## Exchange-field-enhancement of superconducting spin pumping

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A recent ferromagnetic resonance study [Jeon *et al.*, Nat. Mat. 17, 499 (2018)] has reported that spin pumping into a singlet superconductor (Nb) can be greatly enhanced over the normal state when the Nb is coupled to a large SOC spin sink such as Pt. This behaviour has been explained in terms of the generation of spinpolarized triplet supercurrents via spin-orbit coupling (SOC) at the Nb/Pt interface, acting in conjunction with a non-locally induced magnetic exchange field. Here we report the effect of adding a ferromagnet (Fe) to act as an internal source of an additional exchange field to the adjacent Pt spin sink. This dramatically enhances the spin pumping efficiency in the superconducting state compared with either Pt and Fe separately, demonstrating the critical role of the exchange field in generating superconducting spin currents in the Nb.

Spin-triplet Cooper pairs can carry a non-dissipative spin current and are an essential element for the emergent field of superconducting spintronics [1-3]. In the past decade, the generation of spin-polarized triplet pairs within ferromagnets via spin mixing and spin rotation processes at magnetically-inhomogeneous superconductor/ferromagnet (SC/FM) interfaces has been intensively studied [1-4] based on the Josephson effect in SC/FM/SC junctions [5] and the critical temperature  $T_c$  modulation in FM/SC/FM and SC/FM/FM' superconducting spin valves [6,7].

Recent theoretical works [8,9] have suggested spin-orbit coupling (SOC) in combination with a magnetic exchange field  $h_{ex}$  as an alternative mechanism to generate the spin-polarized triplet supercurrents even at a single magnetically-homogeneous SC/FM interface. Briefly, in the presence of  $h_{ex}$ , some of the spin-singlets forming the superconducting condensate of a conventional SC are converted into spin-zero triplets oriented along  $h_{ex}$ . If the SOC, originating either from bulk (Dresselhaus-type) or structure (Rashba-type) inversion asymmetry, could have the necessary orthogonality to  $h_{ex}$ , the spin-zero triplets rotate to form equal-spin triplets [8,9]. The overall conversion efficiency of spin-singlets to equal-spin triplets is then expected to scale with both the amplitude of  $h_{ex}$  and the SOC strength [8,9].

Recent experiments [10-12], have explored the potential role that SOC may play in generating the spin-triplet pair correlations in SC/FM proximity-coupled systems. In particular, our recent ferromagnetic resonance (FMR) study [10] showed that when strong SOC spin sinks (Ta, W, Pt) are added on either side of Nb/Ni<sub>80</sub>Fe<sub>20</sub>/Nb samples, spin

pumping [13,14] from the precessing  $Ni_{80}Fe_{20}$  into the Nb can be substantially larger deep in the superconducting state compared with the normal state. This is the opposite behaviour to what is expected for the spin-singlet superconductivity [15-17], and is attributed to the flow of spin angular momentum through the proximity-induced equalspin triplet states by SOC, either at the  $Ni_{80}Fe_{20}/Nb$  interface [8,9], or possibly at the Nb/Pt interface acting in combination with Landau Fermi-liquid effect [18].

To understand better the mechanisms contributing to enhanced spin pumping in the superconducting state have conducted а series of experiments we on Fe/Pt/Nb/Ni<sub>80</sub>Fe<sub>20</sub>/Nb/Pt/Fe structures. Here the ferromagnetic Fe layers serves as an internal source of  $h_{ex}$  to the neighbouring Pt spin sink [Fig. 1(a)], creating spontaneous spin splitting, which is known to extend to Pt thicknesses of several nanometres [19]. By comparison with FMR results on Pt/Nb/Ni<sub>80</sub>Fe<sub>20</sub>/Nb/Pt control structures without the Fe layers, approximately one order of magnitude enhancement is achieved for certain Pt thicknesses  $t_{Pt}$  but this enhancement disappears for large and small  $t_{Pt}$ , demonstrating the requirement for both SOC and the exchange field in generating substantial superconducting spin currents.

