinsic components,  
165 i.e.,

$$166 \quad \Delta F = \Delta F_{\odot} + \Delta F_{earth} \quad (4)$$

167 where  $\Delta F_{\odot}$  is the change in extrinsic forcing due to solar evolution and  $\Delta F_{earth}$  is the change in  
168 intrinsic forcing due to biological and/or geological evolution of Earth. Equations (1) and (4)  
169 combine to yield

$$170 \quad \Delta F_{earth} = \frac{\Delta T_{earth}}{\lambda} - \Delta F_{\odot} \quad (5)$$

171 with changes in solar forcing given by

$$172 \quad \Delta F_{\odot} = 0.25S_0(1 - a_{pd}) \left( \frac{L_{\odot}}{L_0} - 1 \right) \quad (6)$$

173 where  $S_0$  is the present day solar constant of  $1360.8 \pm 0.5 \text{ W m}^{-2}$  (Kopp & Lean, 2011), and  $a_{pd}$  is  
174 modern Bond albedo (0.31).

175 Equation (6) allows the strength of intrinsic warming, required to counter the faint young Sun, to be  
176 estimated but the results do not lead to novel conclusions. However an extension of this analysis, to  
177 include habitable planets orbiting low-mass stars, leads to the conclusion that such worlds will tend  
178 to cool substantially as they age and, as a consequence, are highly likely to enter a “snowball” state.  
179 It is therefore now time to look at the second astrobiological mystery that this paper considers; the  
180 surprisingly large size of our star.

181

### 182 3. The red dwarf puzzle

183 Imagine spending a randomly chosen minute on a randomly chosen habitable planet. Such a  
184 “habitable moment” is far more likely to be associated with a small star than a large one because  
185 small stars are more common and, conventionally, HZ planets orbiting such stars have many more  
186 habitable moments (i.e., they have longer habitable lifetimes (Kasting et. al., 1993)). Our own  
187 existence as individuals can be thought of as occupying a “habitable moment” and so we should  
188 similarly expect to look up at a small, red star rather than a large yellow one.



189 In more detail, the number of stars of a given mass is expressed by the initial mass function (IMF).  
190 The precise form of the IMF, and whether it remains constant with time, is controversial (Kroupa,  
191 2001) but the debates concern details that do not greatly affect the key result that our Sun is a  
192 relatively large star. For example, the Miller & Scalo (1979) IMF implies that 87% of all stars are  
193 smaller than the Sun whilst the Chabrier (2005) IMF gives 86%. Furthermore, small stars consume  
194 their nuclear fuel more slowly than large stars implying that planets orbiting small stars will remain  
195 habitable for significantly longer than larger ones. For example, Kasting et al. (1993) estimated that  
196 Earth will remain habitable about 3-times longer than an HZ planet orbiting a 1.5 solar-mass star.  
197 Recent statistical modelling (Waltham, 2017) indicates that the combination of more stars and more  
198 time leads to very large increases in the probability of observers. This results from a model—due to  
199 Carter & McCrea (1983)—that the probability of observers increases with  $t^n$  where  $t$  is time available  
200 and  $n$  is around 3; hence a red-dwarf with a main-sequence lifetime 100-times greater than the Sun  
201 is one million times more likely to produce observers. The implication, of the observation that  
202 despite this we orbit a relatively large star, is that there must be something wrong with red-dwarfs—  
203 some reason why planets orbiting small stars are poor habitats (or, at least, not significantly longer-  
204 lived habitats than planets orbiting solar-mass stars).

205 There is no shortage of proposals. Red-dwarfs may be unfavourable because of their flare activity  
206 (Scalo et al., 2007), their early high luminosity (Luger & Barnes, 2015) or because tidal drag slows the  
207 spin rates of HZ planets orbiting small stars (Lammer et al., 2009) but several papers have argued  
208 that none of these problems are insurmountable (Heath et. al., 1999; Tarter et al., 2007; Yang et. al.,  
209 2013).

210 It has also been suggested that planets orbiting small stars will receive less photosynthetically active  
211 radiation (PAR) (Pollard, 1979) and it is certainly plausible that the absence of photosynthesis would  
212 make the appearance of observers less likely. Heath et al. (1999) calculated that PAR could be  
213 reduced by an order of magnitude on planets orbiting small stars but, nevertheless, concluded that

214 there would still be sufficient light to support photosynthesis. They justified this by the observations  
 215 that land-plants on Earth are frequently saturated (i.e., get more light than they can use) and that  
 216 the photic zone in our oceans extends down to depths where solar radiation is only about 1% that at  
 217 the surface. Similar conclusions have been drawn by other authors (e.g., McKay, 2014; Gale &  
 218 Wandel, 2017). However, recent work has suggested that a reduced incidence of PAR is likely to  
 219 result in oxygen-sinks outweighing oxygen-production and, hence, such planets will not have  
 220 oxygen-rich atmospheres (Lehmer et al., 2018).

