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# A Graph Neural Networks-Based Learning Framework with Hyperbolic Embedding for Personalized Tag Recommendation

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**ABSTRACT** Learning high-quality representations of users, items, and tags from historical interactive data is crucial for personalized tag recommendation (PTR) systems. Currently, most personalized tag recommendation models are committed to learning representations from first-order interactions without considering the exploitation of high-order interactive relations, which can be beneficial for avoiding sub-optimal learning. Although several tag recommendation models equipped with graph neural networks (GNN) have been proposed to capture higher-order semantic relevance from raw data, they all carry out representation learning in Euclidean space, which can still easily result in sub-optimal learning due to embedding distortion. In order to further improve the quality of representation learning for PTR, the paper proposes a personalized tag recommendation model based on a lightweight GNN framework with hyperbolic embedding, namely GHPTR. GHPTR explicitly injects higher-order relevance into entity representation through the message propagation and aggregation mechanism of GNN and leverages hyperbolic embedding to alleviate the embedding distortion problem. Experimental results on real-world datasets have demonstrated the superiority of our model over its Euclidean counterparts and state-of-the-art baselines.

**INDEX TERMS** Tag recommendation, graph neural networks, hyperbolic geometry, representation learning, embedding.

#### I. INTRODUCATION

Social tagging gained popularization with the growth of social networking websites. These sites allow users to add terms or keywords, which are most known as tags, to images, videos, and other online items. Social tagging is an efficient tool for users to annotate and organize online items and a dependable aid for websites in delivering information services. It has become indispensable in numerous web platforms and applications. Meanwhile, many personalized tag recommendation (PTR) systems [1] have been developed with the popularity of social tagging. These systems aim to promote a virtuous circle of social tagging services and

facilitate users' tagging process by automatically suggesting lists of candidate tags for users to select.

Like the general recommender systems oriented to users' preferences, the personalized tag recommendation is usually modeled as a ranking problem, and learning-to-rank (L2R) techniques have been widely adopted to tackle it. The dominant paradigm for L2R-based personalized tag recommendation is learning to represent entities including users, items, and tags from their ternary interactions in a low-dimensional embedding space, then generating a ranked list of tags based on learned embeddings. Among such learning techniques, those [2]–[6] related to tensor factorization

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used to be the most competitive because the interactions of triples (user, item, tag) constitute the primary content of raw data, which can be represented as three-order tensors. However, most tensor factorization-based models are committed to learning shallow representations from direct (a.k.a firstorder) interactive relations, and the learned representations can not precisely characterize entities' properties for the lack of semantics. Furthermore, the ternary interactions derived from the social tagging system naturally constitute a tripartite graph [7]. From the perspective of graph learning, a considerable amount of semantic relevance lurks in the highorder connected paths of the graph. Such high-order semantic information is beneficial to recommendations for their ability to reveal the underlying properties of entities, e.g., users' potential preferences on tags.

To fully exploit high-order relevance in raw data, some studies [8] have introduced graph neural networks (GNN) [9]-[11] to the framework of tag recommendation. By utilizing the message propagation and aggregation mechanism of GNN, these models are qualified to encode the high-order semantic relevance into entities' representations, thereby improving the quality of tag recommendations. Despite the effectiveness of GNN-based tag recommendation models, their abilities to express the graph data are constantly hindered by Euclidean spaces. These models are dedicated to learning representations in Euclidean space because Euclidean space is in line with our intuition and easy to visualize, and more importantly, Euclidean space has complete and mature operators of vectors. In parallel, many graph data exhibit complex network structural properties [12], such as scalefree and power-law degree distribution. This includes the tripartite graph of historical tagging information [13]. Recent studies [14], [15] have revealed that Euclidean spaces are not the most meaningful geometric representation for complex networks. The power-law distribution of networks suggests that their overall structure is tree-like. In a tree, the number of nodes increases exponentially with the depth of the tree, while the volume of Euclidean spaces increases polynomially with distance from the origin point. This leads to a distortion problem when embedding a tripartite graph in Euclidean spaces, resulting in sub-optimal learning.

Hyperbolic space has emerged as a promising tool for modeling hierarchical or tree-like data in recent times [14]–[17]. Unlike Euclidean space, which has zero curvature, hyperbolic space is a non-Euclidean space with constant negative curvature. When a disk is embedded into a two-dimensional hyperbolic space with curvature c = -1, its  $(2\pi \sinh r)$  and area  $(2\pi(\cosh r - 1))$  grow exponentially with the radius r. On the other hand, in the two-dimensional Euclidean space, the corresponding circumference  $(2\pi r)$  grows linearly and area  $(\pi r^2)$  grows quadratically. This makes hyperbolic space akin to a continuous version of a tree, making it well-suited for embedding tripartite graphs with lower distortion than in the Euclidean space. Both GNN and hyperbolic embedding are universal learning algorithms. The universality of GNN lies in its message propagation mechanism, i.e., the aggregation of neighbor nodes, which is suitable for capturing the local structural properties of graphs. On the other hand, most graphs have global properties such as scale-free and power-law distribution. These properties cannot be directly reflected by GNN, but can be well presented by hyperbolic embedding.