We measured the  $t_{Pt}$  dependence of the magnetization M [Fig. 1(b)] and the superconducting transition  $T_c$  [Fig. 1(c)] for the two series of samples, with and without the Fe layers. The total M is clearly enhanced by the addition of the Fe layers and it is independent of  $t_{Pt}$ , implying that no significant intermixing/interdiffusion occurs at the Pt/Fe interfaces in any of the samples studied. A noteworthy aspect as a function of  $t_{Pt}$  is found in the  $T_c$  curves:  $T_c$  is strongly suppressed by the presence of the Fe layers (about 2 K for  $t_{Pt} = 0$  nm) and the  $T_c$  difference becomes smaller as  $t_{Pt}$  increases. This proves that the added Fe layers affect the (singlet) superconducting properties of the Nb layer via the

inverse proximity effect, that is, the propagation of Fe-induced exchange (spin-)splitting transmitted through the Pt spacer layer to the Nb/Pt interface [20,21].

To investigate how the Fe-induced  $h_{ex}$  influences spin transport, we measured the temperature (T) evolution of the FMR spectra, for instance, the FMR linewidth  $(\mu_0 \Delta H)$ (directly linked to the Gilbert damping  $\alpha$  and a measure of the net spin current out of the Ni<sub>80</sub>Fe<sub>20</sub>) and the resonance field (associated with the saturation magnetization  $\mu_0 M_s$ ) [10,13,14]. Note that the zero-frequency line broadening  $\mu_0 \Delta H_0$  in our system has been found to be less than |0.5 mT|, which is negligible small for the high frequency regime  $(\geq 10 \text{ GHz})$  [10]. Figure 2(a) shows  $\mu_0 \Delta H$  versus the normalized temperature  $T/T_c$  for Pt/Nb/Ni<sub>80</sub>Fe<sub>20</sub>/Nb/Pt control structures with different  $t_{Pt}$ , taken at a fixed microwave frequency f = 20 GHz. We note that the role of the Pt layers in our system is twofold. One is to proximity-induce equal-spin triplet states in the Nb layers via SOC in combination with hex [8,9]; the other is to provide a dump for spin angular momentum emitted from the middle Ni<sub>80</sub>Fe<sub>20</sub> layer through the induced triplet states (of the Nb) – a consequence of the very short spin-flip length in Pt [13]. The resulting flow/transfer of spin angular momentum through proximity-induced (equal-spin) triplet states into singlet SCs, namely superconducting spin currents, can then be probed by FMR linewidth broadening or Gilbert damping increase of the middle Ni<sub>80</sub>Fe<sub>20</sub> [10, 13]. In the normal state  $(T/T_c > 1)$ ,  $\mu_0 \Delta H$  is almost T-independent for all  $t_{\rm Pt}$  but increases with increasing  $t_{\rm Pt}$  as the Pt becomes a more effective sink for spin current. Upon entering the superconducting state  $(T/T_c <$ 1), a significant  $t_{\text{Pt}}$ -dependent evolution of  $\mu_0 \Delta H(T/T_c)$  takes place: a gradual transition from the narrowing to the broadening of  $\mu_0 \Delta H$  with the increase of  $t_{\text{Pt}}$ . This is basically consistent with our previous findings [10], which can be explained by the enhanced spin transfer via induced (equal-spin) triplet states in the Nb via SOC [8,9,18] associated with

the presence of the Pt (5 nm) contrasting with the blocking of spin transport in the samples with small or zero  $t_{Pt}$  overwhelmed by the singlet superconductivity

For these Fe-absent control samples, the amplitude of the spin transfer in the superconducting state as measured by  $\mu_0\Delta H$  is positively correlated with  $t_{Pt}$ . As in the normal state, the effective Pt spin conductance which controls the amount of spin current outflowing [14] from the precessing Ni<sub>80</sub>Fe<sub>20</sub> diminishes with reducing  $t_{Pt}$ ; in addition, the interfacial Nb/Pt SOC which generates triplet spin supercurrents [10,18] should also quickly decrease as  $t_{Pt}$  goes to zero.