221 It therefore remains unclear what the problem is, if any, with small stars and so there is a need to  
 222 investigate other possible habitability issues. The hypothesis of this paper—that all Earth-like  
 223 planets exhibit a similar intrinsic climate-cooling history—provides a new explanation; the warming  
 224 of slowly evolving, smaller stars is too slow to counter planetary cooling and so initially habitable  
 225 planets become too cold for life on a timescale that is much shorter than their traditional habitable  
 226 lifetime.

227 The consequences of assuming this idea can be quantitatively investigated by using eqn (6) which,  
 228 together with the assumption that all Earth-like planets have similar intrinsic cooling histories (i.e.,  
 229 that intrinsic planetary cooling  $\Delta F_p(t) = \Delta F_{earth}(t)$ ), leads to

$$230 \quad \frac{\Delta T_p}{\lambda} - \Delta F_* = \frac{\Delta T_{earth}}{\lambda} - \Delta F_{\odot} \quad (7)$$

231 where  $\Delta T_p$  is the temperature history of an Earth-like world with insolation history  $\Delta F_*$ . A simple  
 232 rearrangement now produces

$$233 \quad \Delta T = \Delta T_p - \Delta T_{earth} = \lambda(\Delta F_* - \Delta F_{\odot}) \quad (8)$$

234 where  $\Delta T$  is the temperature difference between the planet and Earth *at the same age*. This  
 235 expression models the difference in climate history between Earth and another Earth-like planet in  
 236 terms of their different insolation histories (modelled by  $\Delta F_* - \Delta F_{\odot}$ ), assuming that they experience

237 identical intrinsic changes in greenhouse gas concentrations and albedo (modelled by setting  
 238  $\Delta F_p(t)=\Delta F_{earth}(t)$ ) but with additional changes in greenhouse gasses and albedo due to feedback  
 239 responses (modelled by  $\lambda$ ).

240 Equation (8) implicitly assumes that Earth-like planets are sufficiently similar to Earth that they have  
 241 approximately the same average climate sensitivity (i.e., after averaging via eqn (2)). The error,  $\varepsilon$ ,  
 242 introduced by this assumption is

$$243 \quad \varepsilon = -\left(1 - \frac{\lambda_p}{\lambda_{earth}}\right) \Delta T_{earth} \quad (9)$$

244 the magnitude of which will be less than  $\Delta T_{earth}$  (which is of order 10 K) unless  $\lambda_p > 2\lambda_{earth}$ . The effect  
 245 of a 10K error, on the analysis, will be discussed with the results later.

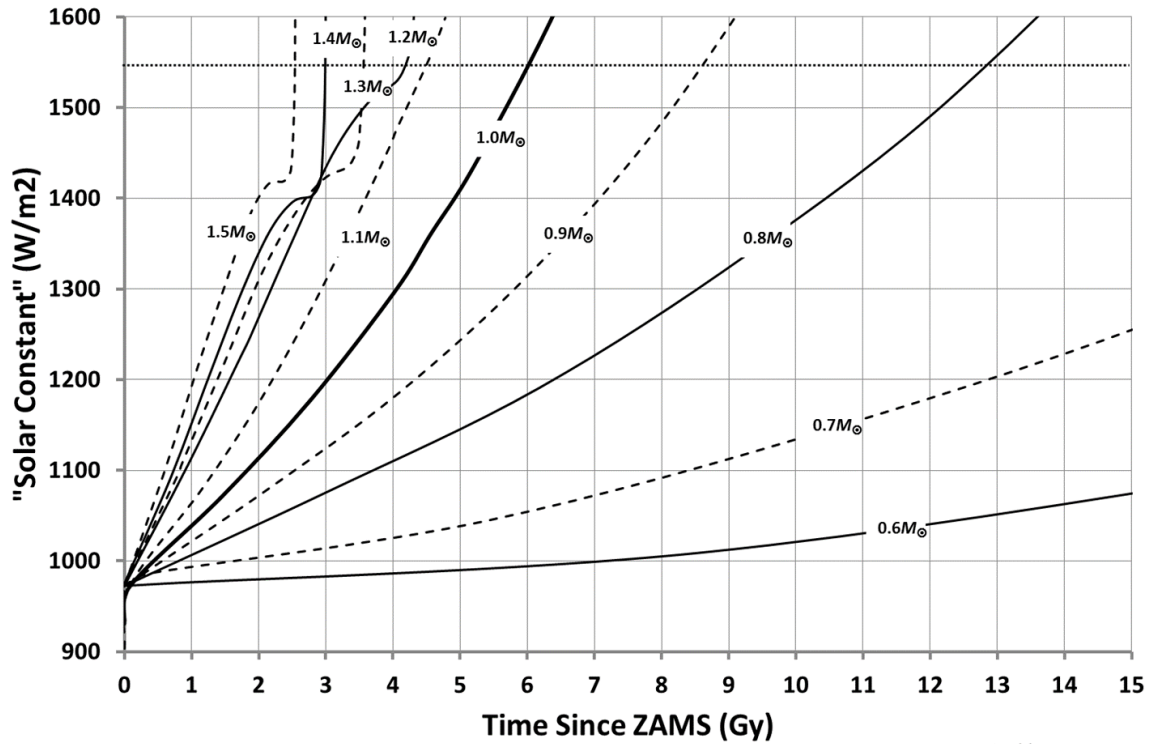
246 Now, let the planet orbit at the distance from its star such that it starts with the same insolation as  
 247 the early Earth. This is ensured if