With the expectation of further enhancing personalized tag recommendation, in this paper, we propose a graph neural networks-based learning framework with hyperbolic embedding for personalized tag recommendation, namely GHPTR, which utilizes GNN to exploit high-order semantic relevance among entities and employs hyperbolic embedding to alleviate the problem of embedding distortion. In the first phase, GHPTR leverages the GNN to capture the semantic relevances in high-order connected paths and encode them into nodes' representations. To be specific, we derive two bipartite graphs from the tripartite interactive graph, i.e., the user-tag graph and the item-tag graph. Then the proposed model represents every node by explicitly aggregating representations of its multi-hop neighbors on each graph. Moreover, we remove feature transformation and non-linear activation components of GNN to make the proposed model more lightweight. The second phase of GHPTR accounts for modeling the interactions between nodes via embedding them into hyperbolic space and calculating the hyperbolic distances between embeddings for the final prediction. We conduct experiments t on two real datasets to validate the effectiveness of the proposed model, and the experimental results have shown its superiority over state-of-the-art baselines.

Our major contributions can be summarized as follows:

- We introduce a GNN with a lightweight architecture to the framework of personalized tag recommendation, which can exploit the local properties of interactive tripartite graph and reduce computational consumption.
- We utilize hyperbolic embedding to improve the expressive ability of the proposed model, which can better accommodate the global properties of interactive data and alleviate the problem of embedding distortion.
- We conduct extensive experiments on two real-world datasets to verify the efficiency of the proposed model, and experimental results show that the proposed model can outperform the state-of-the-art baselines.

The rest of our work is summarized as follows. The related work is discussed in Section II. Section III presents the problem definition of the personalized tag recommendation and formalized description of hyperbolic space. In Section IV, we describe the details of our proposed model. We conduct experiments to show our modelars effectiveness in Section V, followed by conclusions and future works in in Section VI. This article has been accepted for publication in IEEE Access. This is the author's version which has not been fully edited and content may change prior to final publication. Citation information: DOI 10.1109/ACCESS.2023.3347249

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# **II. RELATED WORK**

This section briefly reviews the state-of-the-art related works, including personalized tag recommendation models, GNN-based recommendation models, and hyperbolic recommendation models.

## A. PERSONALIZED TAG RECOMMENDATION MODELS

Social tagging systems have become popular in various web applications, making personalized tag recommendation (PTR) an attractive issue in the research of recommender systems. The core of users' historical tagging information is the ternary interaction among entities, which includes user, item, and tag. This interaction can be represented by a three-order tensor. As a result, most early studies used tensor factorization techniques, such as the tucker decomposition (TD), to learn representations of involved entities in PTR tasks [2], [4], [5].

The TD model's computation cost becomes impractical for large-scale PTR tasks due to its model equation resulting in a cubic runtime in the factorization dimension. To overcome this challenge, Rendle et al. [4] introduced the pairwise interaction tensor factorization (PITF) model, which explicitly models the pairwise interactions between entities, resulting in linear runtime. PITF is widely recognized for its superior performance, and many learning methods derived from it have been proposed to tackle new problem scenarios. Recently, to leverage the end-to-end learning capability of deep neural networks (DNN), several learning frameworks based on DNN [6], [18], [19] have been developed to further improve the performance of traditional PTR models.

Note that all the above models are conducted in Euclidean spaces. As we mentioned before, their capabilities of learning the representations of tree-like data are restricted by the polynomial expansion property of Euclidean space. Meanwhile, these models have overlooked the semantic relevance hidden in high-order interactions, and the embeddings learned by them are only derived from first-order interactions.

# B. GNN-BASED RECOMMENDATION MODELS

Graph Neural Networks (GNN) [9], [10] are a class of deep learning methods designed to perform inference on data described by graphs. GNN can be directly applied to graphs and provide an easy way to do node-level, edge-level, and graph-level prediction tasks. Since the target of the recommender system can be viewed as the link-prediction task, many recommendation models [20]–[26] have adopted GNN to improve representation learning. Representative GNNbased recommendation methods include but are not limited to SR-GNN [27], NGCF [21], LightGCN [22], and GraphRec [23]. [27] proposed a session-based recommendation model using GNN, namely SR-GNN. SR-GNN converts session sequences to graphs and utilizes GNN to capture the inner patterns of items' transitions. The NGCF model [21] employs the graph convolution neural networks (GCN) to carry out message propagation and aggregation on the user-item interactive bipartite graph and fully explores the higher-order similarities between entities to achieve better collaborative filtering performance. [22] found that the two most common components of GCN, i.e., feature transformation and nonlinear activation, contribute little to collaborative filtering and increase the difficulty of training. Therefore they simplified the GCN to a lightweight version called LightGCN for item recommendation. LightGCN retains only the aggregation component, which is closely related to collaborative filtering, and only performs linear message propagation on the bipartite graph to learn the representation of users and items. [23] proposed a GNN-based framework, i.e., GraphRec, to coherently model different bipartite graphs and strengths of social relations for the social recommendation.

