The impact of parameterising light penetration into snow on the photochemical production of NO\textsubscript{x} and OH radicals in snow

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Abstract. Snow photochemical processes drive production of chemical trace gases in snowpacks, including nitrogen oxides (NO\textsubscript{x} = NO + NO\textsubscript{2}) and hydrogen oxide radical (HO\textsubscript{x} = OH + HO\textsubscript{2}), which are then released to the lower atmosphere. Coupled atmosphere–snow modelling of these processes on global scales requires simple parameterisations of actinic flux in snow to reduce computational cost. The disagreement between a physical radiative-transfer (RT) method and a parameterisation based upon the e-folding depth of actinic flux in snow is evaluated. In particular, the photoysis of the nitrate anion (NO\textsubscript{3}\textsuperscript{-}), the nitrite anion (NO\textsubscript{2}\textsuperscript{-}) and hydrogen peroxide (H\textsubscript{2}O\textsubscript{2}) in snow and nitrogen dioxide (NO\textsubscript{2}) in the snowpack interstitial air are considered.

The emission flux from the snowpack is estimated as the product of the depth-integrated photolysis rate coefficient, $v$, and the concentration of photolysis precursors in the snow. The depth-integrated photolysis rate coefficient is calculated (a) explicitly with an RT model (TUV), $v_{\text{TUV}}$, and (b) with a simple parameterisation based on e-folding depth, $v_{\text{e}}$. The metric for the evaluation is based upon the deviation of the ratio of the depth-integrated photolysis rate coefficient determined by the two methods, $v_{\text{TUV}}/v_{\text{e}}$, from unity. The ratio depends primarily on the position of the peak in the photolysis action spectrum of chemical species, solar zenith angle and physical properties of the snowpack, i.e. strong dependence on the light-scattering cross section and the mass ratio of light-absorbing impurity (i.e. black carbon and HULIS) with a weak dependence on density. For the photolysis of NO\textsubscript{2}, the NO\textsubscript{2} anion, the NO\textsubscript{3} anion and H\textsubscript{2}O\textsubscript{2} the ratio $v_{\text{TUV}}/v_{\text{e}}$ varies within the range of 0.82–1.35, 0.88–1.28, 0.93–1.27 and 0.91–1.28 respectively. The e-folding depth parameterisation underestimates for small solar zenith angles and overestimates at solar zenith angles around 60° compared to the RT method. A simple algorithm has been developed to improve the parameterisation which reduces the ratio $v_{\text{TUV}}/v_{\text{e}}$ to 0.97–1.02, 0.99–1.02, 0.99–1.03 and 0.98–1.06 for photolysis of NO\textsubscript{2}, the NO\textsubscript{2} anion, the NO\textsubscript{3} anion and H\textsubscript{2}O\textsubscript{2} respectively. The e-folding depth parameterisation may give acceptable results for the photolysis of the NO\textsubscript{3} anion and H\textsubscript{2}O\textsubscript{2} in cold polar snow with large solar zenith angles, but it can be improved by a correction based on solar zenith angle and for cloudy skies.

1 Introduction

Field and laboratory experiments over the past 2 decades have provided evidence that photochemical reactions occurring within snow lead to the emission of various gaseous compounds from the snowpack (e.g. Jacobi et al., 2004; Jones et al., 2000; Beine et al., 2002, 2006; Dibb et al., 2002; Simpson et al., 2002) and production of radicals, e.g. hydroxyl radical (OH), within the snowpack (e.g. Mauldin et al., 2001; Chen et al., 2004; Sjostedt et al., 2005; France et al., 2011). The porous structure of snowpacks allows the exchange of gases and particles with the atmosphere. The exchange between snowpack and overlying atmosphere depends on dry and wet deposition, transport (including wind pumping and diffusion) and snow microphysics (e.g. Bartels-Rausch et al., 2014). Thus snow can act as both a source and a sink of atmospheric chemical species as summarised in Bartels-Rausch et al. (2014) and Grannas et al. (2007). Photochemistry in the snowpack needs to be fully understood because (1) emitted photolysis products play an impor-
tant role in determining the oxidising capacity of the lower atmosphere – e.g. concentration of O$_3$, HO$_x$, H$_2$O$_2$ – and (2) chemical preserved in ice cores, and potential palaeo-climate proxies, may be altered by reactions with OH radicals, photolysis or physical uptake and release (Wolff and Bales, 1996).

The photolytic lifetime of a chemical species in the snowpack is the reciprocal of the photolysis rate coefficient (also known as the photodissociation rate coefficient), $J$, which is dependent on the actinic flux (also known as spherical or point irradiance) in the snowpack, $I$, the quantum yield of the photolysis reaction, $\Phi$, and absorption cross section of the photolysing species, $\sigma$.

$$J(\theta, z, T) = \int \sigma(\lambda, T) \Phi(\lambda, T) I(\theta, z, \lambda) d\lambda,$$

where $\theta$ is solar zenith angle, $z$ is the depth into the snowpack, $\lambda$ is the wavelength of the incident solar radiation and $T$ is the temperature of the snowpack.

Under clear-sky conditions, a homogeneous snowpack can be separated into two optical layers based on the propagation of actinic flux from the surface into the snow: the near-surface layer, i.e. the top few centimetres of the snowpack, where direct solar radiation is converted to diffuse radiation. Below the near-surface layer is the asymptotic zone, where all solar radiation is diffuse and will decrease exponentially with depth (Warren, 1982).

The relationship between actinic flux (and the photolysis rate coefficient) and depth is complex near the surface of the snowpack due to rapidly changing contributions from both direct and diffuse radiation. Enhancement or attenuation of actinic flux in the near-surface layer compared to above the snow is dependent on the solar zenith angle (Fig. 1 and Fig. 4 in Lee-Taylor and Madronich, 2002). Snowpack is a very scattering and low absorption environment for UV–visible photons with individual snow grains tending to forward-scatter photons (Warren, 1982). The enhancement in actinic flux compared to above the snow occurs for solar zenith angles $< 50^\circ$. For solar zenith angles $\sim 50^\circ$ actinic flux will decrease almost exponentially with depth (Wiscombe and Warren, 1980). For direct radiation from a low sun (large solar zenith angle, i.e. $> 50^\circ$) there is a larger probability that the photons will be scattered upwards and out of the snowpack, leading to a rapid decrease in actinic flux with depth in the first few centimetres of the snowpack, i.e. decreasing faster than exponential (Warren, 1982).