$$248 \quad \Delta F_* = 0.25S_0(1 - a_{pd}) \left(\beta \frac{L_*}{L_0} - 1\right) \quad (10)$$

249 where  $\beta=L_0/L_*$  at zero time. Note that the  $(1-a_{pd})$  term appears because eqn (10) expresses the  
 250 difference in stellar forcing between the planet (at any time) and Earth (at the present day). Its  
 251 appearance in the equation is therefore just a normalization factor and does not imply that  $a_{pd}$   
 252 applies to other planets or to other times.

253 The resulting evolution of the “Solar Constant,” for HZ planets orbiting stars of different mass, is  
 254 shown in Fig. 1 using data taken from Girardi et. al. (2000). Unfortunately, the stellar mass-range  
 255 provided by Girardi et. al. (2000) only extends down to 0.6 solar-masses but this is sufficient to  
 256 demonstrate the effects discussed here.

257 Figure 1 clearly shows that the insolation evolution for an HZ planet is strongly affected by stellar  
 258 mass. In particular the rate of insolation increase with time, goes up with mass (see Fig. 2).



Waltham, Fig. 1

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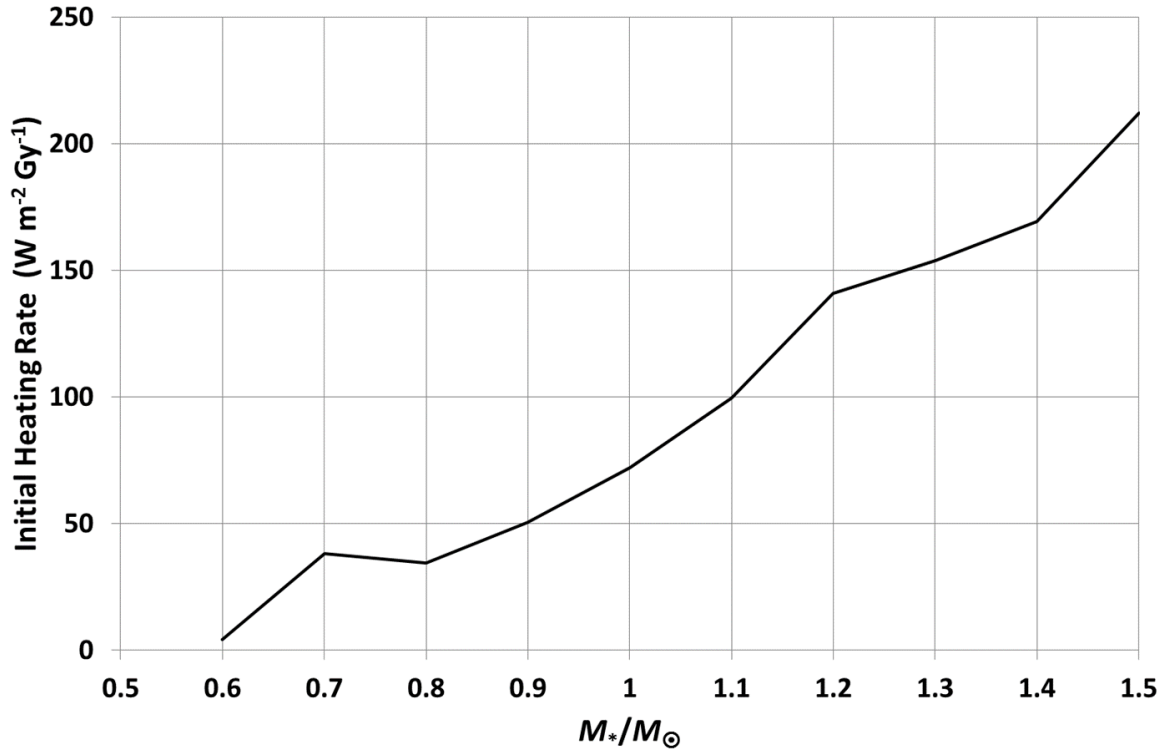
Figure 1. Insolation histories for HZ planets orbiting stars with a range of masses. Trajectories are based upon the stellar evolution models of Girardi et al (2000) together with the assumption that the planets all have the same insolation at the start of their main-sequence evolution with a value chosen to give the present day solar constant at 4.5 Gy for a solar-mass star. Note that the gradients of these trajectories increase with stellar mass (see Fig. 2). The horizontal dotted line shows the insolation reached for the solar-mass case after 6 Gy and this is taken as determining habitable lifetimes assuming habitability is truncated by stellar warming. The resultant habitable lifetimes are shown in Fig. 3 as the “Overheating” curve.