The above GNN-based recommendation models are designed to deal with bipartite graph information, aiming at the traditional item recommendation task. The representative application of GNN in the study of personalized tag recommendation is the GNN-PTR model proposed by [8], which decomposed the tripartite graph of tagging information into two bipartite graphs and leveraged GNN to perform representation learning. GNN-PTR has achieved optimal performance in experiments conducted on multiple real datasets. But in essence, GNN-PTR belongs to the recommendation models that operate in Euclidean space, so it still has limitations in fitting exponential and tree-like data.

# C. HYPERBOLIC RECOMMENDATION MODELS

Due to most interactive data between users and items exhibiting non-Euclidean properties, i.e., the power-law distribution and hierarchical structures, but classical recommendation models, such as Bayesian Personalized Ranking (BPR) [28], Collaborative Metric Learning (CML) [29], and Neural Collaborative Filtering (NCF) [30] are designed in Euclidean space, they may suffer from various degrees of embedding distortion. For this reason, some works [31], [32] make efforts to bridge the gap between hyperbolic space and recommender systems by modifying the matching functions of the recommendation models. The basic idea is to embed the representations of users and items into hyperbolic space, then use hyperbolic distance instead of the inner product or Euclidean distance and neural networks to compute the semantic similarity between user and item. Vinh et al. studied the connection between metric learning in hyperbolic space and collaborative filtering. They devised a new method named HyperML [32] for one-class collaborative filtering. Hyperbolic metric embedding (HME) model [31] is designed for next-poi recommendation. HME jointly captures sequential transition, user preference, category, and region information in a unified approach by learning embeddings in a shared hyperbolic space. Subsequently, several models [33]- **IEEE**Access

[36] enhanced by hyperbolic embedding have been proposed to better perform in traditional recommendation tasks or cope with new tasks. For example, [36] proposed HGCF to capture higher-order information in user-item interactions by incorporating multiple levels of neighborhood aggregation through a hyperbolic GCN module. To exploit mutual semantic relationships among users/items for collaborative filtering tasks, [35] introduced a neighbor construction strategy to build user and item semantic neighborhoods and developed a deep framework with hyperbolic geometry to integrate constructed neighborhoods into the recommendation. Regarding personalized tag recommendation, [37] proposed HPTR to learn the tagging information in hyperbolic space and utilize hyperbolic distance to model the entities' interactions.

HGCF and HPTR are the most relevant works for our model; the difference is that HGCF is suitable for the item recommendation task of binary interaction, and GHPTR is applicable to the personalized tag recommendation of ternary interaction. Moreover, HGCF is optimized by Riemann stochastic gradient descent, and GHPTR adopts the tangent space optimization. Although HPTR is a personalized tag recommendation model based on hyperbolic embedding, it is only a shallow model without considering the higher-order semantic relevance, and our proposed model makes up for this deficiency.

#### **III. PRELIMINARIES**

#### A. PROBLEM DEFINITION

The PTR system is different from item recommendation systems as it comprises three types of entities: users U, items I, and tags T. The historical interactions between these entities is represented as S which is a subset of  $U \times I \times T$ . An element  $(u, i, t) \in S$  indicates that the user u has annotated the item i with the tag t. From the ternary relation set S, personalized tag recommendation methods usually deduce a three-order tensor  $Y \in \mathbb{R}^{|U| \times |I| \times |T|}$ , whose element  $y_{u,i,t}$  is defined as follows:

$$y_{u,i,t} = \begin{cases} 1, & (u,i,t) \in S\\ 0, & otherwise, \end{cases}$$
(1)

where  $y_{u,i,t} = 1$  indicates a positive instance, and the remaining data are the mixture of negative instances and missing values. In addition, the tagging information for a certain user-item pair (u, i) is defined as  $\mathbf{y}_{u,i} = \{y_{u,i,t} | y_{u,i,t}, t \in T\}$ .

PTR aims to recommend a ranked list of tags to a certain user for annotating his target item. Usually, a matching function  $\hat{Y} : U \times I \times T \longrightarrow \mathbb{R}$  is employed to measure and predict users' preferences on tags w.r.t their target items. The entry  $\hat{y}_{u,i,t}$  of  $\hat{Y}$  indicates the degree to which a user u prefers to annotate the item i with the tag t. After predicting the score  $\hat{y}_{u,i,t}$  of all candidate tag t for a given user-item pair (u, i), the personalized tag recommender system generates a ranked list of Top-N tags according to the obtained scores. Formally, the ranked list of Top-N tags given to the user-item pair (u, i) is defined as follows:

$$Top(u, i, N) = \underset{t \in T}{\operatorname{argmax}} \widehat{y}_{u, i, t}, \qquad (2)$$

where N denotes the number of recommended tags.