In the asymptotic zone radiation is diffused, and provided that the snowpack is semi-infinite – i.e. the albedo of the surface underlining the snow does not affect the calculation of the actinic flux within the snowpack – the radiation decreases exponentially according to Beer–Lambert law (France et al., 2011, define semi-infinite as 3–4 $e$-folding depths).

$$I(z, \lambda) = I_0 e^{-\frac{z-z_e}{(\text{depth})}},$$

where $I_0$ is the actinic flux at a reference depth $z_0$ within the asymptotic zone, and $z_e(\lambda)$ is the asymptotic $e$-folding depth at which $I$ has decayed to $1/e$, $\sim 37\%$ of its reference value, $I_0$.

Radiative-transfer (RT) models, such as the TUV-snow model (Lee-Taylor and Madronich, 2002), were developed to capture the non-exponential attenuation of radiation near the surface of the snowpack. However, running a radiative-transfer model is a time-consuming step within large-scale (e.g., 3-D) chemical transport models or global climate models, so photolysis rate coefficients in the snowpack, $J$, are often parameterised with $e$-folding depth (e.g., Thomas et al., 2011), i.e.

$$J_{z_e}(\theta, z) = J_0(\theta) e^{-\frac{z-z_e}{(\text{depth})}},$$

where $J_{z_e}(\theta, z)$ is the parameterised photolysis rate coefficient at depth $z$; $J_0(\theta)$ is the photolysis rate coefficient at the surface of the snowpack at solar zenith angle $\theta$; and $z_e$ is the $e$-folding depth of the snowpack. The aim of this paper is to investigate the accuracy of the $e$-folding depth parameterisation (Eq. 3) relative to a value of $J$ calculated using a physically explicit RT model and Eq. (1). The metric to compare the two models is the depth-integrated photolysis rate coefficient (also known as the transfer velocity; France et al., 2007), which may be considered approximately proportional to the flux of potential gaseous photo-produced compounds.

### Figure 1. Depth profile within “cold polar snow” (base case: $\rho = 0.4$ g cm$^{-3}$, $[\text{BC}] = 4$ ng(C) g$^{-1}$ and $\sigma_{\text{scatt}} = 25$ m$^2$ kg$^{-1}$) of actinic flux, $I$, at $\lambda = 451$ nm at different solar zenith angles $\theta$.
The depth-integrated photolysis rate coefficient, $v$, is calculated (Simpson et al., 2002) as

$$v(\theta) = \int J(\theta, z) \, dz. \quad (4)$$

The depth-integrated production rate of a chemical species $B$ from the photolysis of a chemical species $A$, $F_B(\theta)$, is the product of concentration of $A$, $[A]$, and the depth-integrated photolysis rate coefficient, $v_A$, assuming the concentration of $A$ is constant with depth.

$$F_B(\theta) = [A] v_A(\theta) \quad (5)$$

For example, the photolysis of the nitrate anion, NO$_3^-$, is important and has therefore been studied extensively in the past. It leads to emission of nitrogen oxides (NO$_x$ = NO + NO$_2$) to the atmosphere. The following reactions summarise the main channels of NO$_3^-$ production from NO$_3^-$ photolysis in snowpack. The quantum yield and absorption cross section of all the chemical species used in this study are listed in Table 1.

<table>
<thead>
<tr>
<th>Reaction</th>
<th>Reference for $\Phi$</th>
<th>Quantum yield, $\Phi$ at 258 K</th>
<th>Action spectrum peak, $\lambda_{\text{act peak}}$, nm</th>
</tr>
</thead>
<tbody>
<tr>
<td>R1</td>
<td>Chu and Anastasio (2003)</td>
<td>0.00338</td>
<td>321</td>
</tr>
<tr>
<td>R2</td>
<td>Warneck and Wurzinger (1988)</td>
<td>0.00110</td>
<td>321</td>
</tr>
<tr>
<td>R3</td>
<td>Chu and Anastasio (2007)</td>
<td>0.12066$^a$</td>
<td>345</td>
</tr>
<tr>
<td>R4</td>
<td>Gardner et al. (1987)</td>
<td>0.97900</td>
<td>375</td>
</tr>
<tr>
<td>R7</td>
<td>Chu and Anastasio (2005)</td>
<td>0.68300</td>
<td>321</td>
</tr>
</tbody>
</table>

Species | Reference for $\sigma$
---|---------------------|
NO$_3^-$ | Chu and Anastasio (2003) |
NO$_2^-$ | Chu and Anastasio (2007) |
NO$_2$ | DeMore et al. (1997) |
H$_2$O$_2$ | Chu and Anastasio (2005) |

$^a$ Quantum yield at $\lambda = 345$ nm, the photochemical action spectrum peak of the NO$_3^-$ anion.

Long-wavelength UV light penetrates deeper into the snowpack than shorter-wavelength UV. Therefore, NO$_2$ photolyses within the snowpack and may produce ozone (Reactions R4 and R5).

$$\text{NO}_2 + h\nu \rightarrow \text{NO} + \text{O}^3\text{P}, \quad \lambda_{\text{act peak}} = 375\text{ nm}, \quad (R4)$$

$$\text{O}^3\text{P} + \text{O}_2 + M \rightarrow \text{O}_3 + M \quad (R5)$$

Studies have also demonstrated that photolysis of NO$_3^-$ and NO$_2^-$ in snow and ice contribute to the formation of OH radicals within the snowpack (Dubowski et al., 2001, 2002; Cotter et al., 2003; Chu and Anastasio, 2003; Anastasio and Chu, 2008) through reaction of oxygen radical anion (O$^-$) with water (Reaction R6).

$$\text{O}^- + \text{H}_2\text{O} \rightarrow \text{OH} + \text{OH}^- \quad (R6)$$

In the presence of oxygen, formation of the OH radical may create a radical-initiated oxidising medium allowing oxidation of organic chemicals to emit species such as formaldehyde, acetaldehyde or organic halogens to the lower atmosphere (McNeill et al., 2012). Another source of OH radicals in the snowpack is photolysis of hydrogen peroxide (H$_2$O$_2$) (Chu and Anastasio, 2005, 2007):

$$\text{H}_2\text{O}_2 + h\nu \rightarrow 2\text{OH}, \quad \lambda_{\text{act peak}} = 321\text{ nm}. \quad (R7)$$

The ratio of the depth-integrated photolysis rate coefficients, $Q = \frac{\Phi_{\text{UV}}}{\Phi_{\text{vis}}}$, determined from the two methods – the RT model and e-folding depth parameterisation – were calculated for the photolysis of NO$_3^-$, NO$_2^-$, NO$_2$ and H$_2$O$_2$ in snow. Reactions rate coefficients for Reactions (R1)–(R4) and (R7) were determined for hypothetical snowpacks with different physical and optical properties and under different environmental conditions, e.g. total column ozone.
2 Modelling procedure

The hypothetical homogeneous snowpacks defined in this study were based on three different types of snow – cold polar, wind-packed and melting snow (Table 2, Marks and King, 2014). The snowpacks are assumed to be semi-infinite.