Figure 2(b) displays  $\mu_0 \Delta H(T/T_c)$  for Fe/Pt/Nb/Ni<sub>80</sub>Fe<sub>20</sub>/Nb/Pt/Fe structures with several  $t_{Pt}$ . In the normal state the behaviour is very similar to that of the control samples shown in Fig. 2(a), demonstrating that the addition of the Fe does not enhance the normal spin current. A distinctively different behaviour of  $\mu_0 \Delta H$  as a function of  $t_{Pt}$  appears in the superconducting state when the Fe layers are present – Fig. 2(b) shows that as  $t_{Pt}$ increases, the low *T* suppression of FMR damping for the zero  $t_{Pt}$  sample changes to a large damping enhancement at a thinner  $t_{Pt}$  with the largest enhancement at the intermediate  $t_{Pt}$  of 1.7 nm. This is followed by a slow decrease in damping with  $\mu_0 \Delta H$ enhancement for the thickest Pt layer (5 nm) similar to the sample without the Fe layers.

To characterize the specific difference in  $t_{Pt}$ -dependence between the two series of the samples with [Fig. 2(d)] and without [Fig. 2(c)] the Fe layers, we plotted  $\mu_0 \Delta H(t_{Pt})$ for different (constant) *T*, ranging from 80 to 2 K. For the normal state (*T*/*T*<sub>c</sub> > 1), regardless of the presence of the Fe,  $\mu_0 \Delta H$  increases in an exponential fashion as a function of  $t_{Pt}$ , as expected for diffusive spin transport with the increased Pt spin conductance [13,14]. This normal state behaviour can be quantified using the spin pumping theory [13,14]:

$$\alpha_{sp}(t_{SC,}t_{NM}) = 2 \cdot \left(\frac{g_L \mu_B g_r^{\uparrow\downarrow}}{4\pi M_S t_{FM}}\right) \cdot \left[1 + g_r^{\uparrow\downarrow} \mathcal{R}_{SC} \cdot \left(\frac{1 + g^* \mathcal{R}_{SC} \cdot \tanh\left(\frac{t_{SC}}{l_{Sd}^{SC}}\right)}{\tanh\left(\frac{t_{SC}}{l_{Sd}^{SC}}\right) + g^* \mathcal{R}_{SC}}\right)\right]^{-1};$$
$$g^*(t_{NM}) = g \cdot \left[1 + \frac{g \mathcal{R}_{NM}}{\tanh\left(\frac{t_{NM}}{l_{NM}^{NM}}\right)}\right]^{-1} (1)$$

where  $g_L$  is the Landé g-factor,  $\mu_B$  is the Bohr magneton, and  $\hbar$  is Plank's constant divided by  $2\pi$ .  $g_r^{\uparrow\downarrow}$  is the (effective) spin mixing conductance of the Ni<sub>80</sub>Fe<sub>20</sub>/Nb interface and g is the (effective) spin transfer conductance of the Nb/Pt interface (~35 nm<sup>-2</sup>) [13,22].  $\mathcal{R}_{SC(NM)} \equiv \rho_{SC} l_{sd}^{SC(NM)} e^2 / 2\pi\hbar$  is the spin resistance of the Nb (Pt) layer where  $\rho_{SC}$  is the resistivity of the Nb [10],  $l_{sd}^{SC(NM)}$  is the spin diffusion length of the Nb (Pt) and e is the electron charge.  $t_{FM}$  is the Ni<sub>80</sub>Fe<sub>20</sub> thickness and  $M_s$  is its saturation magnetization. Note that the prefactor 2 takes into account the spin pumping through double  $Ni_{80}Fe_{20}/Nb$  interfaces [13]. We assumed in Eq. (1) that the addition of a 2.5-nmthick Fe layers does not much affect the overall spin pumping effect since its spin conductance ( $< 3 \text{ nm}^{-2}$ ) is small relative to other layers [23] – direct evidence for this is the very similar FMR linewidths for the  $t_{Pt} = 0$  samples with and without Fe shown in Fig. 2. The similar values of  $g_r^{\uparrow\downarrow}$  (9–10 nm<sup>-2</sup>) and  $l_{sd}^{NM}$  (2–3 nm) are extracted from fitting Eq. (1) to the data of Figs. 2(c) and 2(d), implying comparable spin injection/transport properties of both samples in the normal state. The estimated  $l_{sd}^{NM}$  (2–3 nm) is consistent with that obtained from spin pumping and inverse spin Hall effect in FM metal/Cu/Pt structures where spin-memory loss at interfaces (i.e. interface spin-flip scattering) can be neglected [22,24].