#### **B. HYPERBOLIC SPACE**

Hyperbolic space is a smooth Riemannian manifold with constant negative curvature. Due to the exponential expansion rate of the volume, hyperbolic space is well-suited for embedding tree-like data that follows the power-law distribution. Since hyperbolic space is difficult to exhibit intuitively, it is always described by five isometric models [38], i.e., Lorentz (hyperboloid) model, Poincaré ball model, Poincaré half space model, Klein model, and hemisphere model, of which the Poincaré ball and the Lorentz are commonly used in representation learning tasks. Let  $\mathcal{B}^d = \{x \in \mathbb{R}^d \mid ||x|| < 1\}$  be the an open *d*-dimensional unit ball, where  $\| \cdot \|$  denotes the Euclidean norm. The Poincaré ball can be defined by the Riemannian manifold  $(\mathcal{B}^d, g_x^B)$ , where  $g_x^B = \left(\frac{2}{1-||x||^2}\right)^2 g^E$  is the Riemannian metric tensor, in which  $x \in \mathcal{B}^d$  and  $g^{\mathbb{R}} = \mathbf{I}$  denotes the Euclidean metric tensor. The distance between points  $x, y \in \mathcal{B}^d$  is given as:

$$d_B(\boldsymbol{x}, \boldsymbol{y}) = \operatorname{arcosh} \left( 1 + 2 \frac{\|\boldsymbol{x} - \boldsymbol{y}\|^2}{(1 - \|\boldsymbol{x}\|^2) (1 - \|\boldsymbol{y}\|^2)} \right) \quad (3)$$

The Lorentz model, the so-called hyperboloid model can be defined as Riemannian manifold  $(\mathcal{L}^d, g_x^{\mathcal{L}})$ , where  $\mathcal{L}^d = \{x \in \mathbb{R}^{d+1} : \langle x, x \rangle_{\mathcal{L}} = -1, x_0 > 0\}$ , in which  $\langle x, y \rangle_{\mathcal{L}} = -x_0 y_0 + \sum_{i=1}^d x_d y_d$  denotes the Lorentzian scalar product, and where  $g_x^{\mathcal{L}} = \text{diag}([-1, 1, \dots, 1])$ . Based on above definitions, the distance between two points on Lorentz is given as:

$$d_{\mathcal{L}}(\boldsymbol{x}, \boldsymbol{y}) = \operatorname{arcosh}\left(-\langle \boldsymbol{x}, \boldsymbol{y} \rangle_{\mathcal{L}}\right) \tag{4}$$

## IV. THE PROPOSED MODEL

In this section, we first elaborate the overall framework of our proposed model, followed by presenting each component in detail. Finally, we introduce the learning process of model parameters.

The overall framework of our proposed model is illustrated in Figure 1. The model consists of three layers: embedding layer, propagation layer and prediction layer. The function of the embedding layer is to get the initial representation of the nodes based on their ID; The propagation layer is responsible for aggregating the neighbors' representations by message propagation, so as to enrich the semantics of nodes' representations; After combining the higher-order representation of each entity, the prediction layer projects the combined representation to the hyperbolic space through





FIGURE 1: The framework of proposed model

the exponential mapping, and then matches the entity on the basis of the hyperbolic distance. Finally, the model predicts the user's preferred tags on the target item according to the matching degree (score).

#### A. EMBEDDING LAYER

In the embedding layer, we project all involved entities, i.e., users, items, and tags into a low-dimensional latent space according to their IDs. It should be noted that, to facilitate the optimization of the proposed model, the latent space here is not a hyperbolic space, but a tangent space of a hyperbolic space, which has the same flat property as a Euclidean space. The specific reasons are explained in Section IV-C. Specifically, a training instance of our model is a quadruple (u, i, t, t') where u denotes a user and i denotes an item. t corresponds to the the positive tag, which had been assigned to the item i by the user u, and t' represents the negative tag which had not interacted with u and i. First, we perform a lookup operation in the corresponding embedding matrices according to the entity's IDs, then obtain the embedding of user u, item i, positive tag t, and negative tag t'. Formally,

$$e_{u} = \mathbf{U}. \text{ onehot } (u), e_{i} = \mathbf{I}. \text{ onehot } (i),$$
  

$$e_{t}^{U} = \mathbf{T}^{U}. \text{ onehot } (t), e_{t'}^{U} = \mathbf{T}^{U}. \text{ onehot } (t'), \qquad (5)$$
  

$$e_{t}^{I} = \mathbf{T}^{I}. \text{ onehot } (t), e_{t'}^{I} = \mathbf{T}^{I}. \text{ onehot } (t')$$

where onehot(.) denotes the one-hot encoding operation.  $\mathbf{U} \in \mathbb{R}^{|U| \times d}, \mathbf{I} \in \mathbb{R}^{|I| \times d}, \mathbf{T}^U \in \mathbb{R}^{|T| \times d}, \mathbf{T}^I \in \mathbb{R}^{|T| \times d}(d$ is the embedding dimension) are the matrices of user embeddings, item embeddings, user-specific tag embeddings, and item-specific tag embeddings, respectively.

