LEARNING HORIZON AND OPTIMAL ALLIANCE FORMATION

Hans T. W. Frankort[♣]

John Hagedoorn[♣]

Wilko Letterie[♦]

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[♣] *Corresponding author*. City University London, Cass Business School, 106 Bunhill Row, London EC1Y 8TZ, United Kingdom, Tel: (+44)-20-7040-5202, hans.frankort.1@city.ac.uk

[♣] Royal Holloway University of London, School of Management, Egham, Surrey, TW20 0EX, United Kingdom, john.hagedoorn@rhul.ac.uk & UNU-MERIT, Maastricht University, Maastricht, The Netherlands

[♦] Maastricht University, School of Business and Economics, P.O. Box 616, 6200 MD Maastricht, The Netherlands, Tel: (+31)-43-3883645, w.letterie@maastrichtuniversity.nl

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ABSTRACT

We develop a theoretical Bayesian learning model to examine how a firm's *learning horizon*, defined as the maximum distance in a network of alliances across which the firm learns from other firms, conditions its optimal number of direct alliance partners under technological uncertainty. We compare theoretical optima for a 'close' learning horizon, where a firm learns only from direct alliance partners, and a 'distant' learning horizon, where a firm learns both from direct and indirect alliance partners. Our theory implies that in high tech industries, a distant learning horizon allows a firm to substitute indirect for direct partners, while in low tech industries indirect partners complement direct partners. Moreover, in high tech industries, optimal alliance formation is less sensitive to changes in structural model parameters when a firm's learning horizon is distant rather than close. Our contribution lies in offering a formal theory of the role of indirect partners in optimal alliance portfolio design that generates normative propositions amenable to future empirical refutation.

1. INTRODUCTION

Scholars have long noted that technological uncertainty, defined as the difficulty of accurately predicting the future state of the technological environment, motivates firms to enter into alliances with other firms (Auster 1992; Eisenhardt and Schoonhoven 1996; Hagedoorn 2002; Mody 1993; Rosenkopf and Schilling 2007; Steensma et al. 2000). Alliances are an important mechanism for reducing technological uncertainty because they allow firms to learn from their alliance partners about relevant developments in the technological environment (Frankort et al. 2012; Frankort 2013; Gomes-Casseres et al. 2006; Mowery et al. 1996; Oxley and Wada 2009; Powell et al. 1996). However, alliances are not equally effective as an uncertainty-reduction mechanism in all circumstances, while they also induce costs. Therefore, the optimal number of alliances represents a balance between the uncertainty-reduction benefits and costs of alliances, so that a firm has enough alliances to reduce uncertainty effectively, but not so many as for costs to outweigh their benefits (Faems et al. 2012). Convergent with the existence of such a balance, empirical evidence shows that learning-related outcomes tend to be greatest at intermediate alliance portfolio size (Deeds and Hill 1996; Frankort et al. 2012; Lahiri & Narayanan 2013; Rothaermel and Deeds 2006; Vanhaverbeke et al. 2012, 2014).

Nevertheless, even though empirical evidence on optimal alliance portfolio size resonates with a basic trade-off between the uncertainty-reduction benefits and costs of alliances, the underlying theory has overwhelmingly centered on firms' *direct* partners as sources of learning and uncertainty reduction. This somewhat narrow focus on direct partners appears at odds with findings suggesting that alliances may also serve as conduits through which firms learn from their *indirect* partners, i.e., the set of firms that direct partners have access to through their own alliances (Ahuja 2000; Salman and Saives 2005; Soh and Roberts 2005; Vanhaverbeke et al. 2012). To the extent firms have the potential to learn not just from direct but also indirect

partners, a fundamental question arises as to how learning from indirect partners affects the trade-off between the uncertainty-reduction benefits and costs of alliances. Answering this question is important because it is doubtful that the learning potential afforded by indirect partners is straightforwardly proportional to that afforded by direct partners. For example, firms vary greatly in their number of indirect partners for a given number of direct partners (e.g., Iyer et al. 2006)[1], while they may also differ in the extent to which they are aware of (e.g., Lhuillery and Pfister 2011) and benefit from (e.g., Boyd and Spekman 2008; Ghosh and Rosenkopf 2014) such indirect partners. Motivated by these observations, and following a call to begin to consider the role of indirect partners in optimal alliance portfolio design (Lavie 2006: 651), we complement the study of optimal alliance formation under technological uncertainty with a systematic theory of how learning from indirect partners shapes a firm's optimal alliance portfolio size. Our specific research question is this: *In the face of technological uncertainty, how does learning from indirect partners influence a firm's optimal number of direct partners?*

We take a formal approach to answering this question. In particular, we derive normative propositions regarding optimal alliance formation from a theoretical Bayesian learning model of how firms facing technological uncertainty form alliances and then use those alliances to learn and thereby reduce such uncertainty. In addition to being considered a leading formal device for modeling decision making under uncertainty (Cyert and DeGroot 1987), a Bayesian learning framework is particularly well suited to address our specific research question. First, the Bayesian approach accords central importance to the initial uncertainty surrounding key parameters, while

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[1] For example, in the pharmaceutical biotechnology industry during 1990-94, The Upjohn Company and Sepracor Inc. both had two direct partners, though these connected Upjohn to only two indirect partners while connecting Sepracor to well over twenty (Roijakkers and Hagedoorn 2006, p. 439). As another example, in the global semiconductor manufacturing industry during 1990-96, both Matsushita Electric Industrial Co. Ltd. and Motorola Inc. had one direct partner, but Matsushita had two indirect partners while Motorola had six (Kapoor and McGrath 2014, p. 564). These examples foreshadow that the learning potential afforded by firms' respective sets of direct and indirect partners may vary independently. It follows that the theory of optimal alliance formation must explicitly account for heterogeneity in the extent to which distinct sets of indirect partners allow for learning and uncertainty reduction.

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Bayesian updating subsequently allows actors to reduce such uncertainty through a mechanism of learning. This particular temporal sequence, in which actors respond to uncertainty by looking for learning opportunities that in turn help improve their beliefs about the uncertain parameter of interest, sits at the heart of the empirical phenomenon we are interested in modeling.

Second, a Bayesian learning framework allows us to model the effects of multiple parameters relevant to our research question in a tractable way. This is important because factors such as perceived technological uncertainty, the cost of unresolved uncertainty, the viability of interfirm learning, the cost of alliances, and awareness of indirect partners can vary greatly across firms and industries (e.g., Hagedoorn 2002; Harrigan 1985; Rosenkopf and Schilling 2007; Sutcliffe and Huber 1998), while all may individually as well as jointly shape the consequences of learning from indirect partners in perhaps unanticipated ways. A formal Bayesian learning framework, by requiring clear mathematical definitions of all relevant parameters and due to the rigor imposed by the Bayesian updating mechanism, allows us to generate an integrative and logically consistent account of any such effects (Adner et al. 2009).

In our Bayesian learning model, a firm begins with subjective beliefs about key features and trends characterizing an uncertain technological environment. The firm can update its beliefs by forming one or more alliances with other firms. The learning potential of the resulting set of alliances, and so the extent to which a firm can reduce technological uncertainty, is modeled as a function of the firm's *learning horizon*. We define a firm's learning horizon as the maximum distance in a firm's network of alliances across which that firm learns from other firms. We develop two canonical scenarios. In the first scenario, the firm learns only from its direct partners and so we label its learning horizon as 'close'. In the second, the firm learns both from its direct and indirect partners and so we label its learning horizon as 'distant' instead. In our model, more precisely, a firm has a distant learning horizon if it is both aware of one or more indirect partners

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and able to learn from such partners. A comparison of the optimal alliance formation decisions in these distinct scenarios subsequently supplies precise normative propositions on how learning from indirect partners influences optimal alliance formation under technological uncertainty.

Our formal assessment of the relationship between firms' learning horizon and optimal alliance formation under technological uncertainty offers several key results. First, we show that a firm's learning horizon has distinct implications for optimal alliance formation depending on its industry context (e.g., Ahuja 2000, pp. 450-451). Specifically, in industries where technological uncertainty is comparatively high, residual uncertainty is costly, and where alliances are a comparatively affordable and effective solution to technological uncertainty (which we label 'high tech industries'), firms with a distant learning horizon can substitute alliance ties to indirect partners for those with direct partners. In contrast, in industries where technological uncertainty is comparatively low, residual uncertainty is less costly, and where alliances are a comparatively costly and ineffective solution to technological uncertainty (which we label 'low tech industries'), alliance ties to direct and indirect partners act as complements.