Sensitivity tests calculating \( Q \) were run against the following parameters – base case: a typical cold polar snowpack; case 1: the density of the snowpack was varied; case 2: the scattering cross section was varied; case 3: the black carbon (BC) mass ratio was varied; case 4: the HUmid Like Substances (HULIS) mass ratio was varied; case 5: the mass ratio with both BC and HULIS was varied; case 6: the asymmetry factor was varied; and case 7: the total column ozone was varied. Values for these parameters, listed in Table 2, were selected based on previous field measurements made in various geographic locations and conditions (i.e. Grenfell et al., 1994; Beagleshole et al., 1998; King and Simpson, 2001; Fisher et al., 2005; France et al., 2010; Marks and King, 2014).

In case 1, snow densities were varied in the range observed typically in natural snowpack of 0.2–0.6 g cm\(^{-3}\) (Marks and King, 2014, and references therein).

In cases 2–5, the scattering cross section and mass ratio of light-absorbing impurities of the snowpack were varied – both of which have an impact on the propagation of actinic flux within the snowpack. The reciprocal of the \( e \)-folding depth, \( \tau_e \), is the asymptotic flux extinction coefficient, \( \kappa_{ext} \), which is the sum of the scattering, \( r_{scatt} \), and absorption coefficients, \( \mu \) (Lee-Taylor and Madronich, 2002). The scattering and absorption coefficients describe the attenuation per unit length, and both are density-dependent (Lee-Taylor and Madronich, 2002). For general use, the following scattering, \( \sigma_{scatt} \), and absorption, \( \sigma_{abs} \), cross sections are introduced:

\[
\sigma_{ext} = \sigma_{scatt} + \sigma_{abs}. \tag{6}
\]

where \( \sigma_{ext} = \kappa_{ext}/\rho \) is the extinction cross section, \( \sigma_{scatt} = r_{scatt}/\rho \) is the scattering cross section of snow and \( \sigma_{abs} = \mu/\rho \) is the absorption cross section of snow and light-absorbing impurities. In case 2, values of \( \sigma_{scatt} \) were selected to cover a wide range of snow types (Table 2). The values of the scattering cross section are assumed to be independent of wavelength (Lee-Taylor and Madronich, 2002).

The absorption cross section of snowpack is due to wavelength-dependent absorption by ice, \( \sigma_{abs}^{ice} \), and light-absorbing impurities, \( \sigma^{+} \), such as black carbon and HULIS:

\[
\sigma_{abs} = \sigma_{abs}^{ice} + \sigma^{+}. \tag{7}
\]

Warren et al. (2006) showed that BC can dominate the absorption in snow as it is a factor of \(~50\) more efficient absorber of light than mineral dust particles of the same mass. Thus in sensitivity test case 3, black carbon is considered to be the only light-absorbing impurity. For the work presented here the light-absorption cross section of black carbon, \( \sigma_{BC}^{+} \), is assumed to be wavelength-independent and equal to \(~10 \text{ m}^2 \text{ g}^{-1}\) (France et al., 2010; Lee-Taylor and Madronich, 2002). To account for all pollution scenarios, from clean to dirty, the mass ratio of black carbon is varied from 4 to 128 ng g\(^{-1}\), to cover the concentration range typically measured in coastal (Beagleshole et al., 1998), Antarctica-near research stations (Zatko et al., 2013) or in midlatitude snow. Other common pollutants found in snow samples include HULIS, which represent an important fraction of biomass burning, biogenic and marine aerosol etc. (e.g. Voisin et al., 2012). HULIS absorb most effectively in the UV region of the solar spectrum, and the absorption cross section decreases towards the visible (Hoffer et al., 2006). Concentrations of HULIS measured in polar snow vary between 1 and 1000 ng g\(^{-1}\) and depend on the measurement method (Voisin et al., 2012; France et al., 2012), which is taken into account by the range of values used in case 4. In natural snow, it is rare that HULIS would be the only light-absorbing impurity within snow as shown in France et al. (2011) and France and King (2012); therefore, in case 5 a combination of both black carbon and HULIS were used and varied.

In case 6, the asymmetry factor, \( g \), is the average cosine of the scattering angle and is a measure of the preferred scattering direction. Sensitivity tests were run with two different values of \( g \) of 0.89 and 0.86 as discussed by Marks and King (2014) and Libois et al. (2014) respectively. Both selected values are close to 1, indicating light scattering by snow grains is dominated by forward scattering.

Within case 7, column ozone values were varied to cover the seasonal and spatial variability observed above the polar regions. The effect of column ozone on the depth-integrated photolysis rate coefficient ratio was explored as downwelling UV radiation is very sensitive to stratospheric ozone absorption and the attenuation is a strong function of wavelength. Typical value of column ozone in Antarctica (also the glacial average; Kroon et al., 2008) is about 300 DU but can be as low as 150 DU in the Antarctic O\(_3\) hole (Kramarova et al., 2014). Column ozone generally increases from the tropics to midlatitudes. Therefore, there are three different values of total column ozone: 200, 300 and 400 DU.

\begin{table}[h]
\centering
\caption{Properties of snow type studied. Optical and physical properties are based on work by Marks and King (2014) and references therein.}
\begin{tabular}{lll}
\hline
Snow type & \( \rho \) & \( \sigma_{scatt} \) \\
& g cm\(^{-3}\) & cm\(^2\) kg\(^{-1}\) \\
\hline
Cold polar snow & 0.2–0.6 & 15–25 \\
Wind-packed snow & 0.2–0.6 & 5–10 \\
Melting snow & 0.2–0.6 & 0.2–2 \\
\hline
\end{tabular}
\end{table}
Table 3. Optical properties of the snowpacks used. The bold numbers are to highlight the optical property that is varying in that particular case.