267

268

Furthermore, the time at which insolation becomes so strong that a planet becomes uninhabitably warm (approximated here by taking Earth’s insolation at 6 Gy) decreases sharply with increasing mass (see Fig. 3)). From this paper’s point of view, the key result is that small stars are usually considered to have much longer habitable lifetimes than stars of solar-mass because they take longer to cause over-heating. However, as shown below, it is also possible for planets to become uninhabitable due to over-cooling and this dramatically reduces the habitable lifetimes of planets orbiting smaller stars.

274



275

276 Figure 2. The dependence of initial stellar-heating increase-rate on stellar mass (i.e., a plot of the initial gradients from Fig.

277 1). Small mass stars warm much more slowly than high mass stars.

278

279 To calculate the rate of such cooling, equations (6), (8) & (10) can be combined to give

$$280 \quad \Delta T = 0.25 S_0 \lambda (1 - a_{pd}) \left( \beta \frac{L_*}{L_0} - \frac{L_\oplus}{L_0} \right). \quad (11)$$

281 Figure 4 shows this evaluated for planets orbiting a star of mass  $0.6M_\odot$  and for climate sensitivities

282 in the range  $0.2 < \lambda < 2.0 \text{ K W}^{-1} \text{ m}^2$ . For all cases the planet cools compared to Earth, as the planet

283 ages, with the size of this effect depending upon the assumed climate sensitivity.

284 To assess the effect of this cooling on habitability we require an estimate of the temperature

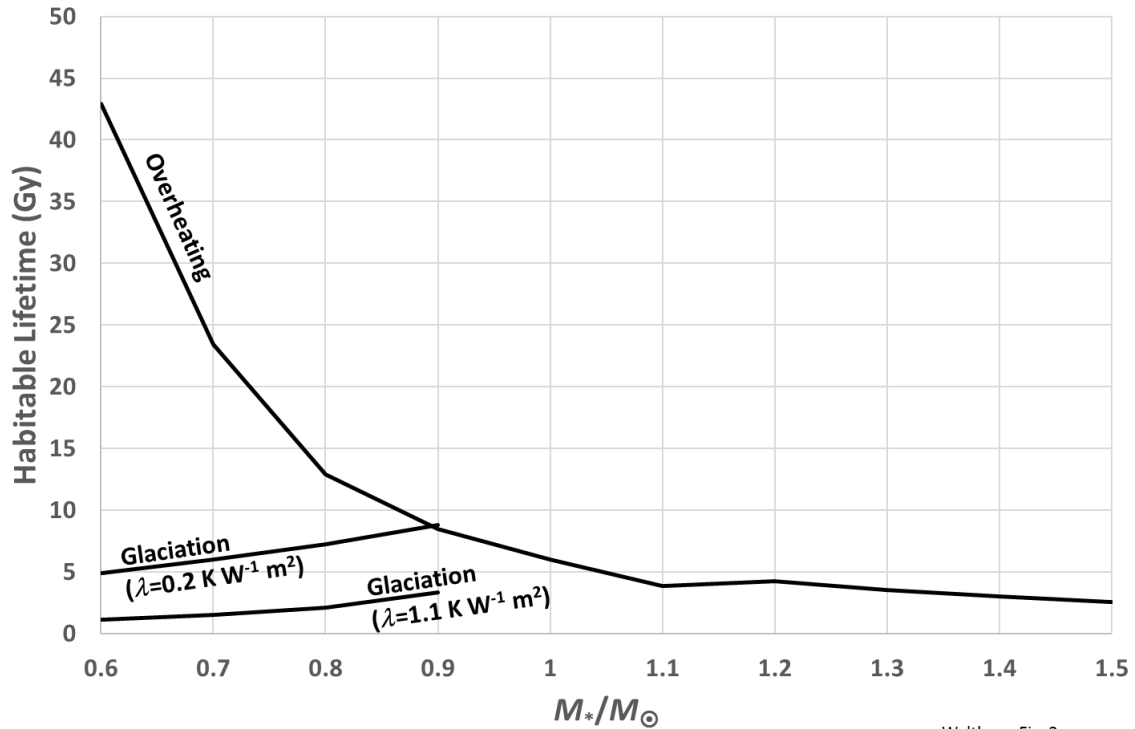
285 difference required to produce global glaciation. North et. al. (1981) predict Snowball-Earth states