Second, we show that given a distant learning horizon, the optimal number of direct partners of a firm in a high tech industry will be more robust to inter-temporal changes in the cost of residual technological uncertainty, the cost of alliances, and the perceived level of technological uncertainty. Through a Bayesian lens, therefore, the inter-temporal stability of a firm's alliance activities may be understood as the strategically optimal outcome of its efforts to reduce technological uncertainty. This novel insight complements prior alliance research, which has often discussed inter-temporal stability in firms' alliance activities through embeddedness and inertia mechanisms (e.g., Gulati and Gargiulo 1999; Hagedoorn 2006; Kim et al. 2006).

The paper is organized as follows: Section 2 introduces the basic setting and payoff structure in our model. Sections 3 and 4 develop expressions for optimal alliance formation under

close and distant learning horizons, respectively. Section 5 compares the respective optimal

decisions in equilibrium and derives our basic propositions. Section 6 generalizes the model to

account for heterogeneous alliance formation and incomplete awareness of indirect partners.

Section 7 discusses the findings and their implications.

2. THE BASIC MODEL

2.1 Setting

We consider a setting in which a firm performs research and development (R&D)

activities within an industry-level technological paradigm. A technological paradigm directs the

search efforts of firms towards an optimal future technology along a technological trajectory

(Breschi et al. 2000; Dosi 1982). A technological trajectory represents "…the activity of

technological process along the economic and technological trade-offs defined by a paradigm…"

(Dosi 1988, p. 1128). However, even though a technological paradigm produces some notion of

what paths of research to pursue and avoid, the superiority of one direction over another is likely

unclear a priori (Nelson and Winter 1982) and so a firm's expectations regarding an 'optimal'

technological trajectory are inevitably imprecise.

We represent the optimal technological trajectory by a parameter T. We assume that a

technological paradigm has one optimal technological trajectory T. An optimal trajectory is not

necessarily the one that is closest to the technological frontier or technologically superior

(Anderson and Tushman 1990; Arthur 1989; Liebowitz and Margolis 1995). Rather, it is the one

that among conceivable alternatives appears most promising "on the ground of some rather

obvious and broad criteria such as feasibility, marketability and profitability" (Dosi 1982, p. 155).

Our assumption of one optimal trajectory is consistent with a flurry of industry cases

documenting the eventual emergence of one comparatively dominant technology across settings

as diverse as cement, glass, and minicomputers (Anderson and Tushman 1990), automobiles,

electronic calculators, picture tubes, television, transistors, and typewriters (Suarez and Utterback 1995), as well as video tapes (Cusumano et al. 1992). Moreover, note that our assumption of one optimal technological trajectory does not preclude the contemporaneous existence of additional trajectories with some merit; all it requires is that at any one moment in time, prevailing technological, economic, and institutional constraints point to one technological trajectory that is on aggregate projected to be more feasible, marketable, and profitable.

Because the optimal technological trajectory depends on trade-offs along several technological, economic, and institutional dimensions and given that such trade-offs reflect a complex interplay between different actors (Dosi 1982; Garud et al. 1997), we assume that T is exogenous to the R&D activities of any one individual firm. If a firm had full information, it would make R&D investments consistent with the technological trajectory as given by T. In what follows, we refer to T as the optimal technology. We assume that each firm has incomplete knowledge about T, yet even though T is uncertain, a firm nevertheless has initial expectations about T based on available information (e.g., that accumulated through prior experience). We represent such initial expectations about the value of T by a prior probability distribution that is normal with mean μ and variance σ_T^2, such that $T \sim N(\mu, \sigma_T^2)$. This prior probability distribution expresses a firm's initial perceived technological uncertainty.

2.2 Payoffs

The technology ultimately implemented by a firm is represented by the decision parameter d. For a decision d, a firm's cost function is given by $C(T, d) = b'|T - d|$, where b' represents the cost a firm incurs when implementing a technology d that deviates from the optimal technology T by one unit and so $b' > 0$. This definition of b' allows for the possibility that a given deviation from T is not equally costly in all settings. For example, it is conceivable that in industries where technological progress is comparatively more important, b'—i.e., the marginal

cost of getting *d* wrong given *T*—is higher than in industries where technological progress is less important. Because of imperfect substitutability of R&D outcomes across different trajectories and due to strong path dependencies within them (Dosi 1982; Nelson and Winter 1982; Sahal 1981), in practical terms one might view $C(T, d)$ as capturing the opportunity cost of suboptimal R&D investment as well as the capital, effort, and time associated with adjusting to, and catching up with progress in, the optimal technological trajectory. The cost function shows that a firm incurs higher costs when the distance between *d* and *T* increases and so absent technological uncertainty, a firm would select $d = T$. However, complete certainty is improbable and so a firm will at best be able to reduce rather than eliminate uncertainty so as to pinpoint *T* with greater precision. Because knowledge about *T* is dispersed across firms within the industry, it is useful for firms to search for information to decrease technological uncertainty.

In our model, a firm can gather information about the properties of *T* by forming one or more alliances with other firms and we represent the number of alliances formed by a firm by η. We assume that each alliance yields one direct observation—i.e., one set of information about the optimal technology *T*. A firm begins with an initial belief represented by the prior probability distribution concerning *T*. Using the observations obtained from its alliances, the firm updates its prior probability distribution and forms a posterior belief—i.e., a posterior probability distribution concerning *T*—that incorporates the observations obtained through its alliances. This transformation or 'updating' of the prior belief concerning *T* into a posterior belief about that parameter is what makes our model Bayesian. In particular, the posterior distribution of the optimal technology *T* is obtained by deriving the distribution of *T* conditional on the prior belief of the firm *and* on the observations obtained from its alliances. Based on this posterior belief about *T*, a firm chooses $d = d^{opt}$ that minimizes the expected value of $C(T, d)$. Thus, d^{opt} is

determined through $\min_{d} \underset{T,\eta}{E} C(T,d)$, where E represents the expectations operator with respect to

T and the η below E denotes that a firm chooses d based on the posterior probability distribution

of T after obtaining observations through its η alliances.

The observations a firm obtains through its alliances are jointly normally distributed with

mean T and a covariance structure as will be given in Section 3, and the posterior probability

distribution of T is normal with mean μ_η and variance σ_η^2. The expression $\underset{T,\eta}{E} |T - d|$ is

minimized when d equals the median of the probability distribution of T. As T follows a normal

distribution, the median and mean are equal and so $\min_{d} \underset{T,\eta}{E} |T - d| = \underset{T,\eta}{E} |T - \mu_\eta| = \underset{T,\eta}{E} |Y|$, where

Y follows a normal distribution with mean zero and variance equal to σ_η^2. The expected value of

the absolute value of Y is equal to $\underset{T,\eta}{E} |Y| = \sqrt{\dfrac{2\sigma_\eta^2}{\pi}}$ (DeGroot 1970, pp. 232-233) and so it follows

that

(1) $\min_{d} \underset{T,\eta}{E} C(T,d) = b' \sqrt{\dfrac{2\sigma_\eta^2}{\pi}} = b \cdot \sigma_\eta,$

where σ_η is the standard deviation of a firm's posterior belief about T, reflecting a firm's

residual technological uncertainty after it obtains sets of information through its alliances, and the

parameter b collects all constant terms. Note that while σ_η plays a role in equation (1), μ_η does

not. Additionally, while a firm may reduce its technological uncertainty through its η alliances

with other firms, each individual alliance involves a cost c that captures the capital, effort, and

time necessary to form, operate, and terminate that alliance. For tractability, we begin by

interpreting the cost c as a parameter that is stable both across alliances as well as across firms.

However, this stability assumption can be relaxed without loss of generality and we take advantage of this possibility in Section 6, when generalizing our equilibrium results.