However, for the superconducting state  $(T/T_c < 1)$ ,  $\mu_0 \Delta H(t_{Pt})$  is affected strongly by the presence of the Fe layers. From a comparison of Figs. 2(c) and 2(d), we can see that there is a clear rise in the  $\mu_0 \Delta H$  enhancement for the  $t_{Pt} = 1.7$  nm sample with the Fe layers. Note also that the superconducting state  $\mu_0 \Delta H(t_{Pt})$  deviates from the exponential fashion for both sample sets [Figs. 2(c) and 2(d)] and so it cannot be fitted by Eq. (1). All these results point to a fundamentally different spin transfer mechanism at play deep in the superconducting state when coupled to either Pt or Pt/Fe spin sink.

We show below that this unprecedented spin transfer phenomenon is consistent with a proximity-induced equal-spin triplet pairing generated by SOC [8,9,18] and enhanced by the Fe-induced exchange (spin-)splitting in the Pt.

A quantitative analysis of the effect of the Fe-induced  $h_{ex}$  on the superconducting spin transport is available in our present study by comparing the  $\mu_0\Delta H$  difference across  $T_c$ , defined as  $\Delta[\mu_0\Delta H] = \mu_0\Delta H(0.5 \cdot T_c) - \mu_0\Delta H(1.5 \cdot T_c)$ , with and without the Fe layers as a function of  $t_{Pt}$  [Fig. 3(a)]. In the absence of the Fe layers,  $\Delta[\mu_0\Delta H]$  monotonically rises with increasing  $t_{Pt}$  and shifts from negative (representing the blocking effect of dominant singlet superconductivity) to positive (indicating enhanced spin transport mediated by triplet pairing). However, when the Fe layers are present, this enhancement becomes more pronounced up to  $t_{Pt} = 1.7$  nm followed a fall to the almost same value for larger thicknesses.

There are several competing effects which lead to this maximum at intermediate thicknesses for the Fe-added samples. Firstly, the interfacial Nb/Pt/(Fe) SOC which appears to be required for triplet spin supercurrent generation [10] should vanish for both sample sets as  $t_{Pt}$  goes to zero – in this case there is no triplet pairing and the spin transport via singlet superconducting states should be lower than in the normal state – thus the  $t_{Pt}$  = 0 data is similar and negative for both sample sets. Secondly, because the spin conductance of the Fe layers is very small (relative to the Pt layers) [23], the overall Pt/(Fe) spin conductance should be reduced with decreasing  $t_{Pt}$  so that for small  $t_{Pt}$  even

if triplet pairs are generated, the absorption of superconducting spin currents by the Pt is inactive. Note that the net flow of spin angular momentum through the induced triplet states by SOC (which is what is measured by the FMR spectroscopy) predominantly depends on the effective Pt spin conductance which tends to increase until the Pt thickness becomes comparable to its spin diffusion length [13]. Finally, the exchange field at the Nb/Pt interface is known to increase rapidly with decreasing  $t_{Pt}$  in Pt/Fe [19] so that if singlet to triplet pair conversion is indeed further enhanced by the induced  $h_{ex}$ , this effect would decay with increasing  $t_{Pt}$ , and for large  $t_{Pt}$  one would expect the data from the two sample sets to become identical as is the case of for the  $t_{Pt} = 5$  nm samples.