286 when mean temperatures fall below  $-5 \text{ C}$  and other authors obtain similar results ( $-3$  to  $-5 \text{ C}$  in

287 Kienert et al. (2012);  $-5$  to  $-7 \text{ C}$  in Feulner & Kienert (2014);  $-9 \text{ C}$  in Feulner (2017)). In contrast,

288 Charney et. al.'s (2013) GCM model can maintain an equatorial water-belt down to a global mean

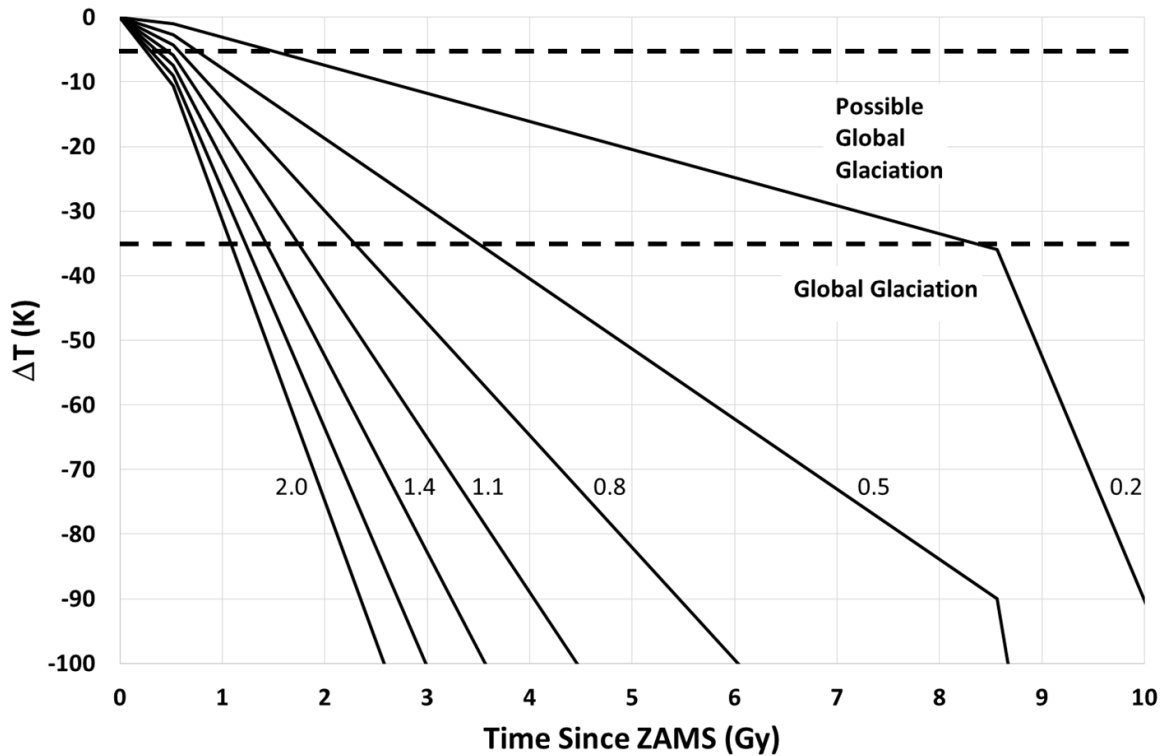
289 temperature of -25 C but this is probably an artefact resulting from the absence of sea-ice dynamics  
 290 (Voigt & Abbot, 2012). The current paper therefore assumes that glaciation will occur if global  
 291 mean temperature falls below  $-5\pm 5$  C.



Waltham, Fig. 3

292  
 293 Figure 3. Habitable lifetimes as a function of stellar mass. The overheating curve is derived as discussed in the caption to  
 294 Fig. 1. The glaciation curves are derived from plots such as Fig. 4 by finding the times where the trajectories cross a  
 295 temperature difference of -20 K. Note that, for stars smaller than the Sun, habitability is truncated by glaciation rather  
 296 than overheating and that, as a consequence, the habitable lifetimes of small stars are much less than usually assumed.

297 Further assuming that, for most of its history, Earth has maintained a temperature of roughly  $15\pm 10$   
 298 C then implies that glaciations will be triggered when the temperature difference between Earth and  
 299 the modelled planet drops below  $-20\pm 15$  K. This range is indicated on Fig. 4 (as “Possible Global  
 300 Glaciation”) and it shows that, for all sensitivities modelled, global glaciation is possible before the  
 301 planet reaches Earth’s present age (4.567 Gy) even if the error (given by eqn (10)) is as much as 10 K.  
 302 Even in the most optimistic case ( $\lambda = 0.2 \text{ K W}^{-1} \text{ m}^2$  and no glaciation until  $\Delta T = -35$  C) habitability  
 303 ceases after 8.5 Gy, i.e., significantly less than the 43 Gy lifetime before over-heating shown on Fig.  
 304 3.