<table>
<thead>
<tr>
<th>Designation</th>
<th>$\rho$ g cm$^{-3}$</th>
<th>[BC] ng(C) g$^{-1}$</th>
<th>$\sigma_{\text{scatt}}$ m$^2$ kg$^{-1}$</th>
<th>O$_3$ col. DU</th>
<th>g</th>
<th>$z_e$ cm$^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Base case</td>
<td>0.4</td>
<td>4.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>13.3</td>
</tr>
<tr>
<td>Case 1</td>
<td><strong>0.2</strong></td>
<td>4.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>25.2</td>
</tr>
<tr>
<td>Density of snowpack</td>
<td><strong>0.6</strong></td>
<td>4.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>9.1</td>
</tr>
<tr>
<td>Case 2</td>
<td>0.4</td>
<td>4.0</td>
<td>2</td>
<td>300</td>
<td>0.89</td>
<td>35.3</td>
</tr>
<tr>
<td>Scattering cross section</td>
<td>0.4</td>
<td>4.0</td>
<td>7</td>
<td>300</td>
<td>0.89</td>
<td>24.4</td>
</tr>
<tr>
<td>Case 3</td>
<td>0.4</td>
<td><strong>0.18</strong></td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>36.9</td>
</tr>
<tr>
<td>Black carbon content</td>
<td>0.4</td>
<td><strong>32.0</strong></td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>4.9</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td><strong>128.0</strong></td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>2.5</td>
</tr>
<tr>
<td>Case 6, g</td>
<td><strong>0.4</strong></td>
<td>4.0</td>
<td>25</td>
<td>300</td>
<td><strong>0.86</strong></td>
<td>12.0</td>
</tr>
<tr>
<td>Ozone column</td>
<td>0.4</td>
<td>4.0</td>
<td>25</td>
<td>200</td>
<td>0.89</td>
<td>13.3</td>
</tr>
<tr>
<td>Case 7</td>
<td>0.4</td>
<td>4.0</td>
<td>25</td>
<td><strong>400</strong></td>
<td>0.89</td>
<td>13.3</td>
</tr>
<tr>
<td>HULIS content</td>
<td>0.4</td>
<td><strong>1.0</strong></td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>36.9</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td><strong>8.0</strong></td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>22.0</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td><strong>17.0</strong></td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>15.3</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td><strong>1000.0</strong></td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>2.06</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td><strong>17.0</strong></td>
<td>2</td>
<td>300</td>
<td>0.89</td>
<td>37.0</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td><strong>1000.0</strong></td>
<td>2</td>
<td>300</td>
<td>0.89</td>
<td>7.3</td>
</tr>
<tr>
<td>Case 5</td>
<td><strong>[BC] + [HULIS]</strong></td>
<td><strong>0.6 + 8</strong></td>
<td>7</td>
<td>300</td>
<td>0.89</td>
<td>30.6</td>
</tr>
</tbody>
</table>

*For cases 1–2 and 4–6, the reported $e$-folding depth, $z_e$, is the average of $e$-folding depth at 321, 345 and 375 nm. For cases 3 and 7, $z_e$ is the $e$-folding depth at 321 nm.

2.1 RT method: radiative-transfer model, TUV

The attenuation of actinic flux with depth was calculated by a coupled atmosphere-snow radiative-transfer model, TUV 4.4, using an eight-stream DISORT (Discrete Ordinates Radiative Transfer Program for a Multi-Layered Plane-Parallel Medium) model (Lee-Taylor and Madronich, 2002). The model treats the snow as a weakly absorbing, very scattering homogenous layer with its optical properties described by the variables $g$, $\sigma_{\text{scatt}}$, and $\sigma_{\text{abs}}$. The snowpacks were modelled as described in detail in Lee-Taylor and Madronich (2002) except the absorption cross section of ice was updated to values given by Warren and Brandt (2008). The model configuration in this study used 110 snowpack layers with 1 mm spacing in the top 1 cm and 1 cm spacing for the rest of the 1 m snowpack, and 72 atmospheric layers with 1 m spacing for the first 10 m above snowpack surface then 10 m intervals until 100 m, 100 m interval up to 1 km, 1 km intervals up to 10 km and 2 km intervals up to 80 km, with no atmospheric loading of aerosol and assumed clear-sky conditions.

Values of the photolysis rate coefficient, $J$, for Reactions (R1)–(R4) and (R7) were calculated by TUV using Eq. (1). The absorption cross section of the chromophores in the ice phase are assumed to be the same as the aqueous phase and are listed with temperature-dependent quantum yields for reactions used in this study (Table 1). Photolysis rate coefficients calculated with the TUV are referred to as the “RT method”.

2.2 $z_e$ method: $e$-folding depth

The $e$-folding depths, $z_e$, for the snowpacks described in Table 3 were calculated by fitting Eq. (2) to an actinic flux depth profile through snowpack obtained from TUV with a vertical resolution of 1 cm from 20 cm below the snowpack surface. At this depth, radiation is effectively diffuse and decays exponentially with depth (asymptotic zone). Field measurements of $e$-folding depth have been previously carried out over similar depths in the snowpack (e.g. France and King, 2012).

Values of $z_e$ were determined for three wavelengths ($\lambda = 321, 345$ and 375 nm) and at seven different solar zenith angles ($0, 36.9, 53.1, 66.4, 78.5, 80$ and $90^\circ$). These wavelengths were chosen as they represent the peak of the photolysis rate coefficient.
tolyis action spectrum for each chemical species (Table 1). The photolysis rate coefficients were approximated by scaling the surface photolysis rate coefficient calculated by the RT method (TUV model) with the average e-folding depth, $z_e$, over seven solar zenith angles at a wavelength that is near the peak of the action spectrum of the chemical species (as shown in Eq. 3). For example in the case of NO$_3^-$ photolysis,

$$J_{z_e, NO_3^-}(\theta, z) = J_{NO_3^-}(\theta, z_0) e^{-\frac{z-z_0}{\lambda_e} \frac{321 \text{ nm}}{cm}}$$

(8)

where $J_{z_e, NO_3^-}(\theta, z)$ is the parameterised photolysis rate coefficient at depth $z$; $J_{NO_3^-}(\theta, z_0)$ is the photolysis rate coefficient of NO$_3^-$ at the surface obtained by the RT method (TUV model); and $z_e(321 \text{ nm})$ is the e-folding depth at a wavelength of 321 nm. For clarity, this e-folding depth parameterisation is called the “$z_e$ method”.

2.3 Ratio of depth-integrated photolysis rate coefficients

To determine the accuracy of the $z_e$ method relative to the RT method, the ratio of depth-integrated photolysis rate coefficients, $Q$, was determined. The $Q$ ratio is defined as depth-integrated photolysis rate coefficient calculated with the RT method over the depth-integrated photolysis rate coefficients estimated by the $z_e$ method. For example, $Q$ in the case of NO$_2$ (Reaction R1) is given by

$$Q = \frac{v_{TUV, NO_2}}{v_{z_e, NO_2}} = \frac{\int J_{NO_3^- \rightarrow NO_2}(z) dz}{J_{NO_3^- \rightarrow NO_2}(z_0) \int e^{-\frac{z-z_0}{\lambda_e} \frac{321 \text{ nm}}{cm}} dz}$$

(9)

where $J_{z_e, NO_3^- \rightarrow NO_2}(z_0)$ is the photolysis rate coefficient for NO$_3^-$ photolysis at the surface of the snowpack. For Reactions (R3), (R4) and (R7), the surface photolysis rate coefficients were scaled, with $e^{-\frac{z-z_0}{\lambda_e} \frac{321 \text{ nm}}{cm}}$ with e-folding depth at 345, 375 and 321 nm respectively for each depth $z$.