Taking these effects together one can see that an intermediate maximum of superconducting spin current might be expected for the samples with Fe as the rapid increase in the induced  $h_{ex}$  and hence triplet pair density with decreasing  $t_{Pt}$  counteracts the reducing SOC and spin conductance associated with the Pt until the disappearance of the Pt removes the spin sink and SOC from the system at it reverts to singlet behaviour.

One can in principle isolate the contribution of the Fe-induced  $h_{ex}(t_{Pt})$  from the other effects of changing Pt thickness by normalizing the  $t_{Pt}$ -dependent enhancement of  $\Delta[\mu_0\Delta H]$  with the Fe layers (red symbol in Fig. 3) to that without the Fe layers (blue symbol) as follows:

$$\Delta[\mu_0 \Delta H(t_{Pt})]_{ex} = \frac{\{\Delta[\mu_0 \Delta H(t_{Pt})] - \Delta[\mu_0 \Delta H(t_{Pt} = 0)]\}^{w/Fe}}{\{\Delta[\mu_0 \Delta H(t_{Pt})] - \Delta[\mu_0 \Delta H(t_{Pt} = 0)]\}^{w/oFe}}.$$
 (2)

The inset of Fig. 3 shows that  $\Delta[\mu_0 \Delta H]_{ex}$  goes up rapidly with reducing  $t_{Pt}$ , reaching a factor of about 7.5 for 0.8 nm. Essentially, the same behaviour was observed in an analysis based on FMR damping  $\alpha$  [Fig. 3(b)], extracted from  $\mu_0 \Delta H(f)$  [10,13,14] (see Ref. [26] for full details).

We have shown that the spin angular momentum transfer into singlet SCs can be

further enhanced by one order of magnitude when spontaneous spin-splitting in the Pt spin sink is induced by the addition of FM layers. The understanding of SOC generation of superconducting spin currents is still evolving, but the latest theory [18, 27] highlights the need for an induced exchange field in the SOC material. For the Fe-absent samples as reported in our previous paper [10] this is indirectly applied by the spin accumulation at the Pt interface, transmitted by the triplet spin current itself, in combination with Landau Fermi liquid interactions. The key finding of this paper is that superconducting spin pumping can be dramatically enhanced by the influence of the direct exchange field of a coupled ferromagnetic layer on the properties of the Pt layer. This not only provides experimental support for the existing theory of triplet mediated transport [8,9,18], but provides a basis for the development of the comprehensive understanding and optimisation of superconducting spin transport.

This work was supported by EPSRC Programme Grant EP/N017242/1.

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[26] See Supplemental Material at [URL will be inserted by publisher] for a detailed analysis of MW frequency dependence of FMR spectra for the samples with and without the Fe layers at low temperatures, effect of the Fe thickness on overall FMR spectra of Fe/Pt/Nb/Ni<sub>80</sub>Fe<sub>20</sub>/Nb/Pt/Fe samples, and experimental details.

[27] In our theoretical work [18], the equilibrium spin currents have been calculated to demonstrate the long-range triplet correlations, but they are not to be equated with the pumped non-equilibrium spin currents. Although quantitative details and mathematical descriptions need to be fully set out, it is evident that with the presence of equilibrium equal-spin triplet pairs in the entire structure, a new channel is opened for spin currents to be transmitted through a singlet SC to Pt spin sink.