Consequently, the optimal number of alliances minimizes the total cost *TC*:

$$(2) \quad TC = \min_{\eta} \left(b \cdot \sigma_{\eta} + c \cdot \eta \right).$$

Thus, a firm's total cost is an increasing function of the posterior standard deviation σ_{η} and so a firm has an incentive to minimize residual technological uncertainty (Hagedoorn et al. 2011; Letterie et al. 2007). As we will show later, because an increase in the number of alliances decreases σ_{η}, the optimal number of alliances represents a resolution of the trade-off between the uncertainty-reduction benefits of alliances on the one hand, and their costs (i.e., $c \cdot \eta$) on the other hand.

3. OPTIMAL ALLIANCE FORMATION FOR A CLOSE LEARNING HORIZON

Consider the case where a firm's learning horizon is close and so it only learns through alliances with its own partners, but not through the alliances of its partners. The observation a firm receives through one alliance, which we represent by x_i, is normally distributed with mean *T* and variance σ_x^2. We assume that individual observations are independent, such that an observation x_i captures the non-redundant part of the information set obtained through one alliance. Thus, we assume that each alliance will yield at least some unique information as compared both with the firm's own knowledge and that accessed through its other alliances. This assumption is conceivable because individual firms tend not to have fully identical knowledge bases. It is also consistent with findings in empirical research showing that firms consider knowledge complementarity when selecting their alliance partners (Arora and Gambardella 1990; Mowery et al. 1998; Rothaermel and Boeker 2008). Note that this independence assumption is

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plausible, as each of a firm's partners must only hold *some* knowledge that is not held by the firm's other partners. Therefore, the independence assumption fully accommodates the possibility that the beliefs a firm's partners hold about the optimal technology T are partly redundant, for example in case such partners also have alliances with one another (Ahuja 2000). By implication, the observations x_1, x_2, ... , x_η that a firm obtains through its η alliances are jointly normally distributed with mean T and a covariance structure as given by a diagonal matrix Σ_x.

Each observation x_i provides a set of information about T but this information set will be imprecise to a greater or lesser extent (i.e., $\sigma_x^2 > 0$). First, due to the "permanent existence of asymmetries among firms, in terms of their…technologies" (Dosi 1988, p. 1155), information is scattered across industry firms and so no individual firm has full information about T. Second, to the extent that knowledge is tacit and embedded in routines and interactions within firms, its transmission across firm boundaries may be challenging (Kogut and Zander 1992). Third, to appropriate the returns to their knowledge, firms have a strategic reason to protect part of their knowledge about T from leakage to their alliance partners (Oxley and Wada 2009). While such strategizing may lead firms to be protective of their in-house knowledge, we assume that firms will not purposely mislead their alliance partners and so strategic motives may affect the variance of an observation but not the mean.

Consequently, after a firm has acquired observations x_1, x_2, ... , x_η through its η alliances, it will face a residual level of technological uncertainty as given by the posterior variance of T:

$$(3) \quad \sigma_\eta^2 = \left(\frac{\eta}{\sigma_x^2} + \frac{1}{\sigma_T^2} \right)^{-1} .$$

Derivation of this posterior variance is given in the Appendix. Equation (3) clearly shows that the Bayesian learning mechanism generates a posterior variance of T that is conditional on both the prior belief of the firm regarding T as well as the observations it obtains from its alliances.

Substituting equation (3) into (2) and solving for the optimal number of alliances η^* yields

(4) $\quad \eta^* = a \cdot \left(\sigma_x^2 \right)^{\frac{1}{3}} - \dfrac{\sigma_x^2}{\sigma_T^2}$,

where $a = \left(\dfrac{b}{2c} \right)^{\frac{2}{3}}$, to save some notation. The optimal number of alliances is a continuous

variable here but in practice a firm will choose an integer value close to η^* yielding the lowest

cost as implied by equation (2). Also, note that in our model, because firms choose the optimal

(in the Bayesian sense) number of alliances η^*, in equilibrium no firm will have an incentive to

deviate from this optimum.

Equation (4) provides a number of results. The optimal number of alliances increases with

the cost of uncertainty b, while it decreases with the cost of alliances c. Moreover, the optimal

number of alliances increases with a firm's perceived level of technological uncertainty σ_T^2.

Consequently, initial technological uncertainty represents an inducement for firms to enter into

alliances that will in turn increase firms' information about T, thus reducing their residual

technological uncertainty σ_η^2. Descriptive findings are consistent with this result. In dynamic

industry settings with high technological uncertainty, such as information technology or

pharmaceutical biotechnology, firms tend to engage in more alliances than in more stable

industry settings, such as food and beverages (Hagedoorn 2002). Equation (4) thus formally

captures the widely-established notion that technological uncertainty constitutes an important

motivation for firms to enter into alliances with other firms (Auster 1992; Hagedoorn 2002;

Mody 1993; Rosenkopf and Schilling 2007).

Finally, to see how the optimal number of alliances depends on the variance of an

observation σ_x^2, we obtain the first order derivative of η^* with respect to σ_x^2 as follows:

(5) $\dfrac{\partial \eta^*}{\partial \sigma_x^2} = \dfrac{a}{3}\left(\sigma_x^2\right)^{-\frac{2}{3}} - \dfrac{1}{\sigma_T^2} = \left(\dfrac{a}{3} - \dfrac{\left(\sigma_x^2\right)^{\frac{2}{3}}}{\sigma_T^2}\right)\left(\sigma_x^2\right)^{-\frac{2}{3}}.$

This derivative varies with the cost b of residual (i.e., posterior) technological uncertainty σ_η relative to the cost of alliances c, and the level of uncertainty σ_T^2 relative to the variance of an observation σ_x^2. Therefore, interpretation of the role of σ_x^2 in shaping η^* is conditional on two distinct industry scenarios that we define as follows[2]:

> A *high tech industry* is one in which (1) the cost b of residual technological uncertainty σ_η is *high* relative to the cost of alliances c, and (2) the initial technological uncertainty σ_T^2 is *high* relative to the variance of an observation σ_x^2.

> A *low tech industry* is one in which (1) the cost b of residual technological uncertainty σ_η is *low* relative to the cost of alliances c, and (2) the initial technological uncertainty σ_T^2 is *low* relative to the variance of an observation σ_x^2.

In a high tech industry, the first order derivative in equation (5) is positive and so a firm will form more alliances when the variance of observations becomes greater. As the incentive to learn through alliances in this setting is strong (loosely, $b > c$ and $\sigma_T^2 > \sigma_x^2$), greater variance of observations induces a firm to establish more alliances. For a low tech industry, the first order derivative in equation (5) is negative and so a firm will form fewer alliances when the variance of observations increases. In this setting, the incentive to learn through alliances is weak (loosely, b

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[2] Our labeling of these two scenarios as 'high tech industry' and 'low tech industry' reflects the close consistency between empirically observed high tech and low tech industries and our theoretical definitions of both. For example, compared to low tech industries, the R&D intensities of high tech industries are much higher (Dyer et al. 2014), while the marginal impact of firms' technology stocks on their value added and market valuations is also higher in high tech industries, such as pharmaceutical biotechnology (e.g., Cuneo and Mairesse 1984; Hall et al. 2005). This suggests that the level of technological uncertainty as well as the cost of residual technological uncertainty is much higher in high tech compared to low tech industries, thus outweighing the costs and learning imperfections of alliances, as reflected in high tech firms' greater propensity to engage in alliances with other firms (Hagedoorn 2002).

$< c$ and $\sigma_T^2 < \sigma_x^2$) and so greater variance of observations reduces a firm's inducement to establish more alliances. Therefore, in high tech industries, where technological uncertainty is severe and expensive, and where alliances are a comparatively affordable and effective solution to such uncertainty, a firm will form more alliances when the variance of observations increases. Conversely, in low tech industries, where technological uncertainty is limited and less expensive, and where alliances are a comparatively expensive and ineffective solution to such uncertainty, a firm will form fewer alliances when the variance of observations increases.

4. OPTIMAL ALLIANCE FORMATION FOR A DISTANT LEARNING HORIZON

Now consider the case where a firm's learning horizon is distant and so it learns both through alliances with its own partners as well as through indirect partners, defined as the set of firms that direct partners have access to through their own alliances. Let each alliance partner have ω alliance partners itself. Because the focal firm is included in ω, we must subtract one from ω to obtain the number of indirect partners provided by a direct partner. Therefore, each of a firm's direct partners yields $\omega - 1$ indirect partners and so η direct alliances yield $\eta \cdot (\omega - 1)$ indirect observations. We assume that individual observations obtained through indirect partners, represented here by x_j, are independent and so each indirect partner will yield at least some unique information compared to the firm's own knowledge base, the knowledge bases of its direct alliance partners, and the knowledge bases of its other indirect partners.