3 Results and discussion

The study evaluates the accuracy of parameterisation of photolysis rate coefficient to variation in solar zenith angle, different photolysis precursors, snowpack properties and total column ozone. Correction factors were also found for each different species to improve the performance of the $z_e$ method.

3.1 The response of e-folding depth to solar zenith angle and wavelength

Radiation in the asymptotic layer, i.e. below the first few centimetres of the snow surface (Fig. 1), decreases exponentially with depth as observed previously at various polar and non-polar sites (Warren and Wiscombe, 1980; Marks and King, 2014; Fisher et al., 2005; King and Simpson, 2001). Table 3 lists the average e-folding depth across seven solar zenith angles for all cases. For the base case, cases 1–3, 6 and 7, the e-folding depths listed are averaged not only across solar zenith angles but also across three wavelengths (321, 345 and 375 nm). There are no significant differences between the calculated e-folding depths, across different solar zenith angles or across the three wavelengths of which the variation coefficients are between 0.002 and 2 %. For snowpacks in cases 4 and 5, the e-folding depths were at a single wavelength (321 nm) only and the variation coefficients range from 0.007 to 0.16 %. Figure 2 shows how e-folding depth varies with wavelength and density, black carbon mass ratio, HULIS mass ratio or scattering cross section of the snowpack. At all wavelengths, the e-folding depth decreases with increasing snow density, and increasing the mass ratio of the black carbon increased the absorption of incident radiation.

Absorption of HULIS is wavelength-dependent; i.e. increasing mass ratio of HULIS only increases absorption of UV and near-UV radiation. However, the absorption of the incident radiation in the visible wavelengths is independent of the mass ratio of HULIS. Increasing the scattering cross section also leads to a decrease in e-folding depth.

Scattering of photons typically occurs at the air–ice interface of a snow grain and absorption occurs within the snow grain. A denser snowpack implies more scattering or absorp-
tion events per unit length. A larger scattering cross section will typically reduce the path length of a photon through the snowpack and reduce the possibility for absorption by ice or light-absorbing impurities. Therefore, increases in density, light-absorbing impurities and scattering cross section result in a smaller e-folding depth.

3.2 Variation of $Q$, ratio of depth-integrated photolysis rate coefficients

Depth-integrated photolysis rate coefficients of the four chemical species considered (NO$_3^-$, NO$_2^-$, H$_2$O$_2$ and NO$_2$) were calculated by the RT method and the $z_e$ method. To evaluate the accuracy of the approximation by the $z_e$ method, the ratio $Q$ ($\frac{\text{TUV}}{\text{RT}}$ using Eq. 9), is calculated and considered independently.

3.2.1 Variation with solar zenith angle

When the solar zenith angle is between 0 and 37°, using the $z_e$ method leads to a depth-integrated photolysis rate coefficient ratio, $Q$, of up to 1.35 (Fig. 3). The underestimation of the $z_e$ method at small solar zenith angles is due to the enhancement of actinic flux compared to above the surface in the near-surface layer being considered in the RT method but being neglected in the $z_e$ method. For solar zenith angles around 50° and larger than 80° the value of $Q$ is close to unity, suggesting the $z_e$ method may be a good approximation for these solar zenith angles. Wiscombe and Warren (1980) suggested that solar illumination around a solar zenith angle of 50° was effectively the same as diffuse radiation, which decreases exponentially with depth from the snow surface. At large solar zenith angles ($>80°$) there is little direct solar radiation relative to diffuse radiation illuminating the snowpack and the snowpack is effectively illuminated by diffuse radiation; thus the difference between the two methods is small. Between the solar zenith angles of ~66 and 75°, i.e. minimum values of $Q$ in Fig. 3, the direct radiation entering the snowpack may be potentially scattered out of the snowpack due to the strong forward-scattering property of snow. Hence, the actinic flux attenuates at a quicker rate than the e-folding depth in the near-surface zone, and the $z_e$ method overestimates the intensity of solar radiation in the snowpack.

In reality, only high-altitude glaciers in the tropics, such as those found in the Himalayas or Andes, would experience the overhead sun or small solar zenith angles in the summer. In the polar regions, where snow emission can dominate boundary layer chemistry (e.g. Davis et al., 2004), solar zenith angles vary between 42.8° (Antarctic/Arcatic Circle) and 66.5° (at the pole) at summer solstice and close to or greater than 90° during winter solstice for the Antarctic/Arcatic Circle. Within this solar zenith angle range, the $z_e$ method is most likely to yield small overestimates of fluxes and photochemical production rate. However, small “effective” solar zenith angles can be achieved in sloping snow-covered terrain, as shown in Fig. 4. The effective solar zenith angle, $\theta_{\text{eff}}$, on a snow-covered slope is the difference between the solar zenith angle normal to a horizontal surface, $\theta_{\text{dir}}$, and the angle of the slope, $\phi$. Therefore, the $z_e$ method might lead to underestimation of depth-integrated production rates on snow-covered mountains.

3.2.2 Variation with chemical species and total column ozone

The value of the ratio $Q$ for the photolysis of the NO$_3^-$ anion and H$_2$O$_2$ is very similar in terms of its response to changing solar zenith angle (Fig. 3a and b). The maximum and minimum values of $Q$ are ~1.27 (underestimation of solar radiation by the $z_e$ method), at direct overhead sun, and ~0.92 (overestimation of solar radiation by the $z_e$ method), at solar zenith angles of ~66–70°. The disagreement between the two methods for the photolysis of NO$_2^-$ is slightly larger,
with the ratio $Q$ ranging between 0.88–1.28 (Fig. 3c). The approximation with the $z_e$ method is the most inaccurate for the photolysis of NO$_2$ within snowpack interstitial air, having $Q$ values range between 0.82 and 1.35 (Fig. 3d).

The NO$_3^-$ anion and H$_2$O$_2$ have the peak of their action spectrum in the UV-B, while the NO$_3^-$ anion and NO$_2$ have a peak in near-UV and visible wavelengths respectively. Solar radiation in the UV region is less intense and more diffuse relative to the UV-A and visible radiation at the snow surface as (1) the ozone layer absorbs strongly in the UV-B and UV-C while relatively weakly in the UV-A and almost negligibly in the visible region and (2) the Rayleigh scattering of photons by air molecules increases as the wavelength decreases. The actinic flux attenuation profile with depth, in snow, of more diffused actinic flux can be better approximated by the $e$-folding depth; therefore, the $z_e$ method provides a better estimation of photolysis rate coefficient profile for NO$_3^-$ and H$_2$O$_2$ compared to NO$_2$ and NO$_2$.