## Figures



FIG. magnetic 1. Structural, properties and induced exchange field in Fe/Pt/Nb/Ni<sub>80</sub>Fe<sub>20</sub>/Nb/Pt/Fe structures. (a) Schematic of the Fe(2.5 nm)/Pt( $t_{Pt}$ )/Nb(30 nm)/Ni<sub>80</sub>Fe<sub>20</sub>(6 nm)/Nb(30 nm)/Pt( $t_{Pt}$ )/Fe(2.5 nm) samples with different Pt thicknesses t<sub>Pt</sub> and a Cartensian coordinate system used in present study. (b) In-plane magnetization M curves of the two series of samples with and without the Fe layers. The inset summarizes the  $t_{\rm Pt}$  dependence of total M of the samples. (c) Normalized resistance  $R/R_{\rm N}$ vs. temperature T plots for the two series of samples with and without the Fe layers. The inset summarizes the  $t_{\rm Pt}$  dependence of the superconducting transition temperature  $T_{\rm c}$  of the samples; for comparison,  $T_c$  of a bare Nb(30 nm) film is also shown. Error bars denote standard deviation of multiple measurements.



FIG. 2. Characterization of exchange field effect on spin transport in the superconducting state. (a) Normalized temperature  $T/T_c$  dependence of the FMR linewidth  $\mu_0 \Delta H$  (top) and the resonance magnetic field  $\mu_0 H_{res}$  (bottom) for Pt( $t_{Pt}$ )/Nb(30 nm)/Ni<sub>80</sub>Fe<sub>20</sub>(6 nm)/Nb(30 nm)/Pt( $t_{Pt}$ ) control samples with various Pt thicknesses  $t_{Pt}$ . The dashed lines in the top panel are given as guides to the eyes. The inset shows the calculated superconducting energy gap  $2\Delta(t_{Pt})$  from the measured  $T_c(t_{Pt})$  [Fig. 1(c)] as a function of  $T/T_c$ . This provides information about how much the added Fe layers further suppress  $2\Delta(t_{\text{Pt}})$  via inverse proximity effect [20,21] in addition to the conventional (singlet) superconducting proximity effect. (b) Data equivalent to a but for  $Fe(2.5 \text{ nm})/Pt(t_{Pt})/Nb(30 \text{ nm})/Ni_{80}Fe_{20}(6 \text{ nm})/Pt(t_{Pt})/Nb(30 \text{ nm})/Ni_{80}Fe_{20}(6 \text{ nm})/Ni_$ nm)/Nb(30 nm)/Pt( $t_{Pt}$ )/Fe(2.5 nm) samples. c, FMR linewidth  $\mu_0 \Delta H$  as a function of  $t_{Pt}$ of the Pt/Nb/Ni<sub>80</sub>Fe<sub>20</sub>/Nb/Pt control samples at various T. The solid lines are fits to estimate the effective values of spin mixing conductance at the Ni<sub>80</sub>Fe<sub>20</sub>/Nb interface and spin diffusion length of the Pt using the spin pumping model [13,14]. The inset shows data and fits for the normal state. (d) Data equivalent to (c) now for the Fe/Pt/Nb/Ni<sub>80</sub>Fe<sub>20</sub>/Nb/Pt/Fe samples. Error bars denote standard deviation of multiple measurements.



FIG. 3. Exchange-field-enhanced spin transport in the superconducting state. (a) Pt thickness  $t_{\text{Pt}}$  dependence of the FMR linewidth  $\mu_0 \Delta H$  difference across  $T_c$ , defined as  $\Delta[\mu_0 \Delta H] = \mu_0 \Delta H(0.5 \cdot T_c) - \mu_0 \Delta H(1.5 \cdot T_c)$ , with and without the Fe layers. (b) Data equivalent to a now for the Gilbert damping  $\alpha$  [13,14]. The inset shows the estimated contribution of the Fe-induced exchange field  $h_{\text{ex}}$  to the spin transport, denoted as  $\Delta[\mu_0 \Delta H]_{\text{ex}}$  or  $\Delta[\alpha]_{\text{ex}}$ , as a function of  $t_{\text{Pt}}$ . Error bars denote standard deviation of multiple measurements.