For the reasons as outlined in the previous Section, the set of information about the optimal technology T captured through an observation x_j will be imprecise. Because an increase in distance between firms makes the movement of knowledge more challenging (Burt 2010), we assume that a firm's indirect partners yield more variable observations about T than its direct partners. Specifically, in our model a firm observes $y_j = x_j + \upsilon_j$, where the stochastic term υ_j is

normally distributed with mean zero and variance σ_υ^2, the latter which represents the additional

transmission noise surrounding an indirect observation compared to an observation drawn from a

direct partner. While an indirect observation also has a mean T, its variance is $\sigma_x^2 + \sigma_\upsilon^2$ and so

the uncertainty-reduction potential of one indirect observation is smaller than that of one direct

observation because $\sigma_x^2 + \sigma_\upsilon^2 > \sigma_x^2$.

With a distant learning horizon, after acquiring η direct and $\eta \cdot (\omega - 1)$ indirect

observations, a firm faces a residual level of technological uncertainty as given by the posterior

variance of T:

$$(6) \quad \sigma_\eta^2 = \left(\frac{\eta}{\sigma_x^2} + \frac{\eta \cdot (\omega - 1)}{\sigma_x^2 + \sigma_\upsilon^2} + \frac{1}{\sigma_T^2} \right)^{-1} = \left(\frac{\eta}{\sigma_x^2} \cdot \frac{\left(\sigma_\upsilon^2 + \omega \sigma_x^2 \right)}{\left(\sigma_x^2 + \sigma_\upsilon^2 \right)} + \frac{1}{\sigma_T^2} \right)^{-1}.$$

Note that the expression in equation (6) bears analogy to equation (3), except that it additionally

accounts for the uncertainty-reduction potential of $\eta \cdot (\omega - 1)$ indirect partners. In equation (3),

which gives the posterior variance of T for a close learning horizon, each observation obtained

from one direct partner has a variance equal to $\left(\dfrac{1}{\sigma_x^2} \right)^{-1} = \sigma_x^2$. In equation (6), which instead gives

the posterior variance of T for a distant learning horizon, each observation obtained from one

direct partner has a variance that is in the aggregate equal to

$$f(\omega) = \left(\frac{1}{\sigma_x^2} \cdot \frac{\left(\sigma_\upsilon^2 + \omega \sigma_x^2 \right)}{\left(\sigma_x^2 + \sigma_\upsilon^2 \right)} \right)^{-1} = \sigma_x^2 \cdot \frac{\sigma_x^2 + \sigma_\upsilon^2}{\sigma_\upsilon^2 + \omega \sigma_x^2} < \sigma_x^2.$$ Consequently, though indirect observations

themselves have greater transmission noise than direct observations, the overall variance of the

combined information sets obtained through one of a firm's direct partners is smaller for a distant

compared to a close learning horizon. Substituting equation (6) into (2) and solving for the

optimal number of alliances η^{**} yields

$$(7) \quad \eta^{**} = a \cdot \left(\sigma_x^2 \frac{\left(\sigma_x^2 + \sigma_\upsilon^2 \right)}{\left(\sigma_\upsilon^2 + \omega \sigma_x^2 \right)} \right)^{\!\!1/3} - \frac{\sigma_x^2}{\sigma_T^2} \frac{\left(\sigma_x^2 + \sigma_\upsilon^2 \right)}{\left(\sigma_\upsilon^2 + \omega \sigma_x^2 \right)}.$$

Here, too, observe the analogy to equation (4) for a close learning horizon. Assuming for the

moment that all firms are identical in their alliance formation strategies, we can impose the

symmetry condition $\omega = \eta$ to obtain a Nash equilibrium as follows:

$$(8) \quad \eta^{**} = a \cdot \left(\sigma_x^2 \frac{\left(\sigma_x^2 + \sigma_\upsilon^2 \right)}{\left(\sigma_\upsilon^2 + \eta^{**} \sigma_x^2 \right)} \right)^{\!\!1/3} - \frac{\sigma_x^2}{\sigma_T^2} \frac{\left(\sigma_x^2 + \sigma_\upsilon^2 \right)}{\left(\sigma_\upsilon^2 + \eta^{**} \sigma_x^2 \right)}.$$

In our theoretical model this is a likely outcome because to this point, we have assumed that the

payoffs and costs of alliance formation are symmetric. After we compare equilibria for close and

distant learning horizons, we relax this symmetry condition in Section 6 in order to generalize our

equilibrium results. A solution for equation (8) is not tractable but the expression nevertheless

has properties directly relevant to our decision problem. For instance, an increase in the

transmission noise σ_υ^2 generates:

$$(9) \quad \lim_{\sigma_\upsilon^2 \to \infty} \eta^{**} = \lim_{\sigma_\upsilon^2 \to \infty} a \cdot \left(\sigma_x^2 \frac{\left(\sigma_x^2 + \sigma_\upsilon^2 \right)}{\left(\sigma_\upsilon^2 + \eta^{**} \sigma_x^2 \right)} \right)^{\!\!1/3} - \frac{\sigma_x^2}{\sigma_T^2} \frac{\left(\sigma_x^2 + \sigma_\upsilon^2 \right)}{\left(\sigma_\upsilon^2 + \eta^{**} \sigma_x^2 \right)} = a \cdot \left(\sigma_x^2 \right)^{1/3} - \frac{\sigma_x^2}{\sigma_T^2} = \eta^*.$$

Thus, for a distant learning horizon, if the variability of observations drawn from indirect partners

increases, then a firm's uncertainty reduction progressively becomes a function of localized

learning from direct partners alone. In that case, η^{**} asymptotically converges to η^*. The

transmission noise σ_υ^2 captures the inverse of a firm's ability to learn from indirect partners and

so the intuition of equation (9) is that despite the presence of indirect partners, a firm nevertheless

has a close learning horizon if it is unable to learn from indirect partners.

Next, to see how the optimal number of alliances given a distant learning horizon varies

with the main parameters of the model, we restrict our attention to a *high tech industry* because in

a low tech industry, equilibrium outcomes for several partial derivatives are indefinite. First note

that in a high tech industry $f(\eta^{**}) = \sigma_x^2 \cdot \dfrac{(\sigma_x^2 + \sigma_\upsilon^2)}{(\sigma_\upsilon^2 + \eta^{**}\sigma_x^2)} < \sigma_x^2$; $\dfrac{\partial f(\eta^{**})}{\partial \eta^{**}} < 0$; $0 < \dfrac{\partial f(\eta^{**})}{\partial \sigma_x^2} < 1$;

$\dfrac{\partial f(\eta^{**})}{\partial \sigma_\upsilon^2} > 0$; and $\left(\dfrac{a}{3} f(\eta^{**})^{-\frac{2}{3}} - \dfrac{1}{\sigma_T^2}\right) > 0$. Furthermore,

(10) $\quad \dfrac{\partial \eta^{**}}{\partial a} = \dfrac{\left(f(\eta^{**})\right)^{\frac{1}{3}}}{1 - \dfrac{\partial f(\eta^{**})}{\partial \eta^{**}}\left(\dfrac{a}{3} f(\eta^{**})^{-\frac{2}{3}} - \dfrac{1}{\sigma_T^2}\right)} > 0$.

Recall that $a = \left(\dfrac{b}{2c}\right)^{\frac{2}{3}}$ and so the optimal number of alliances increases with the cost of residual

technological uncertainty b, while it decreases with the cost of alliances c, as in the case of a

close learning horizon (see equation (4)). Also, the first order derivative of η^{**} with respect to a

firm's perceived level of technological uncertainty σ_T^2 is

(11) $\quad \dfrac{\partial \eta^{**}}{\partial \sigma_T^2} = \dfrac{f(\eta^{**})\big/\sigma_T^4}{1 - \dfrac{\partial f(\eta^{**})}{\partial \eta^{**}}\left(\dfrac{a}{3} f(\eta^{**})^{-\frac{2}{3}} - \dfrac{1}{\sigma_T^2}\right)} > 0$.