#### **B. PREDICTING LAYER**

The task of the predicting layer is to embed the nodes' representations encoded with higher-order relevance in hyperbolic space and model nodes' interactions via hyperbolic distance, and finally output the predicted score through a matching function. The specific process is as follows:

By stacking multiple propagation layers, we obtain the embedding sets of each entity. Every element in the set represents the semantic relevance of different-order neighbors, it is conducive to characterizing different properties of an entity, so we combine all corresponding elements into a single embedding. Formally,

$$e_{u}^{*} = \alpha_{1}e_{u}^{(1)} + \alpha_{2}e_{u}^{(2)} + \dots + \alpha_{l-1}e_{u}^{(l-1)} + \alpha_{l}e_{u}^{(l)}$$

$$e_{t}^{U*} = \alpha_{1}e_{t}^{U(1)} + \alpha_{2}e_{t}^{U(2)} + \dots + \alpha_{l-1}e_{t}^{U(l-1)} + \alpha_{l}e_{t}^{U(l)}$$

$$e_{i}^{*} = \alpha_{1}e_{i}^{(1)} + \alpha_{2}e_{i}^{(2)} + \dots + \alpha_{l-1}e_{i}^{(l-1)} + \alpha_{l}e_{i}^{(l)}$$

$$e_{t}^{I*} = \alpha_{1}e_{t}^{I(1)} + \alpha_{2}e_{t}^{I(2)} + \dots + \alpha_{l-1}e_{t}^{I(l-1)} + \alpha_{l}e_{t}^{I(l)}$$
(6)

where  $a_l$  denotes the weight of a embedding in the *l*-th layer. In order to simplify our model, we empirically set the  $a_l$  to  $\frac{1}{(L+1)}$ , where *L* is the total number of propagation layers.

Based on the obtained higher-order representations, we define a matching function with hyperbolic distance for the final prediction. Given a triplet (u, i, t), the matching function  $\hat{y}_{u,i,t}$  can be defined as:

$$\widehat{y}_{u,i,t} = p\left(d_H(e_u^*, e_t^{U*}) + d_H(e_i^*, e_t^{I*})\right)$$
(7)

where  $d_H(\cdot)$  denotes the hyperbolic distance function,  $p(\cdot)$  is the transformation function for converting hyperbolic distances to the matching degree, here we take it as  $p(x) = \beta x + c$  with  $\beta \in \mathbb{R}$  and  $c \in \mathbb{R}$ .

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Note that in order to adequately examine the influence of hyperbolic embedding on the performance of our proposed GHPTR model, we take Poincaré Ball and Lorentz as the geometric representation of hyperbolic space, and obtain two versions of the proposed model, called GHPTR(P) and GHPTR(L). Thus the hyperbolic distance  $d_H(\cdot)$  in this paper will be computed according to Equation 3 and Equation 4, respectively.

#### C. MODEL TRAINING

The construction idea of training dataset is inspired by the work [4]: When observing a certain pair (u, i) in historical interactions S, it can be inferred that the user u should prefer tag t over tag t' iff the triple (u, i, t) can be observed from S and (u, i, t') can not be observed. Based on this idea, the training set  $D_S$  (i.e., the set of quadruple (u, i, t, t')) with the pairwise constraint is defined as:

$$D_S = \{ (u, i, t, t') \mid (u, i, t) \in S \land (u, i, t') \notin S \}$$

$$(8)$$

The objective of model training is to maximize the gap between the matching scores  $\hat{y}_{u,i,t}$  of the positive triple (u, i, t) and negative triple (u, i, t'), so we adopt the Bayesian Personalized Ranking (BPR) optimization criterion [28] to learn model parameters  $\Theta = \{\mathbf{U}, \mathbf{I}, \mathbf{T}^{\mathbf{U}}, \mathbf{T}^{\mathbf{I}}, \beta, c\}$ , and build the objective function of proposed model as follows:

$$\mathcal{L} = \min_{\Theta} \sum_{(u,i,t,t') \in D_s} -\ln\sigma\left(\widehat{y}_{u,i,t} - \widehat{y}_{u,i,t'}\right) + \lambda_{\Theta} \|\Theta\|_F^2$$
(9)

As the Poincaré ball and Lorentz are both Riemannian manifolds with constant negative curvature, their related parameters need to be updated by Riemannian gradient, so the Riemannian stochastic gradient descent(RSGD) [39] has been widely adopted to optimize most of Hyperbolic embeddingbased models [14], [31]. However, RSGD is challenging in practice. Concerning our model, its parameters consist of {U, I, T} that require to be projected into hyperbolic space and { $\beta$ , c} that with no requirement for projection. To avoid using two corresponding optimizers, we update all the parameters via tangent space optimization [16], [17].