The wavelength of the peak in the action spectrum of a chemical species also has an impact on its response to changes in column ozone concentration (case 7) in terms of photolysis rate coefficient. The surface photolysis rate coefficients for NO$_3^-$ and H$_2$O$_2$ are more sensitive to the changes in column ozone, due to their action spectrum peak in the UV-B region, compared to species that have their peak in UV-A, such as NO$_2^-$ and NO$_2$. The surface values of $J_{NO_3^-}$ (Fig. 5a) and $J_{H_2O_2}$ increased by $\sim 20\%$ when total ozone column decreased from 300 to 200 DU, while surface values of $J_{NO_2}$ and $J_{NO_2}$ (Fig. 5b) only increased by approximately 6 and 0.9% respectively. When total ozone column increased from 300 to 400 DU, surface values of $J_{NO_3^-}$ and $J_{H_2O_2}$ dropped approximately by $\sim 14\%$, whereas surface values of $J_{NO_2}$ and $J_{NO_2}$ only decreased by $\sim 5$ and 0.6% respectively.

Despite the value of the photolysis rate coefficient varying with values of different column ozone, especially for the NO$_3^-$ anion and H$_2$O$_2$, the propagation of radiation throughout the snowpack was not affected by the column ozone; i.e. the value of $Q$ was unchanged by changing the ozone column, and the $z_e$ method is not sensitive to ozone column values.

3.2.3 Variation with snow physical properties

Density (case 1), scattering cross section (case 2), light-absorbing impurities (cases 3–5) and asymmetry factor (case 6) were considered as the four varying physical properties of the snowpack in this study. Figure 3 highlights three results in terms of various physical properties of the snowpacks: Firstly, snow density has a small effect on the ability of the $z_e$ method to reproduce the results of RT method. Secondly, the $z_e$ method underestimates depth-integrated photolysis rate coefficients significantly for relatively clean snowpacks and snowpacks with low scattering cross section at small and large solar zenith angles. Thirdly, changes of $Q$ with increasing mass ratio of light-absorbing impurities depend on the chemical species being photolysed. All three of these effects depend on either the ratio of direct to diffuse radiation in the top of the snowpack or the conversion of direct solar radiation to diffuse solar radiation in the near-surface layer of the snowpack.

With regard to the density of the snowpack, the photolysis rate coefficient maxima are at a deeper depth for snowpacks with lower density. That is, the path length of the photon is longer for less-dense snowpacks. However, for the range of density values found in natural snow (case 1, $\rho = 0.3$–0.6 g cm$^{-3}$) the difference in the $Q$ ratio is very small, of the order of $\sim 3.5\%$ (red symbols and lines in Fig. 3).

Scattering cross section of the snowpack: lower values of the scattering cross section imply longer path length of the photon between individual scattering events. Hence, the maximum photolysis rate coefficients tend to occur deeper into the snowpacks, as shown in blue in Fig. 6 (Scatt2, i.e. melting snow), compared with snowpacks that have a larger scattering cross section (magenta in Fig. 6, BaseC, i.e. cold polar snow). Thus for snowpacks with a small scattering cross section the agreement between the RT and $z_e$ methods is likely to be poor as the $z_e$ method will not capture the behaviour in the near-surface layer accurately.

Light-absorbing impurities in the snowpack: the propagation of actinic flux and the vertical variation of photolysis rate coefficient within snowpack is dominated by scattering when light-absorbing impurity contents are low and therefore the absorption properties of the impurity become unimportant, i.e. there is no difference between the value of $Q$ for snowpack BC0.18 and HULIS1 listed in Table 3. In case 3, absorption due to black carbon, the variation of $Q$ with solar zenith angle is approximately the same for the photolysis of NO$_3^-(\lambda \sim 321 \text{ nm})$, H$_2$O$_2(\lambda \sim 321 \text{ nm})$, NO$_2^-(\lambda \sim 345 \text{ nm})$ and NO$_2(\lambda \sim 375 \text{ nm})$. Except for heavily polluted snow, e.g. snowpack BC128 ($\rho = 0.4$ g cm$^{-3}$, [BC] = 128 ng (g$^{-1}$) and $\sigma_{\text{scatt}} = 25$ m$^2$ kg$^{-1}$), the ratio $Q$ for photolysis of the NO$_2^-$ anion and NO$_2$ deviated from
snowpacks with lower black carbon mass ratio slightly (~3 and ~3.5% respectively). In Fig. 6, black lines representing the extreme polluted case – BC128 – the photolysis rate coefficient calculated by the two methods matches at around 2 cm depth for the NO$_3^-$ anion, but ~4 and ~5 cm for the NO$_2^-$ and NO$_2$ respectively. The latter two compounds have the peak of their action spectrum at larger wavelengths relative to the NO$_3^-$ anion and H$_2$O$_2$ as discussed in Sect. 3.2.2. The ratio of direct to diffuse incident radiation in the snowpack increases with wavelength around 300–400 nm and will increase the difference between the photolysis rate coefficient depth profile calculated by the $z_e$ and RT methods especially in the top few centimetres of the snowpack.

In case 4, the absorption due to HULIS is considerable. A mass ratio of 100 ng g$^{-1}$ of HULIS in the snowpack will reduce the photolysis of NO$_3^-$ anion and H$_2$O$_2$ much more than the photolysis of NO$_2^-$ and NO$_2$ as HULIS absorption cross section increases with decreasing wavelengths. The absorption cross section due to 1, 8, 17 and 1000 ng g$^{-1}$ of HULIS is respectively equivalent to 0.18, 1.4, 3.0 and 177 ng(C) g$^{-1}$ of black carbon at 321 nm, but only equivalent to 0.11, 0.87, 1.85 and 109 ng(C) g$^{-1}$ of black carbon at 345 nm and 0.06, 0.50, 1.05 and 62.0 ng(C) g$^{-1}$ of black carbon at 375 nm. If the light-absorption by impurities in a snowpack is dominated by black carbon, then the value of $e$-folding depth in the UV-B and UV-A will be similar. However, if the light-absorption in the snow is dominated by HULIS (or even dust), then strictly a different $e$-folding depth is needed for each wavelength that is characteristic of the photolysis of the species of interest.