Therefore, a firm's optimal number of direct partners increases if the firm perceives greater

technological uncertainty. Next,

(12) $\quad \dfrac{\partial \eta^{**}}{\partial \sigma_\upsilon^2} = \dfrac{\dfrac{\partial f(\eta^{**})}{\partial \sigma_\upsilon^2}\left(\dfrac{a}{3} f(\eta^{**})^{-\frac{2}{3}} - \dfrac{1}{\sigma_T^2}\right)}{1 - \dfrac{\partial f(\eta^{**})}{\partial \eta^{**}}\left(\dfrac{a}{3} f(\eta^{**})^{-\frac{2}{3}} - \dfrac{1}{\sigma_T^2}\right)} > 0$

and so if the additional transmission noise surrounding an observation from an indirect partner

becomes greater, then the number of direct partners increases to compensate for such additional

variance. Similarly, note that

$$(13) \quad \frac{\partial \eta^{**}}{\partial \sigma_x^2} = \frac{\dfrac{\partial f(\eta^{**})}{\partial \sigma_x^2}\left(\dfrac{a}{3} f(\eta^{**})^{-\frac{2}{3}} - \dfrac{1}{\sigma_T^2}\right)}{1 - \dfrac{\partial f(\eta^{**})}{\partial \eta^{**}}\left(\dfrac{a}{3} f(\eta^{**})^{-\frac{2}{3}} - \dfrac{1}{\sigma_T^2}\right)} > 0$$

and so the number of direct partners increases when the variability of observations obtained through a firm's direct partners increases.

5. COMPARING EQUILIBRIA

Having developed the Bayesian analysis for both close and distant learning horizons, we now turn to a comparison of η^* and η^{**}, the respective optimal decisions for the two scenarios. We begin with two key insights from the prior Sections. First, equilibrium outcomes respond differently to increases in information variability depending on the context because $\frac{\partial \eta^*}{\partial \sigma_x^2} > 0$ in a high tech industry whereas $\frac{\partial \eta^*}{\partial \sigma_x^2} < 0$ in a low tech industry. Second, for a distant learning horizon each observation through a direct partner has a variance that is, in the aggregate, equal to

$f(\eta^{**}) = \sigma_x^2 \cdot \dfrac{(\sigma_x^2 + \sigma_v^2)}{(\sigma_v^2 + \eta^{**} \sigma_x^2)} < \sigma_x^2$ and so the overall variability of information a firm obtains through its alliances is smaller for a distant rather than a close learning horizon.

A change from a close to a distant learning horizon can be viewed as an aggregate decrease in information variability. By Sections 3 and 4, this has opposing implications in high versus low tech industries. Specifically, in a high tech industry $\frac{\partial \eta^*}{\partial \sigma_x^2} > 0$ and so a firm will form fewer alliances if the variability of observations decreases. By this result, and because

$f(\eta^{**}) = \sigma_x^2 \cdot \dfrac{(\sigma_x^2 + \sigma_v^2)}{(\sigma_v^2 + \eta^{**} \sigma_x^2)} < \sigma_x^2$, a static comparison of η^* and η^{**} (equations (4) and (8))

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generates a smaller optimum for a distant compared to a close learning horizon, i.e., $\eta^* > \eta^{**}$.

This generates the following proposition:

> **Proposition 1.** *In a high tech industry, a firm's optimal number of alliances is smaller when it has a distant rather than a close learning horizon.*

Thus, in a high tech industry, a firm with a distant learning horizon can *substitute* alliance ties to indirect partners for those with direct partners. Conversely, if the learning horizon is close—i.e., a firm has no indirect partners or it does have, but cannot learn from, such partners—then a firm's optimal number of alliances becomes greater.

In a low tech industry $\dfrac{\partial \eta^*}{\partial \sigma_x^2} < 0$ and so a firm will form more alliances if the information

variability of observations decreases. By this result, and because $f\left(\eta^{**}\right) = \sigma_x^2 \cdot \dfrac{\left(\sigma_x^2 + \sigma_\upsilon^2\right)}{\left(\sigma_\upsilon^2 + \eta^{**}\sigma_x^2\right)} < \sigma_x^2$,

a static comparison of η^* and η^{**} (equations (4) and (8)) generates a larger optimum for a

distant compared to a close learning horizon, i.e., $\eta^* < \eta^{**}$. This generates the following

proposition:

> **Proposition 2.** *In a low tech industry, a firm's optimal number of alliances is greater when it has a distant rather than a close learning horizon.*

Thus, in a low tech industry, a distant learning horizon instead generates *complementarity* between a firm's alliance ties to direct and indirect partners: a firm that learns both from direct and indirect partners will benefit more from a larger number of direct partners.

One key insight following directly from our analysis is that though a firm's learning horizon does have an impact on optimal alliance formation, the nature of this association depends

on characteristics of the industry context within which the firm is embedded (here, whether the industry is low tech or high tech). Together, propositions 1 and 2 reinforce Ahuja's (2000, pp. 450-451) suggestion that the nature of the interaction between ties to direct and indirect partners "… can only be understood relative to a particular context…"

Though propositions 1 and 2 represent static implications of the Bayesian learning model, the analysis also has dynamic implications for firms in a high tech industry. Suppose a firm optimizes its number of alliances every period as a consequence of period-by-period changes in the structural parameters of the model. Then, its optimal decision and so its optimal number of alliances may vary by period. Indeed, the sensitivity of a firm's optimal number of alliances to changes in structural model parameters may differ between close and distant learning horizons.

To examine such a dynamic effect, we focus our attention on b, c, and σ_T^2 because dynamic implications of changes in the variance of an observation σ_x^2 are indefinite. We first obtain the partial derivatives of η^* with respect to the structural parameters a (capturing b and c) and σ_T^2 and then use the properties of $f(\eta)$ to compare these partial derivatives to equations (10) and (11), respectively. For a close learning horizon, the relevant partial derivatives of η^* are

$\dfrac{\partial \eta^*}{\partial a} = \left(\sigma_x^2\right)^{1/3}$ and $\dfrac{\partial \eta^*}{\partial \sigma_T^2} = \dfrac{\sigma_x^2}{\sigma_T^4}$. Next, recall that $f\left(\eta^{**}\right) = \sigma_x^2 \cdot \dfrac{\left(\sigma_x^2 + \sigma_\upsilon^2\right)}{\left(\sigma_\upsilon^2 + \eta^{**}\sigma_x^2\right)} < \sigma_x^2$, which means that

the numerator of the expression $\dfrac{\left(f\left(\eta^{**}\right)\right)^k}{1 - \dfrac{\partial f\left(\eta^{**}\right)}{\partial \eta^{**}}\left(\dfrac{a}{3} f\left(\eta^{**}\right)^{-2/3} - \dfrac{1}{\sigma_T^2}\right)}$, which itself appears as the

numerator in the respective partial derivates of η^{**} (equations (10) and (11)), is smaller than

$\left(\sigma_x^2\right)^k$, where $k \in \left\{1/3, 1\right\}$. The denominator, i.e., $1 - \dfrac{\partial f\left(\eta^{**}\right)}{\partial \eta^{**}}\left(\dfrac{a}{3} f\left(\eta^{**}\right)^{-2/3} - \dfrac{1}{\sigma_T^2}\right)$, is larger than 1

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because $\dfrac{\partial f\left(\eta^{**}\right)}{\partial \eta^{**}}<0$, and $\left(\dfrac{a}{3}f\left(\eta^{**}\right)^{-\frac{2}{3}}-\dfrac{1}{\sigma_T^2}\right)>0$ in a high tech industry. Therefore, a

comparison of the relevant first order derivatives of η^{*} and η^{**} with respect to b, c, and σ_T^2

generates the following proposition:

Proposition 3. *In a high tech industry, the optimal number of alliances is less sensitive to*

changes in the structural parameters b, c, and σ_T^2 when a firm has a distant rather than

a close learning horizon (i.e., $0<\dfrac{\partial \eta^{**}}{\partial a}<\dfrac{\partial \eta^{*}}{\partial a}$ and $0<\dfrac{\partial \eta^{**}}{\partial \sigma_T^2}<\dfrac{\partial \eta^{*}}{\partial \sigma_T^2}$).