We recall that a *d*-dimensional hyperbolic space is a Riemannian manifold  $\mathcal{M}$  with a constant negative curvature -c(c > 0), the tangent space  $\mathcal{T}_x \mathcal{M}$  at point x on  $\mathcal{M}$  is a *d*-dimensional flat space that best approximates  $\mathcal{M}$  around x, and the elements  $\mathbf{v}$  of  $\mathcal{T}_x \mathcal{M}$  are referred to as tangent vectors. In our work, We define all the parameters in the tangent space so that we can update them via powerful Euclidean optimizers(e.g., Adam). When it comes to calculating the hyperbolic distance  $d_H$ , we use the exponential map  $\exp_x^{H^d}(\mathbf{v})$  to recover the corresponding parameters ( project  $\mathbf{v}$  of tangent space back to hyperbolic space). The exponential map related to the Poincaré ball is formulated as follows:

$$\exp_{\boldsymbol{x}}^{\mathcal{B}^{d}}(\mathbf{v}) = \boldsymbol{x} \oplus \left( \tanh\left(\frac{\lambda_{\boldsymbol{x}} \|\mathbf{v}\|}{2}\right) \frac{\mathbf{v}}{\|\mathbf{v}\|} \right) \qquad (10)$$

Where  $\oplus$  denotes the *Möbius* addition operator [40] that provides an analogue to Euclidean addition for hyperbolic space. Formally,

$$\boldsymbol{x} \oplus \boldsymbol{y} := \frac{\left(1 + 2\langle \boldsymbol{x}, \boldsymbol{y} \rangle + \|\boldsymbol{y}\|^2\right)\boldsymbol{x} + \left(1 - \|\boldsymbol{x}\|^2\right)\boldsymbol{y}}{1 + 2\langle \boldsymbol{x}, \boldsymbol{y} \rangle + \|\boldsymbol{x}\|^2\|\boldsymbol{y}\|^2} \quad (11)$$

The corresponding exponential map of Lorentz is given as:

$$\exp_{\boldsymbol{x}}^{\mathcal{L}^{d}}(\mathbf{v}) = \cosh\left(\|\mathbf{v}\|\right)\boldsymbol{x} + \sinh\left(\|\mathbf{v}\|\right)\frac{\mathbf{v}}{\|\mathbf{v}\|}$$
(12)

### **V. EXPERIMENTS AND ANALYSIS**

In this section, we first set up the experiments, and then present the performance comparison and result analysis.

#### A. EXPERIMENTAL SETUP

In our experiments, we choose two public available datasets , i.e., LastFM and ML10M, to evaluate the performance of all compared methods. Similar to [4], we preprocess each dataset to obtain their corresponding p-core, which is the largest subset where each user, item, and tag has to occur at least p times. In our experiments, every datasets is the result of 5-core or 10-core preprocessing. The general statistics of datasets are summarized in TABLE 1.

TABLE 1: Description of datasets.

Dataset	Users	Items	Tags	Tag assignments
LastFM-core5	1348	6927	2132	162047
LastFM-core10	966	3870	1024	133945
ML10M-core5	990	3247	2566	61688
ML10M-core10	469	1524	1017	37414

We adopt the leave-one-out protocol to evaluate the recommendation performance of all compared methods. Specifically, for each pair (u, i), we select the last triple (u, i, t)according to the timestamp and transfer it from S to  $S_{test}$ . The remaining observed triples constitute the training set  $S_{train} = S - S_{test}$ . Similar to the item recommendation problem, the PTR provides a top- N ranked list of tags for a given pair (u, i), so we employ two typical ranking metrics to measure the performance of all compared methods, i.e., Precision@N and Recall@N. Formally,

For both metrics, we set N = 3, 5, 10 in the experiments.

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# B. BASELINES AND PARAMETER SETTINGS

In order to evaluate the effectiveness of our proposed model, we choose the following personalized tag recommendation models as baselines:

- PITF: PITF [4] explicitly models the pairwise interactions among users, items and tags by inner product, it is a strong competitor in the field of personalized tag recommendation.
- NLTF [3] is a non-linear tensor factorization model, which enhances PITF by exploiting the Gaussian radial basis function to capture the nonlinear interactive relations among users, items and tags.
- ABNT: ABNT [6] utilizes the multi-layer perception to model nonlinear interactions between users, items, and tag, and employs attention networks to capture complex patterns of users' behaviors.
- HPTR: HPTR [37] learns the representations of entities by modeling their interactive relationships in hyperbolic space and utilizes hyperbolic distance to measure semantic relevance between entities.
- GNN-PTR: GNN-PTR [8] is a graph-neural-networks enhanced tag recommendation model, which introduce the GNN to the pairwise interaction tensor factorization framework for mining high-order similarity between embeddings.

We empirically set the parameters of baselines according to their corresponding literature in order to recover their optimal performance: the dimension of embedding dis set to 64, and the learning rate  $\eta$  is tuned amongst  $\{0.0001, 0.0005, 0.001, 0.005, 0.01, 0.05\}$ . For the ABNT model, the number of hidden layers is set to 2. All the parameters of HPTR and GHPTR are defined in tangent space  $\mathcal{T}_{x}\mathcal{M}$  located at origin point (x = 0) of hyperbolic space. The number of propagation layers is set to 3 for both GNN-PTR and GHPTR. We adopt Adam [41] as the optimizer for all involved models.

# C. PERFORMANCE COMPARISION

The experimental results of all comparison models on each dataset are presented in the following tables.