Asymmetry factor of the snowpack: Libois et al. (2014) recently suggested that the value of the asymmetry parameter, $g$, should be $g = 0.86$ due to non-spherical grains observed in the laboratory and in the field in Antarctica and the French Alps. The $e$-folding depth is sensitive to the value of the asymmetry factor as shown by Libois et al. (2013). Reducing the asymmetry factor from 0.89 to 0.86 reduces the tendency of photons being forward-scattered, and hence the $e$-folding depth is reduced by ~11%. The reduction in photolysis rate coefficient is also ~11%. Nevertheless, there are no significant relative differences between the RT and $z_e$ methods for changing $g$. The parameterisation with $e$-folding depth generated a similar approximation of photolysis rate coefficient for either of the two $g$ values. The other properties of the snowpacks were unchanged.

### 3.3 Parameterisation correction

The difference in the depth-integrated photolysis rate coefficient, $v$, between the $z_e$ method and RT method can be minimised by applying a correction factor, $C(\theta)$, as a function of the solar zenith angle. The correction factor, $C(\theta)$, was computed by fitting a quadratic equation to the plot of depth-integrated photolysis rate coefficient ratio, $q$ (Eq. 9), of each reaction as a function of solar zenith angle. The fitting is categorised into two types of snow – (1) wind pack and cold polar snow, and (2) melting and clean snow. Formulation of the correction factor, $C$, is shown in Eq. (10), and the coefficients ($a$, $b$, $c$) of the quadratic equation are listed in Tables 4 and 5 for “wind pack and cold polar” and “melting and clean” snow respectively. The depth-integrated photolysis rate coefficient approximated by the $z_e$ method at a particular solar zenith angle can then be corrected by multiplying by the correction factor, $C(\theta)$, at that particular solar zenith angle as shown in Eq. (11).

$$
C(\theta) = a \cos^2(\theta) + b \cos(\theta) + c,
$$

$$
v^\text{Corr}_{z_e}(\theta) = C(\theta)v_{z_e}(\theta),
$$

where $C(\theta)$ is the correction factor at a particular solar zenith angle; $a$, $b$, $c$ are the coefficient of the quadratic equation; $v_{z_e}$ is the depth-integrated photolysis rate coefficients approximated by the $z_e$ method; and $v^\text{Corr}_{z_e}$ is the corrected depth-integrated photolysis rate coefficient $v_{z_e}$.

For snowpacks with a large $e$-folding depth, i.e. > 30 cm – for example either having a small scattering cross section or containing a small amount of light-absorbing impurities – it is suggested to apply correction factors for “melting and clean snow” when solar zenith angles are smaller than 50° and larger than 80° to reduce the error by 10–30%. For snowpacks that have an $e$-folding depth smaller than 30 cm, the
within the snowpack would be exponential. Therefore, on the ground will be diffused and the decay of actinic flux will be non-exponential, than deeper into the snowpack, causing a potentially larger error estimating depth-integrated photolysis rate coefficients compared to the RT (radiative transfer) method. The deviation depends on the chemical species, solar zenith angle being small ($\theta < 37^\circ$); the chemical species of interest having an action spectrum peak near or in the visible wavelength, such as NO$_2$ and NO$_3$; (3) melting and clean snowpack correction factors should be applied when the solar zenith angles are small than 30$^\circ$ or between 60 and 70$^\circ$. This could reduce the error by up to 15%.

The correction was evaluated by comparing the depth-integrated photolysis rate coefficients computed by the RT method, $v_{\text{TUV}}$, to depth-integrated photolysis rate coefficient approximated by the $v_z$ method, $v_{z_e}$, and the corrected depth-integrated photolysis rate coefficient by the $v_{z_e}$ method, $v_{z_e}^{\text{Corr}}$, for all four species at 20 different solar zenith angles of snowpacks (Table 3) using wind pack and cold polar snowpack correction factors, and results are shown in Fig. 7. For evaluating the melting and clean snowpack correction factors, snowpack Scatt2 (Table 3) was used, and results are shown in Fig. 8. The corrections factors for the NO$_3$ photolysis rate coefficient were also tested against snowpacks HULIS1, HULIS8 and Comb (Table 3).

The correlation between $v_z$ and $v_{z_e}^{\text{Corr}}$ with $v_{\text{TUV}}$ is described by the square of correlation coefficients, $R^2$, listed in Tables 4 and 5. The $R^2$ is a measure of how well the data points fit a model. A value of 1 indicates a perfect fit, while a value of 0 indicates no correlation at all. The $R^2$ values are listed in Table 4 for different snowpacks (BaseC, HULIS8 and Comb) with and without applying the correction factors.

### Table 4. Parameterisation correction for “cold polar and coastal” snowpacks. Values of the correlation coefficient were calculated for two different snowpacks (BaseC, HULIS8 and Comb) with and without applying the correction factors.

<table>
<thead>
<tr>
<th>Species</th>
<th>$a$</th>
<th>$b$</th>
<th>$c$</th>
<th>BaseC $R^2$, $v_z$</th>
<th>BaseC $R^2$, $v_{z_e}$</th>
<th>BaseC $R^2$, $v_{z_e}^{\text{Corr}}$</th>
<th>HULIS8 $R^2$, $v_z$</th>
<th>HULIS8 $R^2$, $v_{z_e}$</th>
<th>HULIS8 $R^2$, $v_{z_e}^{\text{Corr}}$</th>
<th>Comb $R^2$, $v_z$</th>
<th>Comb $R^2$, $v_{z_e}$</th>
<th>Comb $R^2$, $v_{z_e}^{\text{Corr}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NO$_3^-$</td>
<td>0.452</td>
<td>-0.320</td>
<td>1.000</td>
<td>0.9788</td>
<td>0.9996</td>
<td>0.9886</td>
<td>0.9997</td>
<td>0.9468</td>
<td>0.9927</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>H$_2$O$_2$</td>
<td>0.485</td>
<td>-0.334</td>
<td>0.989</td>
<td>0.9758</td>
<td>0.9998</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NO$_2^-$</td>
<td>0.494</td>
<td>-0.345</td>
<td>0.980</td>
<td>0.9749</td>
<td>1.0000</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NO$_2$</td>
<td>0.758</td>
<td>-0.495</td>
<td>0.941</td>
<td>0.9435</td>
<td>0.9995</td>
<td></td>
<td></td>
<td></td>
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</tbody>
</table>

There are many factors that might have an impact on the disagreement between the two methods not taken into account in this study. Cloudy skies are not taken into account. However, clouds convert direct radiation into diffuse radiation. Under a very thickly clouded sky all radiation reaching the ground will be diffused and the decay of actinic flux within the snowpack would be exponential. Therefore, on a cloudy day the $z_e$ method would provide a very good approximation of actinic flux profile and photolysis rate coefficient within snowpack even without correction. Other assumptions have also been made on snowpack properties, i.e. assuming homogeneous single-layer snowpack, black carbon or HULIS as the only absorber other than ice and constant vertical chemical concentration profile. Geographic location and weather conditions may have a major influence on the number of layers within snowpack and the distribution of their physical and optical properties. Last, but not least, field observations on the Antarctic Plateau (Frey et al., 2009; France et al., 2011) show there is a much higher nitrate ion concentration in the top few centimetres of the snowpack, the region of the snowpack where the solar radiation attenuation is often non-exponential, than deeper into the snowpack, causing a potentially larger error estimating depth-integrated production rates from the $z_e$ method.