The ordering of the first-order derivatives in proposition 3 implies that a firm's optimal number

of direct partners is expected to be more stable—i.e., less sensitive to changes in b, c, and σ_T^2—

if the firm learns both from direct and indirect partners. To see why this happens, note that our

Bayesian model and the resulting Nash equilibrium explicitly account for firms considering the

alliance formation behavior of their direct partners. Indeed, even though parameters b, c, and σ_T^2

are assumed exogenous to individual firms, in the case of a distant learning horizon, a focal firm

calibrates optimal alliance formation in part based on its expectations concerning partners'

alliance formation. Because in that case, a firm can benefit from learning from indirect partners,

it will determine optimal alliance formation keeping in mind such indirect learning benefits.

These indirect benefits are absent in the case of a close learning horizon, which in turn gives rise

to the contrast between close and distant learning horizons as summarized in proposition 3.

For example, let us assume that perceived technological uncertainty σ_T^2 increases, which

represents an exogenous shock that might be due to, for example, the discovery of an additional

trajectory within a technological paradigm. By equations (3) and (6), the effect of such a shock

would be to increase the posterior variance of T—i.e., the residual technological uncertainty faced by the firm. Equations (4) and (8) indicate that such an increase in σ_T^2 is a motivation for the firm to increase its number of alliances, both for close and distant learning horizons. Crucially though, the partners of the firm will be similarly motivated and so in case of a distant learning horizon, the firm's increased learning requirement will be satisfied in part by its partners' alliance formation. In our model, the optimal number of alliances in the resulting equilibrium explicitly takes into account the alliance formation patterns of partners. Compared to a close learning horizon, this is the mechanism reducing variance in the focal firm's optimal number of alliances under a distant learning horizon. A similar line of reasoning holds for the effects of parameters b and c. Compared to a close learning horizon, a firm's distant learning horizon in a high tech industry therefore acts as a buffer from changes in several structural model parameters because in equilibrium the firm accounts for partners' responses to such changes.

6. GENERALIZING THE MODEL

6.1 Heterogeneous Alliance Formation

Thus far, we have assumed that $\omega = \eta$ in order to obtain a symmetric Nash equilibrium, while we also treated a focal firm as having access to $\omega - 1$ indirect partners. First, even if $\omega = \eta$, the latter assumption is restrictive because some of partners' direct partners may be 'redundant' from the perspective of a focal firm, in that they might themselves be direct partners of the firm as well (Ahuja 2000; Walker et al. 1997). Moreover, multiple direct partners might have alliances with one and the same indirect partner. In both scenarios, a focal firm's number of non-redundant, unique indirect partners will be smaller than $\omega - 1$. Second, the assumption that $\omega = \eta$ is itself restrictive because firms tend to differ in their number of alliance partners (e.g., Roijakkers and Hagedoorn 2006; Kapoor and McGrath 2014; Powell et al. 1996). Such heterogeneity may be, for

example, due to differences in the costs firms incur to form, operate, and terminate an alliance. Indeed, though to this point we have interpreted the cost c as a parameter that is stable both across alliances as well as across firms, this stability assumption can be relaxed without loss of generality.[3] In this Section, we generalize our model to allow explicitly for heterogeneous alliance formation.

Let $\varpi - 1$ be the average number of indirect partners that are 'non-redundant' from the perspective of a focal firm. Then, by equation (7) a firm's optimal number of alliances is given by

$$(14) \quad \eta^{\dagger} = a \cdot f(\varpi)^{\frac{1}{3}} - \frac{f(\varpi)}{\sigma_T^2},$$

where $f(\varpi) = \sigma_x^2 \cdot \dfrac{\left(\sigma_\upsilon^2 + \sigma_x^2\right)}{\left(\sigma_\upsilon^2 + \varpi \sigma_x^2\right)}$. In this setting, propositions 1 and 2 will hold if $f(\varpi) < \sigma_x^2$, which

requires that the number of unique indirect partners is positive, i.e. $\varpi - 1 > 0$. This condition will be satisfied if it is possible for the direct partners of a firm to give access to at least strictly more than an average of zero non-redundant, unique indirect partners. The opportunity for non-redundancy appears to be a weak requirement, first, given the hundreds and often thousands of firms populating many industries (e.g., United States Census Bureau 2012). Second, empirical research shows that non-redundancy is prevalent even in networks with high degrees of local redundancy, due to the propensity of some firms to form 'bridging' ties across otherwise disconnected parts of an alliance network (e.g., Powell et al. 2005; Rosenkopf and Padula 2008; Schilling and Phelps 2007; Sytch et al. 2011). In this more general model, then, not all direct partners of the firm are required to have unique partners themselves: even if only one of a firm's direct partners has one unique partner itself, a distant learning horizon can exist and so the necessary conditions for propositions 1 and 2 are replicated. Therefore, by relaxing the symmetry

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[3] Specifically, this more general assumption amounts to interpreting c as the *expected* cost of forming, operating, and terminating an alliance.

condition through allowing $\varpi \neq \eta$, we impose much weaker sufficiency conditions on propositions 1 and 2.

This generalization of our model to account for heterogeneous alliance formation allows for a descriptive comparison between key implications of propositions 1 and 2 and performance in empirically-observed alliance portfolios. One key implication of proposition 1 is that in a high tech industry the number of direct alliance partners optimal for technological learning is *smaller* for firms with a more extensive learning horizon. This implication is fully consistent with results in Ahuja (2000) and Vanhaverbeke et al. (2012), suggesting that the number of direct alliance partners optimal for learning in a number of technology-intensive industries during 1981-1996 was smaller for firms with greater numbers of indirect partners. One key implication of proposition 2 is that in a low tech industry the optimal number of direct alliance partners is instead *greater* for firms with a more extensive learning horizon. Consistent with this implication, Koka and Prescott (2008) show that in the low tech steel industry during 1980-94, firms that simultaneously had greater numbers of direct as well as indirect partners outperformed others, and this effect was even more pronounced during periods of environmental stability.

We now turn to generalizing proposition 3. Given that $\frac{\partial \eta^*}{\partial a} = \left(\sigma_x^2\right)^{1/3}$, it is straightforward to show that

$$(15) \qquad \frac{\partial \eta^\dagger}{\partial a} = f(\varpi)^{1/3} + \left(\frac{a}{3} f(\varpi)^{-2/3} - \frac{1}{\sigma_T^2}\right) \cdot \frac{\partial f(\varpi)}{\partial \varpi} \cdot \frac{\partial \varpi}{\partial a} \leq \frac{\partial \eta^*}{\partial a} + \left(\frac{a}{3} f(\varpi)^{-2/3} - \frac{1}{\sigma_T^2}\right) \cdot \frac{\partial f(\varpi)}{\partial \varpi} \cdot \frac{\partial \varpi}{\partial a} \ .$$

Furthermore, $\frac{\partial f(\varpi)}{\partial \varpi} = -\sigma_x^4 \cdot \frac{\left(\sigma_x^4 + \sigma_x^2 \sigma_v^2\right)}{\left(\sigma_v^2 + \varpi \sigma_x^2\right)^2} < 0$ and in a high tech industry $\left(\frac{a}{3} f(\varpi)^{-2/3} - \frac{1}{\sigma_T^2}\right) > 0$.

Thus, it follows that $\frac{\partial \eta^\dagger}{\partial a} \leq \frac{\partial \eta^*}{\partial a}$ if $\frac{\partial \varpi}{\partial a} > 0$ and so if both $\frac{\partial \eta^\dagger}{\partial a} > 0$ and $\frac{\partial \varpi}{\partial a} > 0$, then the main features of proposition 3 are replicated. In practice, this requires that both a firm and its average

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partner increase their number of alliances in response to an increase in the parameter $a = \left(\dfrac{b}{2c}\right)^{2/3}$,

reflecting an increase in the cost of residual technological uncertainty b relative to the cost of

alliances c.