From TABLE 2 to TABLE 5, we have the following observations:

(1) Among the baselines not equipped with hyperbolic embeddings, the GNN-PTR is superior to other models for all evaluation metrics, which indicates that the neighborhood aggregation implemented by message propagation mechanisms is efficient for enhancing tag recommendation. The reason for the poor performance of the rest may be that they learn shallow representations from low-order interactions. Thus, the learned representations lack the semantics for approximating the user's tagging preference. (2) Although HPTR is a shallow representation learning model, it outperforms the GNN-PTR in most cases of our experiments, and the reason for this may be that HPTR desires to model better the global structural properties (e.g., scale-free or power-law) of the interactive tripartite, so it leverages hyperbolic embedding to alleviate the distortion problem. GNN-PTR focuses on the local properties of the graph. Therefore, it utilizes GNN to capture high-order relevance within the neighborhood. This result implies that using global properties is more effective than local properties in improving the performance of tag recommendations.

(3) GHPTR shows the best performance overall involved baselines. it surpasses Precision@10 of the best baselines by 8.6%, 12.5%, 12.7%, and 14.1% on Lastfm-core5, Lastfm-core10, ML10M-core5, and ML10M-core10, respectively. With respect to Recall@10, the improvements of GHPTR over best baselines are 5.7%, 5.0%, 11.1%, and 8.8% on the above four datasets. The main reason should be that we integrated GNN and hyperbolic geometry into the learning framework of personalized tag recommendation. In this way, the learned representations are endowed with the global and local structural properties of the raw data so that the proposed model is challenging to fall into sub-optimal learning, resulting in the enhancement of recommendation performance.

# D. EFFECT OF EMBEDDING DIMENSION



FIGURE 2: Effect of the parameter d for GHPTR

In our proposed model, the dimension of embeddings d is an essential parameter since it controls the expressive ability of the whole model, so we conduct additional experiments to study the sensitivity of d to the performance of our model by tuning it within {8, 16, 32, 64, 128, 256, 512, 1024}. Here we choose Precision@5 to give an insight into the impact on performance with respect to the parameter d, the experimen-

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Method	Precision@3	Precision@5	Precision@10	Recall@3	Recall@5	Recall@10
ABNT	0.1563	0.1353	0.1018	0.1569	0.2194	0.3298
NLTF	0.1949	0.1678	0.1191	0.2275	0.3239	0.4523
PITF	0.2127	0.1789	0.1274	0.2571	0.3479	0.4814
HPTR	0.2612	0.2229	0.1424	0.3597	0.4383	0.5191
GNN-PTR	0.2324	0.1913	0.1327	0.3244	0.4169	0.5454
GHPTR(P)	0.3030	0.2398	0.1546	0.3868	0.4770	0.5642
GHPTR(L)	0.3043	0.2390	0.1547	0.3914	0.4776	0.5673

#### TABLE 2: LastFM-5core

### TABLE 3: LastFM-10core

Method	Precision@3	Precision@5	Precision@10	Recall@3	Recall@5	Recall@10
ABNT	0.2041	0.1767	0.1342	0.1981	0.2592	0.3534
NLTF	0.2544	0.2163	0.1351	0.2945	0.4118	0.5142
PITF	0.2515	0.2087	0.1458	0.3204	0.4158	0.5654
HPTR	0.2861	0.2255	0.1574	0.3501	0.4714	0.5771
GNN-PTR	0.2646	0.2142	0.1461	0.3476	0.4529	0.5874
GHPTR(P)	0.3406	0.2657	0.1682	0.4311	0.5252	0.6170
GHPTR(L)	0.3382	0.2658	0.1772	0.4339	0.5267	0.6119

TABLE 4: ML10M-5core

Method	Precision@3	Precision@5	Precision@10	Recall@3	Recall@5	Recall@10
ABNT	0.1022	0.0829	0.0413	0.2391	0.2938	0.3444
PITF	0.1323 0.1497	0.1021	0.0597 0.0641	0.2974 0.3208	0.3561 0.3909	0.4312 0.4623
HPTR	0.1611	0.1106	0.0707	0.3616	0.4156	0.4766
GNN-PTR	0.1524	0.1055	0.0672	0.3331	0.3965	0.4851
GHPTR(P)	0.1904	0.1358	0.0788	0.4112	0.4703	0.5325
GHPTR(L)	0.1915	0.1375	0.0797	0.4158	0.4799	0.5391

TABLE 5: ML10M-10core

Method	Precision@3	Precision@5	Precision@10	Recall@3	Recall@5	Recall@10
ABNT	0.1183	0.0959	0.0601	0.2610	0.3714	0.4572
NLIF PITF	0.1635 0.1798	0.1142 0.1272	0.0729 0.0744	0.3388 0.3770	0.4334 0.4523	0.5340 0.5205
HPTR	0.2189	0.1483	0.0825	0.4969	0.5485	0.5960
GNN-PTR	0.1933	0.1390	0.0842	0.4602	0.5460	0.6398
GHPTR(P)	0.2507	0.1706	0.0957	0.5683	0.6294	0.6884
GHPTR(L)	0.2519	0.1726	0.0960	0.5713	0.6343	0.6898

tal results are plotted in FIGURE 2. From the content of the figure, we can have the following observations and findings:

(1) In the beginning, the values of Precision@5 increase stably with the growth of d. When d exceeds 128, most of the curves are no longer in an uptrend, which indicates that merely increasing the dimension is not conducive to sustained improvement of recommendation. The main reason may be similar to the Euclidean embedding: the learning model will obtain sufficient learning ability when d reaches a certain threshold. After that, continuously increasing the embedding dimension can also lead to overfitting problems.