### 4 Conclusions

The parameterisation of snowpack actinic flux based on the $e$-folding depth – the $z_e$ method, which approximates the actinic flux profile by an exponential function – may lead to under/overestimation of depth-integrated photolysis rate coefficients compared to the RT (radiative transfer) method. The deviation depends on the chemical species, solar zenith angle and properties of the snowpack. The $z_e$ method is most likely to provide a poor estimation of depth-integrated photolysis rate under four conditions: (1) solar zenith angle or effective solar zenith angle being small ($\theta < 37^\circ$); (2) the chemical species of interest having an action spectrum peak near or in the visible wavelength, such as NO$_2$ and NO$_3$; (3) melting and clean snowpack correction factors not taken into account.
Table 5 lists the correction factors for depth-integrated photolysis rate coefficient of NO$_2^-$. These factors were applied to correct the measured values for both clean and heavily polluted snowpacks.

Figure 7. Depth-integrated photolysis rate coefficient at various solar zenith angle for different species within snowpack BaseC ($\rho = 0.4$ g cm$^{-3}$, [BC] = 4 ng (C) g$^{-1}$ and $\sigma_{\text{scatt}} = 25$ m$^2$ kg$^{-1}$).

Figure 8. Depth-integrated photolysis rate coefficient at various solar zenith angle for different species within snowpack Scat2 ($\rho = 0.4$ g cm$^{-3}$, [BC] = 4 ng (C) g$^{-1}$ and $\sigma_{\text{scatt}} = 2$ m$^2$ kg$^{-1}$).

The discrepancy between the $z_e$ and RT methods can be improved by applying the correction factors, $C(\theta)$, especially for melting and clean snowpack (i.e. snowpacks have an $e$-folding depth larger than $\sim 30$ cm), for which the ratio of depth-integrated photolysis rate coefficient between the two methods, $Q$, has reduced from 0.82–1.35 to 0.97–1.02 for photolysis of NO$_2$, from 0.88–1.28 to 0.99–1.02 for photolysis of the NO$_3^-$ anion, from 0.93–1.27 to 0.99–1.03 for photolysis of the NO$_2^-$ anion, and from 0.91–1.28 to 0.98–1.06 for H$_2$O$_2$. In the polar regions, solar zenith angles larger than 42.8° are the norm; the simple $z_e$ method provides an acceptable estimation (10–16% underestimation compared to radiative transfer model). However, if the site of interest is a tropical glacier, low-latitude, slope snowpack or have a small effective solar zenith angle ($\theta < 37^°$) and is moderately to heavily polluted (e.g. $e$-folding depth smaller than 30 cm), then correction factors, $C$, from Tables 4 should be applied to reduce error up to 15%. Correction factors, $C$, listed in Table 5 should be applied with a correction factor of 15%

or melting (e.g. $e$-folding depth larger than 31 cm) to reduce the difference by up to 30%.

The values of $e$-folding depth used in some of the previous modelling studies were broadly based on field measurements (Thomas et al., 2011; Simpson et al., 2002). Recently research groups have started to develop new algorithms to estimate optical properties of snowpack, such as grain size and mass ratio of pollutants, from satellite measurements (Zege et al., 2011; Malinka, 2014; Khokanovsky, 2015). These measurements and algorithms can be integrated into large-scale chemical transport models in the future to estimate $e$-folding depth and photolysis rate coefficient for wide inaccessible areas.

An important approximation of the $e$-folding depth ($z_e$) method is that snowpack is optically thick, i.e. assuming the snowpack is semi-infinite. For shallow snowpacks the exact RT method should be used. It is unlikely a robust simple parameterisation could be developed to correct the $z_e$ method for shallow snowpacks over a range of light-absorbing snowpack, solar zenith angles and underlying terrains for the thin snowpack, i.e. soil or sea ice. For shallow snowpacks (< 2–3 $e$-folding depths) the RT method is recommended.
### Table A1. Notation.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\sigma$</td>
<td>Absorption cross section of chemical species</td>
<td>cm$^2$ molecule$^{-1}$</td>
</tr>
<tr>
<td>$\sigma_{\text{ice}}$</td>
<td>Absorption cross section of ice</td>
<td>cm$^2$ kg$^{-1}$</td>
</tr>
<tr>
<td>$\mu_{\text{abs}}$</td>
<td>Absorption coefficient</td>
<td>m$^{-1}$</td>
</tr>
<tr>
<td>$\sigma^+$</td>
<td>Absorption cross section per mass of impurities</td>
<td>cm$^2$ kg$^{-1}$</td>
</tr>
<tr>
<td>$I$</td>
<td>Actinic flux</td>
<td>quanta cm$^{-2}$ s$^{-1}$ nm$^{-1}$</td>
</tr>
<tr>
<td>$z_e$</td>
<td>Asymptotic e-folding depth</td>
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<tr>
<td>$g$</td>
<td>Asymmetry factor</td>
<td>dimensionless</td>
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<td>$c$</td>
<td>Correction factor for depth-integrated photolysis rate coefficient</td>
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<tr>
<td>$\rho$</td>
<td>Density of snowpack</td>
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<tr>
<td>$\kappa_{\text{ext}}$</td>
<td>Extinction coefficient</td>
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<tr>
<td>$J$</td>
<td>Photolysis rate constant</td>
<td>s$^{-1}$</td>
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<tr>
<td>$F$</td>
<td>Photochemical production rate</td>
<td>$\mu$mol cm$^{-2}$ s$^{-1}$</td>
</tr>
<tr>
<td>$\Phi$</td>
<td>Quantum yield</td>
<td>dimensionless</td>
</tr>
<tr>
<td>$Q$</td>
<td>Quotient, ratio of depth-integrated photolysis rate coefficient</td>
<td>dimensionless</td>
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<tr>
<td>$r_{\text{scatt}}$</td>
<td>Scattering coefficient</td>
<td>m$^{-1}$</td>
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<tr>
<td>$\sigma_{\text{scatt}}$</td>
<td>Scattering cross section</td>
<td>m$^2$ kg$^{-1}$</td>
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<td>$\theta$</td>
<td>Solar zenith angle</td>
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<td>Total absorption cross section</td>
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<tr>
<td>$v$</td>
<td>depth-integrated photolysis rate coefficient</td>
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