Similarly, because $\dfrac{\partial \eta^*}{\partial \sigma_T^2} = \dfrac{\sigma_x^2}{\sigma_T^4}$,

(16) $\quad \dfrac{\partial \eta^\dagger}{\partial \sigma_T^2} = \dfrac{f(\varpi)}{\sigma_T^4} + \left(\dfrac{a}{3} f(\varpi)^{-2/3} - \dfrac{1}{\sigma_T^2}\right) \cdot \dfrac{\partial f(\varpi)}{\partial \varpi} \cdot \dfrac{\partial \varpi}{\partial \sigma_T^2} \le \dfrac{\partial \eta^*}{\partial \sigma_T^2} + \left(\dfrac{a}{3} f(\varpi)^{-2/3} - \dfrac{1}{\sigma_T^2}\right) \cdot \dfrac{\partial f(\varpi)}{\partial \varpi} \cdot \dfrac{\partial \varpi}{\partial \sigma_T^2}.$

As in the above, if both $\dfrac{\partial \eta^\dagger}{\partial \sigma_T^2} > 0$ and $\dfrac{\partial \varpi}{\partial \sigma_T^2} > 0$, the sensitivity of a firm's number of alliances in

case of a distant learning horizon is lower than that of a close learning horizon, i.e., $\dfrac{\partial \eta^\dagger}{\partial \sigma_T^2} \le \dfrac{\partial \eta^*}{\partial \sigma_T^2}$.

Under these two fairly general assumptions, the key properties of proposition 3 are

replicated, generating the following proposition:

Proposition 4. *In a high tech industry, if alliance formation is <u>heterogeneous</u> (i.e., $\varpi \ne \eta$)*

and firms are <u>homogeneous</u> in the sign of their sensitivity (i.e., both $\dfrac{\partial \eta^\dagger}{\partial a} > 0$ and

$\dfrac{\partial \varpi}{\partial a} > 0$, *and both* $\dfrac{\partial \eta^\dagger}{\partial \sigma_T^2} > 0$ *and* $\dfrac{\partial \varpi}{\partial \sigma_T^2} > 0$ *), then the optimal number of alliances is*

less sensitive to changes in the structural parameters b, c, and σ_T^2 when a firm has a

distant rather than a close learning horizon (i.e., $0 < \dfrac{\partial \eta^\dagger}{\partial a} < \dfrac{\partial \eta^*}{\partial a}$ *and* $0 < \dfrac{\partial \eta^\dagger}{\partial \sigma_T^2} < \dfrac{\partial \eta^*}{\partial \sigma_T^2}$ *).*

Therefore, once we allow for heterogeneous alliance formation, which only introduces weak

additional constraints, the influence of a firm's learning horizon on the sensitivity of the firm's

optimal number of alliances to changes in structural model parameters is identical in proposition

4 compared to proposition 3. One key implication of proposition 4 is that relative to a firm with a more restricted learning horizon, a firm with a more extensive learning horizon benefits more from a given level of inter-temporal stability in its number of direct alliance partners. As an illustrative example, consider Advanced Micro Devices Inc. (AMD) and National Semiconductor Corporation (NSC) during 1977-99.[4] Both firms operated mainly in the semiconductors subsector of the high tech information technology industry, a setting that has historically experienced great variation in the level of technological uncertainty, the cost of residual technological uncertainty, and the cost of alliances (e.g., Bresnahan and Greenstein 1999; Frankort 2013; Grove 1996; Kapoor 2013; Schilling 2015; Sytch et al. 2011), and so we might expect *a priori* that the learning horizon may have an effect consistent with proposition 4.

AMD and NSC were similar on a number of dimensions. For example, both had their home in Silicon Valley and were among few semiconductors companies having remained independent by the end of the 1970s (Chandler 2005). Moreover, average annual R&D investments were similar between the two firms, at around $235MM, while both divided their alliance activities across IT subsectors in comparable ways, with around 80% of the alliances in microelectronics. They also had similar shares of contractual alliances compared to joint ventures. Finally, the extent to which partners had alliances among themselves—i.e., the density of the two alliance portfolios—was comparable as well. Despite all such similarities, however, AMD on average outperformed NSC by about 80% on patent-based measures of technological learning, which raises the question: what might explain such a differential? Our theory related to proposition 4 would predict that part of the difference in technological learning may have been due to the comparatively greater benefit AMD derived from the stability in its number of direct

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[4] We developed this brief comparative case example based on combined data drawn from the Cooperative Agreements and Technology Indicators database (alliance data, 1977-99), the NBER patent data file (data on technological learning in IT, 1977-99), as well as searches of historical annual reports in Mergent Online and Mergent Archives (additional data, 1978-99). Details are available upon request.

partners, afforded by a more extensive distant learning horizon. Indeed, though the alliance portfolios of both firms were equally stable in terms of inter-temporal variance in numbers of direct partners, the extent of the learning horizon of AMD, in terms of numbers of indirect partners per direct partner, was on average more than 1.2 times that of NSC.

6.2 Incomplete Awareness

In his classic treatment of interorganizational relationship formation, Van de Ven (1976, p. 31, italics added) noted that "organizations must be *aware* of possible sources…where their needed resources can be obtained; otherwise organizational directors are likely to conclude that the goal or need which motivates the search for resources cannot be attained." To this point, we have treated firms' awareness of indirect partners strictly dichotomously: firms are either unaware (i.e., a close learning horizon) or fully aware of all their non-redundant, unique indirect partners (i.e., $\varpi > 1$). However, there can be a discrepancy between a firm's total number of unique indirect partners (i.e., $\eta \cdot (\varpi - 1)$) and those that the firm knows to exist.[5] In this Section, we focus on a further generalization of our model to account for incomplete awareness.

To incorporate incomplete awareness into our theory, it suffices to let $\varpi' - 1$ be the average number of non-redundant indirect partners that a focal firm is aware of. It is straightforward to see that the necessary conditions for propositions 1 and 2 are replicated if $\varpi' > 1$. Hence, regardless of a firm's actual number of unique indirect partners, as soon as it is aware of at least one such partner (i.e., $\varpi' > 1$), propositions 1 and 2 will hold. Turning to proposition 4, if ϖ' rather than ϖ is the relevant parameter from the standpoint of a firm facing an alliance formation decision, the features of proposition 4 are replicated if a firm with a greater

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[5] This possibility is fully consistent with the literature on competitor identification, suggesting that cognitive limitations may lead to discrepancies between firms' industry environments and cognitive models of such environments (Porac et al. 1995), which can have consequences for firm decision making (Zajac and Bazerman 1991). To date, the implications of such cognitive constraints have remained largely unaddressed in the alliance literature (Westphal 2008).

number of unique indirect partners is aware of more such partners than a firm with a smaller

number of unique indirect partners, i.e., $corr(\varpi, \varpi') > 0$. This assumption is reasonable because

the alliance portfolio of a firm with a greater number of partners should be more visible than that

of a firm with a smaller number of partners.

Because σ_υ^2 represents the inverse of a firm's ability to learn from indirect partners, we

can now be more precise in our distinction between close and distant learning horizons. If a firm

is unaware of unique indirect partners (i.e., $\varpi' = 1$), then its ability to learn from them is

irrelevant and so the firm has a close learning horizon. Instead, if the firm is aware of at least one

unique indirect partner (i.e., $\varpi' > 1$) *and* it is able to learn from that partner (i.e., $\sigma_\upsilon^2 < \infty$), then it

has a distant learning horizon. Therefore, neither awareness nor ability alone is sufficient for a

firm to act on the learning potential afforded by non-redundant indirect partners. In particular, all

effects summarized in propositions 1, 2, and 4 will hold if both $\varpi' > 1$ and $\sigma_\upsilon^2 < \infty$.

Though our labeling of learning horizons as close or distant at first blush suggests that the

learning horizon concept has a strictly binary interpretation, the extent of the learning potential

associated with different learning horizons actually represents a continuum, with three boundary

scenarios. First, firms without indirect partners, those that have indirect partners yet without

awareness of them, or those that have indirect partners yet without the ability to learn from them

have the most restricted learning horizon, which we labeled a close learning horizon. Second,

firms that are aware of one unique indirect partner and are at least minimally able to learn from

that partner have the most restrictive distant learning horizon. Third, firms with many indirect

partners that they are both aware of and able to learn from have the most extensive distant

learning horizon.