305

306 Figure 4. Predicted temperature history of an HZ planet orbiting a 0.6 solar-mass star. The different curves correspond to  
 307 different assumed climate sensitivities with values in  $\text{K W}^{-1} \text{ m}^2$ . The vertical axis corresponds to the temperature  
 308 difference of the modelled planet from the Earth at the same age. The horizontal dashed lines indicate the  
 309 temperature differences where global glaciation is likely to commence (i.e., it is possible by  $\Delta T = -5\text{K}$  and highly likely  
 310 by  $\Delta T = -35\text{K}$ ).

311 Two specific cases will now be used for the purpose of comparing glaciation timescales for stars of  
 312 different masses. Taking the Earth-to-planet temperature-difference required for glaciation as  $-20\text{C}$ ,  
 313 glaciation occurs, with the  $0.6M_{\odot}$  star, just before 5Gy for  $\lambda = 0.2\text{ K W}^{-1} \text{ m}^2$  and well before 1.5 Gy if  
 314  $\lambda = 1.1\text{ K W}^{-1} \text{ m}^2$ . Repeating this analysis for the range  $0.6M_{\odot} \leq M \leq 0.9 M_{\odot}$  produces the  
 315 “Glaciation” lines in Fig. 3. The key result is that habitable lifetimes for stars smaller than the Sun  
 316 are substantially reduced, as a result of glaciation, compared to their traditional habitable lifetimes  
 317 based upon over-heating. Note that this remains true even when a very low climate sensitivity is  
 318 assumed in order to simulate the effects of negative feedback from silicate weathering (i.e., for  
 319  $\lambda = 0.2\text{ K W}^{-1} \text{ m}^2$ ). Thus, HZ planets orbiting stars smaller than the Sun do not have substantially

320 longer habitable lifetimes than Earth and so, if the hypothesis of approximately constant intrinsic  
321 cooling is correct, it resolves the puzzle of why we do not orbit a red-dwarf.