(2) Compared with GHPTR (L), the curve of GHPTR (P) exhibits less smooth, such observation is consistent with previous studies [14], [17], The reason lies in the Equation 3 of Poincaré ball distance ,i.e.,  $d_{\mathcal{B}}(\boldsymbol{x}, \boldsymbol{y}) = \operatorname{arcosh}\left(1 + 2\frac{\|\boldsymbol{x}-\boldsymbol{y}\|^2}{(1-\|\boldsymbol{x}\|^2)(1-\|\boldsymbol{y}\|^2)}\right)$ , When the norm of  $\boldsymbol{x}$  or  $\boldsymbol{y}$ 

approaches 1, that is, when the embeddings are closer to the edge of the ball, the denominator of the equation rapidly approaches 0, resulting in instability of the calculation results.

### E. EFFECT OF PROPAGATION LAYERS

For the GHPTR model, the number of message propagation layers l is another important hyper-parameter, which controls the range of capturing the semantic relevance in the higherorder connected paths. In order to analyze the impact of l on the recommendation quality of our model, we conduct a set of extended experiments in this section. With Recall@5 as the indicator, we keep the same settings described in Section V-A and adjust the value of l in steps of 1 until l=3, reporting the result of Recall@5 obtained by the model for each l.

Figure 3 exhibits the performance of GHPTR under different l values on each dataset. As shown in the figure, This article has been accepted for publication in IEEE Access. This is the author's version which has not been fully edited and content may change prior to final publication. Citation information: DOI 10.1109/ACCESS.2023.3347249

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(b) ML10M-5core

FIGURE 3: Effect of the parameter l for GHPTR

for both model versions, their recommendation performance improves as the number of message propagation layers increases. When the number of propagation layers reaches 2 or 3, the model's performance on most datasets decreases. The reason is that excessive stacking of propagation layers will introduce the semantic information of long-range neighbors into the representation of the target node, and the semantic relevance between these neighbors and the target is relatively weak. Therefore they become useless or even noisy information that will be finally encoded into the representations, thus decreasing the performance of our proposed model.

#### F. ABLATION STUDY

The learning framework of our GHPTR contains two components: a lightweight GNN workflow and a hyperbolic matching process. To study the rationality of these two components, we remove them from the proposed model and obtain two corresponding variants, denoted as GHPTR-H and GHPTR-G. We conducted an extended set of experiments to observe the performance of GHPTR and its variants on ML10M-10core and LastFM-10core, taking Precision@10 as the evaluation metric and setting all involved hyper-parameters the same as GHPTR in Section V-A. In addition, considering the relative stability of the Lorentz model, we choose it as the geometric representation of the hyperbolic space in this section. The experimental results on different embedding dimension *d* ranging from 16 to 256 are plotted in FIGURE 4.

As shown in FIGURE 4, we can get the following observations and inferences:



FIGURE 4: Ablation study of GHPTR

(1) The performance curves of the variants are all lower than that of the original model, indicating that each component of the GHPTR significantly affects recommendation quality. On the other hand, the performance of GHPTR-H is inferior to that of GHPTR-G, revealing that hyperbolic embedding contributes more to recommended performance than GNN. More importantly, this result suggests that we should give priority to learning the global properties of interactive data when constructing personalized tag recommendation models.

(2) Both GHPTR and GHPTR-G outperform GHPTR-H at lower embedding dimensions. With the increase of embedding dimension, the performance improvement of these two models is not as significant as that of GHPTR-H. This observation is consistent with studies [16], [17], which indicates that the advantage of hyperbolic spaces is reflected in the lower embedding dimensions because its exponential expansion property can endow the embedded model with considerable expressiveness in the lower dimension. In contrast, Euclidean space requires larger embedding dimensions to obtain sufficient learning ability. Furthermore, when embedding dimensions reach a certain threshold, they all will fall into overfitting problems.

## **VI. CONCLUSION**

Existing hyperbolic embedding-based tag recommendation models only account for the macro properties of the data, overlooking the node-level properties. In comparison, GNNbased tag recommendation models are competent for exploiting the properties of nodes and their neighborhoods. In this work, in order to learn both global and local properties of historical interactions, we present a lightweight yet effective personalized tag recommendation model based on the integration of hyperbolic embedding and GNN. Through extensive experiments on two datasets, we are able to demonstrate the effectiveness of GHPTR over other baselines.

Although hyperbolic embedding is adept at representing treelike data, we should not neglect the advantages of Euclidean space. Compared with hyperbolic space, the vector operators of Euclidean space is more efficient, and the relative distance between point can be better distinguished via Euclidean metrics. Considering the advantages of hyperbolic and Euclidean

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spaces, our future work will construct contrasting views from these spaces and carry out graph contrastive learning [42] to obtain more semantics for promoting personalized tag recommendations.

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