7. DISCUSSION

To begin to consider the role of indirect partners in optimal alliance portfolio design (e.g., Lavie 2006: 651), we asked how learning from indirect partners influences a firm's optimal number of direct partners in the face of technological uncertainty. Our formal Bayesian learning model of optimal alliance formation demonstrated, first, that a firm's learning horizon has distinct normative implications for optimal alliance formation depending on the firm's specific industry context. In a high tech industry, where technological uncertainty is comparatively high, residual uncertainty is costly, and where alliances are a comparatively affordable and effective solution to technological uncertainty, firms with a distant learning horizon can substitute alliance ties to indirect partners for those with direct partners. In contrast, in a low tech industry, where technological uncertainty is comparatively low, residual uncertainty is less costly, and where alliances are a comparatively costly and ineffective solution to technological uncertainty, alliance ties to direct and indirect partners act as complements. These basic implications of our model resonate with recent literature analyzing complementarities across firms' learning activities (e.g., Cassiman and Veugelers 2006), by suggesting that the question of whether alliance ties to direct and indirect partners are complements or substitutes must be answered with reference to relevant contextual variables (Ahuja 2000, pp. 450-451).

Second, our model implies that in a high tech environment and relative to a firm with a more restricted learning horizon, a firm with a more extensive learning horizon benefits more from a given level of inter-temporal stability in its number of direct alliance partners. In particular, given a distant learning horizon, the optimal number of direct partners of a firm in a high tech industry will be more robust to inter-temporal changes in the cost of residual technological uncertainty, the cost of alliances, and the perceived level of technological uncertainty. Therefore, in high tech industries, the inter-temporal stability of some firms' alliance

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activities may be understood as the strategically optimal outcome (in the Bayesian sense) of firms' efforts to reduce technological uncertainty. Our novel strategic explanation for inter-temporal stability in firms' alliance activities complements prior research that has often discussed such stability in terms of embeddedness and inertia mechanisms (e.g., Gulati and Gargiulo 1999; Hagedoorn 2006; Kim et al. 2006).

Our treatment of the learning horizon concept captures in an integrative way various factors of importance when considering the role of indirect partners in optimal alliance portfolio design. At a basic level, it allows firms to vary in their number of indirect partners for a given number of direct partners. Though existing research has already begun to account for such a possibility (Ahuja 2000; Vanhaverbeke et al. 2012), it has nevertheless implicitly assumed that firms' learning from indirect partners is purely a function of the number of such partners. More broadly, it has tended to assume that knowledge flows fairly easily beyond individual alliance dyads, for example, between indirectly connected firms (Ghosh and Rosenkopf 2014). However, a firm with five indirect partners may be aware of all five yet have a limited ability to learn from them, while an otherwise identical firm may be aware of only two indirect partners yet have a strong ability to learn from these two. To account for such heterogeneity, our model formally incorporates as relevant parameters the extent to which firms are aware of and able to learn from their indirect partners. This way, our theory facilitates a refocusing, away from the assumption that firms' learning from indirect partners is a direct function of the actual number of such partners, towards a more nuanced account that considers both firms' cognitive limitations in observing other firms (Westphal 2008) as well as limitations in learning from them (Burt 2010; Ghosh and Rosenkopf 2014).

Further opportunities exist to extend our research as well as address some of its limitations. First, in part because our approach has been theoretical, it will be important to subject

the predictions of our theoretical model to empirical testing. For example, though a few prior studies appear generally consistent with propositions 1 and 2, research in low tech industries is limited as is the systematic study of factors such as the awareness of and ability to learn from indirect partners. Moreover, while the consistency of our brief comparative case of AMD versus NSC with proposition 4 is promising (Section 6.1), empirical refutation through a large-scale empirical design would be necessary. Such empirical tests might answer a number of related questions: Do measures of firms' learning horizon predict alliance formation and firm learning? Can they predict the inter-temporal stability of firms' alliance portfolio size? If so, then how will such effects vary across industries with different levels of technological uncertainty? Reliance on secondary data may not suffice to address such questions because learning horizons can vary in their extent with the awareness of and ability to learn from indirect partners. Thus, surveys may be used to gauge firms' view of the partner landscape (e.g., Lhuillery and Pfister 2011).

Second, our model is based on the assumption that within a technological paradigm, it is eventually possible to discern one optimal technological trajectory. This assumption is reasonable in light of multiple and diverse corroborative industry cases (e.g., Anderson and Tushman 1990; Cusumano et al. 1992; Suarez and Utterback 1995). Nonetheless, it is of course possible that, at least in the intermediate term, multiple trajectories cannot easily be distinguished based on projections regarding their feasibility, marketability, and profitability. Future research might account for the possibility of multiple concurrent optimal trajectories in the intermediate term, which mathematically amounts to defining T to be a vector of values (e.g., Raiffa and Schlaifer 1961; Zellner 1971). We speculate that our results will remain similar in spirit under the assumption that the elements of the vector of optima are somehow positively correlated, such that observations obtained through alliances at once allow firms to update their beliefs about all conceivable optima. In practice, this is plausible either if the technologies underlying multiple

optimal trajectories are comparable on at least a subset of all relevant technological dimensions or if they are complementary in defining a common application domain (e.g., Kodama 1991).

In conclusion, our study extends the alliance literature by offering a formal and integrative account of the role of indirect partners in optimal alliance portfolio design, generating several normative propositions amenable to future empirical refutation. We hope our theory offers an impetus for further exploration of the effects of firms' learning horizon on the formation and consequences of alliances by firms faced with technological uncertainty.

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APPENDIX: DERIVATION OF THE POSTERIOR VARIANCE (EQUATION (3))

Suppose the covariance matrix for the observations x_1, x_2, ... , x_η is given by Σ_x^η. Each variable x_i is normally distributed with mean T and variance $\sigma_{x_i}^2$. The posterior distribution function is

$$f(x_1,...,x_\eta,T) = f(x_1,...,x_\eta \mid T) \cdot f(T) \propto \exp\left(-\frac{1}{2}(x - \iota T)^T (\Sigma_x^\eta)^{-1}(x - \iota T)\right) \cdot \exp\left(-\frac{1}{2}\frac{(T - \mu)^2}{\sigma_T^2}\right),$$

where ι is an η by 1 vector whose elements contain the number 1 and x is an η by 1 vector containing the observations x_i. To determine the posterior variance of T it suffices to collect all

terms that involve T^2, i.e., $\left(\iota^T (\Sigma_x^\eta)^{-1}\iota + \frac{1}{\sigma_T^2}\right)T^2$. Because we assume that observations are

independently and identically distributed, $\left(\iota^T (\Sigma_x^\eta)^{-1}\iota + \frac{1}{\sigma_T^2}\right)T^2 = \left(\sum_{i=1}^{\eta}\frac{1}{\sigma_x^2} + \frac{1}{\sigma_T^2}\right)T^2$. Therefore, the

posterior variance of T is equal to $\sigma_\eta^2 = \left(\frac{\eta}{\sigma_x^2} + \frac{1}{\sigma_T^2}\right)^{-1}$.

AUTHOR BIOGRAPHIES

Hans T. W. Frankort is Associate Professor (Senior Lecturer) in Strategy at Cass Business School, City University London. His main research focuses on the determinants and consequences of interorganizational relationships, with particular emphasis on research and development alliances in technology-intensive industries. His work has appeared in *Academy of Management Journal*, *Advances in Strategic Management*, *Industrial and Corporate Change*, and *Research Policy*, among others.

John Hagedoorn is Professor of Strategy and International Business at the School of Management, Royal Holloway University of London. He is also a Professorial Fellow at the Maastricht Economic Research Institute on Innovation and Technology (UNU-MERIT) and Professor Emeritus at the School of Business and Economics, Maastricht University. His research focuses on interfirm partnerships and contract law, mergers and acquisitions, innovation and technological change, and international strategy. His work has appeared in *Academy of Management Journal*, *Academy of Management Review*, *Advances in Strategic Management*, *Business History*, *Business History Review*, *Global Strategy Journal*, *Industrial and Corporate Change*, *International Journal of Industrial Organization*, *Journal of Economic Behavior and Organization*, *Journal of Financial Economics*, *Journal of International Business Studies*, *Journal of Management Studies*, *Organization Studies*, *Research Policy*, *Small Business Economics*, *Strategic Management Journal*, and *Strategic Organization*, among others.

Wilko Letterie is Associate Professor at the School of Business and Economics, Maastricht University. His research focuses on factor demand decisions and alliance formation under uncertainty. His work has appeared in *Economica*, *Industrial and Corporate Change*, *Journal of Economic Behavior and Organization*, *Journal of Law, Economics, and Organization*, *Journal of Monetary Economics*, *Research Policy*, *The Review of Economics and Statistics*, *Small Business Economics*, and *Strategic Organization*, among others.