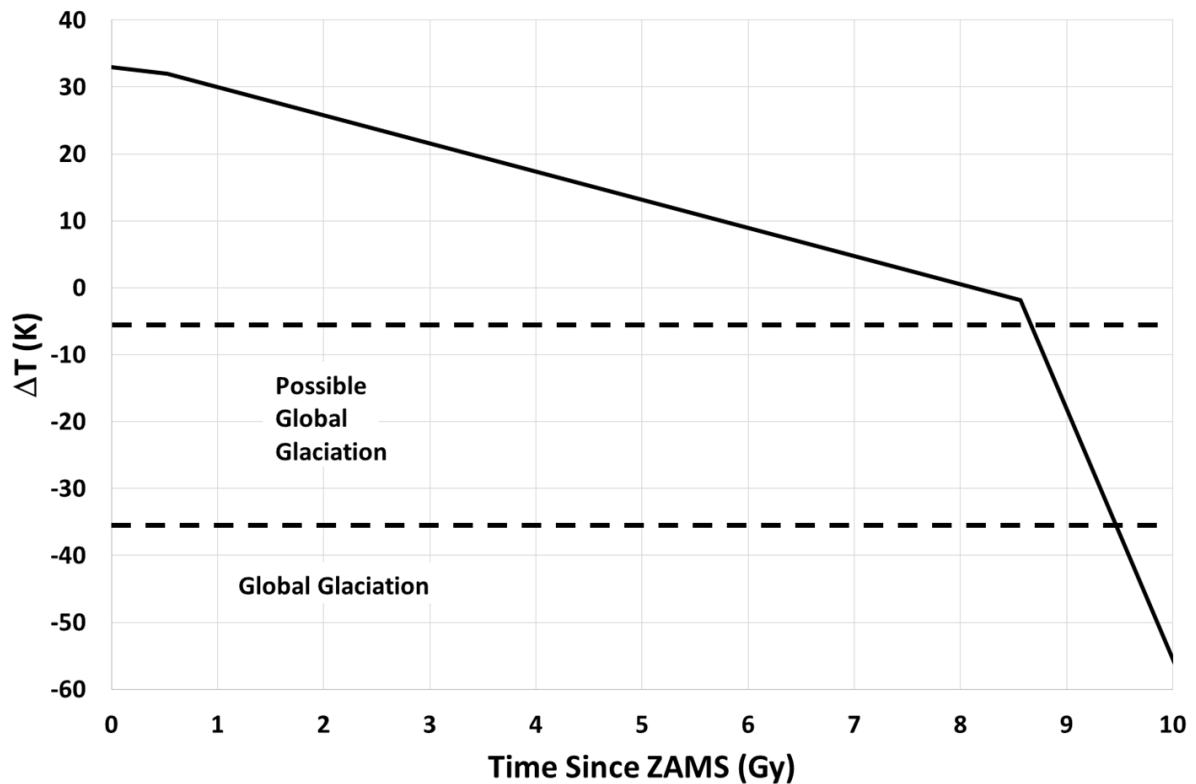
322

#### 323 4. Complications

324 The foregoing analysis assumed that the modelled planets were at the right distance from their star  
325 to ensure that their initial insolation was identical to that of the early Earth. Furthermore, there was  
326 an implicit assumption that, at any given stage of planetary evolution, equal insolation implies equal  
327 temperature; this is not quite correct since the redward shift of starlight for smaller stars results in  
328 great IR absorption and, hence, temperatures are higher for the same insolation (this produces the  
329 outward shift of the HZ boundaries with decreasing stellar mass shown in the work of Kopparapu et  
330 al. (2014)). The importance of these effects can be evaluated by increasing the initial insolation of  
331 the modelled planets to simulate the consequences of either being closer to the star or of increased  
332 absorption of IR radiation.

333 Figure 5 is identical to Fig. 4 except that the initial insolation has been increased by 100% (i.e., the  
334 planet has been moved a factor  $1/\sqrt{2}$  closer to the star) and, to be maximally conservative, it only  
335 shows the low climate sensitivity case (i.e.,  $0.2 \text{ K W}^{-1} \text{ m}^2$ ). The planet then starts with a temperature  
336 33K above Earth's initial temperature and steadily cools until it becomes glaciated after 9 to 10 Gy  
337 on the main-sequence. Comparison with Fig.4 shows that this has only extended the planet's  
338 habitable lifetime by 1 Gy. Hence, a warm-start/greater-IR-absorption does not significantly affect  
339 the conclusion that intrinsic cooling will render planets of small-stars uninhabitable much faster than  
340 their traditional habitable lifetime.





341

342 Figure 5. Predicted temperature history of an HZ planet orbiting a 0.6 solar-mass star, assuming that the planet orbited at  
 343 the right distance to give twice the initial insolation experienced by the early Earth. For simplicity, this is only shown  
 344 for the lowest climate sensitivity of  $0.2 \text{ K W}^{-1} \text{ m}^2$ . Note that, even for this extreme case, the lifetime before  
 345 glaciation is not much greater than that shown in Fig. 4.

346

347 5. Discussion

348 It must be emphasised that the modelling shown in Figs. 2, 3, 4 & 5 is not evidence supporting the  
 349 hypothesis of this paper; that would be circular reasoning because the figures were produced  
 350 assuming the hypothesis to be correct. What the modelling does show is that, if the hypothesis is  
 351 correct, planets orbiting small stars do not have significantly longer habitable lifetimes than those  
 352 orbiting solar-mass stars. It also shows that, even if the hypothesis is incorrect, intrinsic climate  
 353 cooling must closely match extrinsic stellar-warming if a planet is to have a long habitable lifetime.

354 However, if this mechanism is to be a plausible explanation for the red-dwarf-puzzle, intrinsic  
355 climate cooling rates do need to be roughly constant across Earth-like planets. The next step,  
356 therefore, is to produce evidence supporting that possibility. Coupled carbon-cycle and climate  
357 models are one way this might be achieved and some progress has already been made. The models  
358 of Krissansen-Totton & Catling (2017) and Krissansen-Totton et al. (2018) produce temperature,  
359 atmospheric-CO<sub>2</sub> and ocean-pH histories that are consistent with observational constraints.  
360 Critically, their studies show that the decreasing intrinsic warming through time results from roughly  
361 equal contributions due to continental-growth, decreasing heat-flow and biological evolution, i.e.,  
362 2/3 of the effect is due to purely geological processes that might be approximately reproduced on  
363 another Earth-like planet.

364 It is, however, possible that plate-tectonics operates very differently on other planets with different  
365 compositions and masses and that, therefore, cooling histories and outgassing histories may also be  
366 very different. At present it is difficult to investigate this in detail since there is little agreement even  
367 about the factors needed to allow plate-tectonics to occur at all. In many studies (Valencia et. al.,  
368 2007; Valencia & O'Connell, 2009; van Heck & Tackley, 2011; Foley et. al., 2012) plate tectonics is  
369 predicted to be more likely for larger planets but other models predict the opposite (O'Neill &  
370 Lenardic, 2007; Stamenković & Breuer, 2014; Noack & Breuer, 2014). It has also been claimed that  
371 size is relatively unimportant compared to other issues such as the presence or absence of water  
372 (Korenaga, 2010). These disparate conclusions occur because of different assumptions concerning  
373 mantle-rheology, lithosphere-weakening, internal temperatures and plate-initiation. Stamenković &  
374 Breuer (2014) concluded that the key factor was whether these different assumptions led to plate-  
375 yielding that was more likely, or less likely, for planets with warmer interiors. In contrast, Weller &  
376 Lenardic (2016) argued that the key difference concerned whether the mantle was primarily warmed  
377 from below or by internal radioactivity. Hence, the current situation is that we do not have a good  
378 understanding of which factors are important for plate tectonics and, therefore, of whether plate  
379 tectonics can operate at very different rates to those seen on Earth.

380 However, the geological parameters of interest (i.e., the rate of fall in the outgassing, plate-  
381 spreading and continent-growth rates) are ultimately controlled by secular cooling of Earth's interior  
382 and, whilst the precise details of this secular cooling remain contentious, a major factor must be the  
383 surface-area to volume ratio (heat losses depend on surface area and heat sources depends upon  
384 volume). Thus it is possible that rates of geological evolution will, to a first approximation, be  
385 inversely proportional to planetary radius. Rocky planets only exist up to about 10 Earth-masses  
386 which corresponds to a roughly factor of two change in radius. Hence, a large super-Earth might see  
387 intrinsic climate-forcing falling at half the rate of Earth. The implication, that geological rates might  
388 only vary by a factor of a few between planets, is partially supported by the model of Kadoya &  
389 Tajika (2015) which shows that changes in planetary mass from 1/5 of Earth to 5-times Earth (i.e., a  
390 change by a factor 25) produces less than a factor of 2 change in the effective rate of CO<sub>2</sub> outgassing.  
391 On the other hand, it is also possible that the increased uplift/erosion rates associated with  
392 increased plate-tectonic speeds have the effect of cancelling the effects of increased  
393 outgassing/ingassing (Sleep, pers. comm.) in which case intrinsic cooling will not change much with  
394 planet radius.

395 However, taking the conservative position that intrinsic cooling does depend upon planet size, the  
396 effect of the resulting small changes in intrinsic-climate-cooling rate can be gauged from Fig. 2.  
397 Figure 2 shows how the rate of initial stellar forcing changes with stellar mass and it demonstrates  
398 that a factor of two change in the rate of intrinsic-cooling would change the optimum stellar mass by  
399 about  $0.2M_{\odot}$ . For example, assume a planet orbiting a solar-mass star maintains a balance between  
400 stellar-warming and intrinsic cooling. This optimum therefore occurs when the solar constant is  
401 changing at a rate of  $72 \text{ W m}^{-2} \text{ Gy}^{-1}$ . However, this rate drops by half (to  $34 \text{ W m}^{-2} \text{ Gy}^{-1}$ ) for a  $0.8M_{\odot}$   
402 star and doubles, for a  $1.2M_{\odot}$  star, to  $141 \text{ W m}^{-2} \text{ Gy}^{-1}$ . Hence, plausible changes in planetary  
403 evolution rate may alter the optimum stellar mass slightly but will not do so sufficiently to change  
404 the conclusion of this paper (that planets orbiting small stars have reduced habitability lifetimes as a  
405 consequence of glaciation).

406 Rates of biological evolution should also be considered. It is possible that biospheres on different  
407 planets evolve at similar rates so that all three contributions to intrinsic forcing would be the same  
408 on another inhabited Earth-like world. However, that proposal lacks supporting evidence. An  
409 interesting alternative interpretation is that biological development occurs at a range of rates so that  
410 planets with slower bio-evolution would be favoured when orbiting smaller stars (i.e., the balance  
411 between extrinsic warming and intrinsic cooling would occur for smaller stars if the biological  
412 component of cooling progresses more slowly). The effect would be small, however, since the rate  
413 of increase in stellar warming drops off quickly with star mass. This can also be seen from Fig. 2  
414 since, even for a very low rate of biological evolution, the optimum stellar mass only falls slightly  
415 (i.e., it is 2/3 of the solar rate, implying no biological evolution at all, for a stellar mass of  $0.9M_{\odot}$ ).

416 Further progress, on confirming/refuting the hypothesis of this paper, requires development of  
417 more sophisticated coupled modelling of geodynamics, carbon cycles and climate. Hypothesis  
418 verification would also be significantly aided by better estimates of Earth's ancient, global, mean  
419 temperatures.

420

## 421 6. Conclusion

422 If the processes which have maintained Earth's temperate climate are common to all Earth-like  
423 worlds then HZ planets orbiting small stars will tend to suffer global glaciation within a time-frame  
424 much shorter than their traditional habitable lifetimes. Hence, resolving the faint young Sun  
425 paradox may, parsimoniously, also resolve the mystery of why Earth orbits a relatively rare and  
426 short-lived type of star. Confirming this hypothesis requires development of sophisticated models of  
427 Earth's evolution which couple secular cooling of the interior, plate-tectonics, the carbon cycle and  
428 climate.

429

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